

ADAMS' NEW

ARITHMETIC,

SUITED TO HALIFAX CURRENCY;

IN WHICH THE

PRINCIPLES OF OPERATING BY NUMBERS

ARE

ANALYTICALLY EXPLAINED,

AND

SYNTHETICALLY APPLIED:

THUS

COMBINING THE ADVANTAGES

TO BE DERIVED BOTH FROM

THE INDUCTIVE AND SYNTHETIC MODE OF INSTRUCTING:

THE WHOLE

MADE FAMILIAR BY A GREAT VARIETY OF USEFUL AND INTERESTING

EXAMPLES, CALCULATED AT ONCE TO ENGAGE THE PUPIL IN

THE STUDY, AND TO GIVE HIM A FULL KNOWLEDGE

OF FIGURES IN THEIR APPLICATION TO ALL THE PRACTICAL PURPOSES OF LIFE.

DESIGNED FOR THE USE OF SCHOOLS AND ACADEMIES IN THE BRITISH PROPINGES.

BY DANIEL ADAMS, M. D.

PUBLISHED BY WALTON & GAYLORD.

1833.

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PREEDA OU.

THERE are two methods of teaching: the synthetic and the analytic. In the synthetic method, the pupil is first presented with a general view of the science he is studying, and afterwards with the particulars of which it consists. The analytic method reverses this order: the pupil is first presented with the particulars, from which he is led, by certain natural and easy gradations, to those views which are more general and comprehensive.

The Scholar's Arithmetic published in 1801, is synthetic. If that is a fault of the work, it is a fault of the times in which it appeared. The analytic or inductive menthod of teaching, as now applied to elementary instruction, is among the improvements of later years. Its introduction is ascribed to PESTALOZZI, a distinguished teacher in Switzerland. It has been applied to arithmetic, with great ingenuity,

by Mr. Colburn, in our own country.

The analytic is unquestionably the best method of acquiring knowledge; the synthetic is the best method of recapitulating or reviewing it. In a treatise designed for school education, both methods are useful. Such is the plan of the present undertaking which the author, occupied as he is with other objects and pursuits, would willingly have forborne, but that, the demand for the Scholar's Arithmetic still continuing, an obligation, incurred by long-continued and extended patronage, did not allow him to decline the labor of a revisal, which should adapt it to the present more enlightened views of teaching this science in our schools. In doing this, however, it has been necessary to make it a new work.

In the execution of this design, an analysis of each rule is first given, containing a familiar explanation of its various principles; after which follows a synthesis of these principles, with questions in form of a supplement. Nothing is taught dogmatically; no technical term is used till it has first been defined, nor any principle inculcated without a previous developement of its truth; and the pupil is made to understand

the reason of each process as he proceeds.

The examples under each rule are mostly of a practical nature, beginning with those that are very easy, and gradually advancing to those more difficult, till one is introduced containing larger numbers, and which is not easily solved in the mind; then in a plain, familiar manner, the pupil is shown how the solution may be facilitated by figures. In this way he is made to see at once their use and their application.

At the close of the fundamental rules, it has been thought advisable to collect into one clear view the distinguishing properties of those rules, and to give a number of examples involving one or more of them. These exercises will prepare the pupil more readily to understand the application of these to the succeeding rules; and, besides, will serve to interest him in the science, since he will find himself able, by the application of a very few principles, to solve many curious questions.

The arrangement of the subjects is that, which to the author has appeared most natural. Fractions, have received all that consideration which their importance demands. The principles of a rule called Practice are exhibited, but its detail of cases omitted, as unnecessary since the adoption and general use of federal money. The Rule of Three, or Proportion, is retained and the solution of questions involving the principles of proportion, by analysis, is distinctly shown.

The articles Alligation, Arithmetical and Geometrical Progression, Annuities and Permutation, were prepared by Mr. IRA Young, a member of Dartmouth College, from whose knowledge of the subject, and experience in teaching, I have derived important aid in other parts of

the work.

The numerical paragraphs are chiefly for the purpose of reference; these references the pupil should not be allowed to neglect. His attention also ought to be particularly directed, by his instructer, to the illustration of each particular principle, from which general rules are deduced; for this purpose, recitations by classes ought to be instituted in every school where arithmetic is taught.

The supplements to the rules, and the geometrical demonstrations of the extraction of the square and cube roots, are the only traits of

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PUBLISHERS' PREFACE.

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THE author of the following practical treatise upon Arithmetic, has made himself favorably known in the United States and to a considerable extent in the Canadas, for a great number of years, by his works, designed for the use of Academies and primary schools. The "Scholars' Arithmetic," published in the year 1801, continued in almost universal use, until within a very short time past. But juster views beginning to prevail, and sounder principles becoming established in the public mind, upon the subject of elementary education, a revision of the work seemed necessary. At this time, "Adams' New Arithmetic," was published .-This seems evidently to have been prepared with much care. The author has recognized in it throughout, this important law in relation to the mind, that it must first be made acquainted with particular facts, or there will be no ability to arrive at correct general conclusions. Particular examples are therefore given upon each subject, and from them, in a manner obvious to the young mind, all the general rules are deduced. In other words, the author has carefully and prudently pursued, in his book, what is called the analytic method. The care used in defining necessary terms, which might not be quite clear, the practical character of the examples given under each rule, the methodical disposition of the different parts of each subject, and of the different subjects, the general perspicuity, simplicity and accuracy of the work, render it invaluable to the pupil.

It is due the author to observe, that "Adams' New Arithmetic," for its adaptation to the capacities of young and ordinary minds, is justly considered the best practical treatise

which has been offered to the public.

In the present edition, the main purpose in view was to adapt Adam's work to the currency of the British Provinces. No separate article, as in the original, has been allotted to Federal Money; for this the pupil has been referred to Decimal Fractions, in which also almost all the examples will be found in the money of the United States.—Additional examples in the compound rules have been giv-

en, and the old ones retained, under the title of Halifax currency; and generally, throughout the book, where denominations of money occur, Halifax currency has been

substituted for Federal Money.

The rules and examples in Reduction of Currencies have been essentially changed; and in Reduction, after the Table of English Money, which is called the Table of Halifax Currency, a list of the Gold and Silver Coins current in the Province, has been inserted. This may be depended upon as entirely accurate. The tables of French, and Dry, Long, Square, and Solid Measure, have been given—and what are the weights and measures established by law in this Province is also stated.

The most novel feature in the book will be found in the rule of Interest. Certainly an innovation, but it is believed, an improvement, has been made. The pounds in any given sum upon which interest is to be cast, are left to stand as the units, and the shillings and pence are reduced to decimal parts of a pound. The interest is then obtained the same as in Federal Money, and the decimal parts in the result reduced to shillings and pence. It is considered, that this method is more simple, and concise, and will be found in practice to be more convenient than any other. But setting aside considerations of temporary convenience, if this change and attempted amelioration, shall assist in some very slight degree in turning men's minds toward the Decimal Ratio, and inducing them to look forward to a period when all the denominations of money, weights and measures, throughout the world, shall be expressed in DECIMALS, it cannot be affirmed that no benefit has been obtained:

The importance of the principal and essential alteration in the book, viz. the adaptation of it to the currency of the country, will not fail to be observed by every one. It is indeed singular, that hitherto, no Canadian Arithmetic in the English language, has been published. Mercantile, agricultural, and generally the business men of the country, will be aware of a benefit to be realized, and it is considered that something also bearing a relation to political advan-

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Stanstead, L. C. Aug. 1, 1833.

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NUMERATION.

T1. A SINGLE or individual thing is called a unit, unity, or one; one and one more are called two; two and one more are called three; three and one more are called four; four and one more are called five; five and one more are called six; six and one more are called seven; seven and one more are called eight; eight and one more are called nine; nine and one more are called ten, &c.

These terms, which are expressions for quantities, are called numbers. There are two methods of expressing numbers shorter than writing them out in words; one called the Roman method by letters,* and the other the Arabic method by figures. The latter is that in general use.

In the Arabic method, the nine first numbers have each an appropriate character to represent them. Thus,

"In the Roman method by letters, I represents one; V, five; X. ten; L, fifty; C, one hundred; D, five hundred; and M, one thousand.

As often as any letter is repeated, so many times is its value repeated, unless it be a letter representing a less number, placed before one representing a greater; then the less number is taken from the greater, thus IV represents four, IX nine, &c., as will be seen in the following

A military	MR. Links	TABLE.	Service Military or seem
One	I.	Ninety.	LXXXX, or XC.
Two	ii.	One bundred	C.
Three	III.	Two hundred	CC.
Four	IIII, or IV.	Three hundred	CCC.
Five	V.	Four hundred	CCCC.
Six	VI.	Five hundred	D, or Io.*
Seven	VII.	Six hundred	DC.
Eight	VIII.	Seven hundred	DCC.
Nine	VIIII, or IX.	Eight hundred	DCCC.
Ten	X.	Nine hundred	DCCCC.
Twenty	XX.	One thousand	M, or Clast
Thirty	XXX.	Five thousand	100. or V.;
Forty	XXXX. or XI	.Ten thousand	
Fifty	nio L. saludo), seini		CCIAO, or X.
The state of the s		Fifty thousand	I000.
Sixty	LX.	Hundred thousa	hdCCCIDDD, or C.
Seventy	LXX.	One million	M. male of her
Eighty	LXXX.	Two millions	MM. della
A Company			

¹⁰ is used instead of D to represent five hundred, and for every additional annexed at the right hand, the number is increased ten times.

t Clo is used to represent one thousand, and for every C and o put at each end, the number is increased ten times.

A line drawn over any number increases its value one thousand times.

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A unit, u	nity, or	one.	is ren	resent	ted b	v this	character	1.
Two	•			•	•	•		2.
Three	•							3.
Four								4.
Five	•							5.
Six								6.
Heven								7.
Eight			•					8.
Nine			•					9
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with	h ce it-	write,	in th	e plac	e or t	inits,	a cipher, 0,	10
One ten	h of its	eir si	gnine	s noti	nng	; thus		10.
One ten a					•	•	Eleven	11.
One ten a						•	Twelve	12.
One ten a					1	•	Thirteen	13.
One ten a					•	•	Fourteen	
One ten a					٠	•	Fifteen	15.
One ten a						•	Sixteen	16.
One ten a						•	Seventeen	
One ten a					1	•	Eighteen	
One ten a			are	called		•	Nineteen	19.
Two tens			•	•	•	•	Twenty	20.
Three ten			• ,	•	•	•	Thirty	30.
Four tens			•	•	•	•	Forty	40.
Five tens			•		•	•	Fifty	50.
Six tens a			•	•	•	•	Sixty	60.
Seven ten			•	•	•	•	Seventy	70.
Eight tens			•	•	•	•	Eighty	80.
Nine tens			•			•	Ninety	90.
Ten tens a								
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n 16. teen 17. een 18. een 19. y 20.

50. 40. 50. 60. 70.

80. 90. f a atof

> 100. 111.

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T 2. There are three hundred sixty-five days in a year. In this number are contained all the orders now described. viz. units, tens, and hundreds. Let it be recollected, units. occupy the first place on the right hand; tens, the second place from the right hand; hundreds, the third place. number may now be decomposed, that is, separated into parts. exhibting each order by itself, as follows:-The highest order, or hundreds, are three, represented by this character. 3; but, that it may be made to occupy the third place, counting from the right hand, it must be followed by two ciphers. thus, 300. (three hundred.) The next lower order, or tens, are six, (six tens are sixty,) represented by this character. 6: but, that it may occupy the second place, which is the place of tens, it must be followed by one cipher, thus 60, (sixty.) The lowest order, or units, are five, represented by a single character, thus, 5, (five.)

We may now combine all these parts together, first writing down the five units for the right hand figure, thus, 5; then the six tens (60) on the left hand of the units, thus 65; then the three hundreds (300) on the left hand of the six tens, thus, 365, which number, so written, may be read three hundred, six tens, and five units; or, as is more usual,

three hundred and sixty-five.

T 3. Hence it appears, that figures have a different value according to the place they occupy, counting from the right hand towards the left.

Hund. Tens. Units.

Take for example the number 3 3 3, made by the same figure three times repeated. The 3 on the right hand, or in the first place, signifies 3 units; the same figure, in the second place, signifies 3 tens, or thirty; its value is now increased ten times. Again, the same figure in the third place, signifies neither 3 units, nor 3 tens, but 3 hundreds, which is ten times the value of the same figure in the place immediately preceding, that is, in the place of tens; and this is a fundamental law in notation, that a removal of one place towards the left increases the value of a figure TEN TIMES.

Ten hundred make a thousand, or a unit of the fourth order. Then follow tens and hundreds of thousands, in the

7 3.

same manner as tens and hundreds of units. To thousands succeed millions, billions, &c., to each of which, as to units and to thousands, are appropriated three places,* as exhibited in the follwing examples:

Quadrillions.	Trillions.	Billions.	Millions.	Thousands.	of Units.
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& Units					
3,	174	, 5 9 2	,837		
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	or period of to the Quadrillions.	or period of \ Quadrillions. \(\begin{array}{c} \colon &	our period of Quadrillions. 'E Units 5th period, 7 1 Hundreds or period of Y 2 1 Tens Trillions. 4th period, 6 6 Tens or period of 8 6 Tens or period of 8 6 Tens	or period of Quadrillions. 'E Units 5th period of L 1 Hundreds or period of L 2 Tens Trillions. 4th Period, C 5 G Hundreds or period of C 6 G Tens Billions. 6 G Tens Sid period, 0 0 Hundreds or period of C 2 Units Millions. 2 Units	2

To facilitate the reading of large numbers, it is frequently practised to point them off into periods of three figures each, as in the 2d example. The names and the order of the periods being known, this division enables us to read numbers consisting of many figures as easily as we can read three figures only. Thus, the above examples are read 3 (three) Quadrillions, 174 (one hundred seventy-four) Trillions, 592 (five hundred ninety-two) Billions, 837 (eight hundred thirty-seven) Millions, 463 (four hundred sixty-three) Thousands, 512 (five hundred and twelve.)

After the same manner are read the numbers contained in the following Hundreds of Millions. Tens of Millions.

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This is according to the French method of counting. The English, after hundreds of millions, instead of proceeding to billions, reckon thousands, tens and hundreds of thousands of millions, appropriating six places, instead of three, to millions, billions, &c.

thousands

as to units * as exhi-

NUMERATION TABLE.

Those words at the head of the table are applicable to any sum or number, and must be committed perfectly to memory, so as to be readily applied on any occasion.

Of these characters, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, the nine first are sometimes called significant figures, or digits, in distinction from the last, which, of itself, is of no value, yet, placed at the right hand of another figure, it increases the value of that figure in the same ten fold proportion as if it had been followed by any one of the significant figures.

Note. Should the pupil find any difficulty in reading the following numbers, let him first transcribe them, and point them off into periods.

5768	52831209	286297314013
34120	175264013	5203845761204
701602	3456720834	13478120673019
6539285	25037026531	341246801734526

The expressing of numbers, (as now shown,) by figures, is called Notation. The reading of any number set down in figures, is called Numeration.

After being able to read correctly all the numbers in the foregoing table, the pupil may proceed to express the following numbers by figures:

1. Seventy-six.

2. Eight hundred and seven.

3. Twelve hundred, (that is, one thousand and two hundred.)

4. Eighteen hundred.

3 5 3 3, 5 1 Thousands. frequently figures each. r of the peread nume can read are read 3

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- 5. Twenty-seven hundred and nineteen.
- 6. Forty-nine hundred and sixty.
- 7. Ninety-two thousand and forty-five.
- 8. One hundred thousand.
- 9. Two millions, eighty thousands, and seven hundreds.
- 10. One hundred millions, one hundred thousand, one hundred and one.
 - 11. Fifty-two millions, six thousand, and twenty.
- 12. Six billions, seven millions, eight thousand, and nine hundred.
- 13. Ninety-four billions, eighteen thousand, one hundred and seventeen.
- 14. One hundred thirty-two billions, two hundred millions, and nine.
- 15. Five trillions, sixty billions, twelve millions, and ten thousand.
- 16. Seven hundred trillions, eighty-six billions, and seven millions.

addition

OF SIMPLE NUMBERS.

T 4. 1. James had five peaches, his mother gave him 3 peaches more; how many peaches had he then?

2. John bought one book for 9 pence, and another for 6 pence; how many pence did he give for both?

3. Peter bought a waggon for 10 shillings, and sold it so as to gain 4 shillings; how many shillings did he get for it?

4. Frank gave 15 walnuts to one boy, 8 to another, and had 7 left; how many walnuts had he at first?

5. A man bought a carriage for 54 pounds; he expended 8 pounds in repairs, and then sold it so as to gain 5 pounds; how many pounds did he get for the carriage?

6. A man bought 3 yoke of oxen; for the first he gave 16 pounds, for the second he gave 18 pounds, and for the third he gave 20 pounds; how many pounds did he give for the three!

7. Samuel bought an orange for four pence, and some walnuts for three pence; then he bought a knife for 1 shilling, and a book for 4 shillings; how many shillings did he spend, and how many pence?

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l some l shilldid he 8. A man had 3 calves worth 10 shillings each, 4 calves worth 15 shillings each, and 7 calves worth 2 pounds each; how many calves had he?

9. A man sold a cow for 4 pounds, some corn for 5 pounds, wheat for 7 pounds, and butter for 2 pounds; how many

pounds must be receive ?

The putting together two or more numbers, (as in the foregoing examples,) so as to make one whole number, is called Addition, and the whole number is called the sum, or amount.

10. One man owes me 5 pounds, another 6 pounds, another 14 pounds, and another 3 pounds; what is the amount due to me?

11. What is the amount of 4, 3, 7, 2, 8, and 9 pounds?

12. In a certain school 9 study grammar, 15 study arithmetic, 20 attend to writing, and 12 study geography; what is the whole number of scholars?

Signs. A cross, +, one line horizontal and the other perpendicular, is the sign of addition. It shows that humbers, with this sign between them, are to be added together. It is sometimes read plus, which is a Latin word, signifying more.

Two parallel, horizontal lines, =, are the sign of equality. It signifies that the number before it is equal to the number after it. Thus, 5+3=8 is read 5 and 3 are 8; or, 5 plus (that is, more) 3 is equal to 8.

In this manner let the pupil be instructed to commit the

following

ADDITION TABLE.

2+0=2 3+0=3	4+0=4	5-0-5
2+1=3 3+1=4	4 + 1 = 5	5-1-6
2+2=43+2=5	4-2-6	5-2-7
2+3=53+3=6	4 1 3 = 7	513-8
2+4=63+4=7	4 4 8	514- 9
2+5=73+5=8	415-0	5 1 5 - 10
2+6=83+6=9	416-10	5 1 6 - 11
2+7=93+7=10	A 17 - 11	5 7 7 19
2+8=10 $3+8=11$	4 T 8 _ 10	5+8=13
2+9=11 3+9=12	4 0 - 12	5 0 14
~ · - 11 0 - 3 - 1%	11 11 11 11 11 11	0 十 7 = 14

$$5+9 = how many?$$
 $8+7 = how many?$
 $4+3+2 = how many?$
 $6+4+5 = how many?$
 $2+0+4+6 = how many?$
 $3+0+9+5 = how many?$
 $3+0+9+5 = how many?$
 $1+3+5+7+8 = how many?$
 $1+3+5+7+8 = how many?$
 $1+2+3+4+5+6 = how many?$

To. When the numbers to be added are small, the addition is readily performed in the mind; but it will frequently be more convenient, and even necessary, to write the numbers down before adding them.

13. Harry had 43 books in his little library, his father gave him 25 volumes more; how many volumes had he then?

One of these numbers contains 4 tens and 3 units. The other number contains 2 tens and 5 units. To unite these two numbers together into one, write them down one under the other, placing the units of one number directly under units of the other, and the tens of one number directly under tens of the other, thus:

43 volumes, Having written the numbers in this 25 volumes. manner, draw a line underneath.

Ans.

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+0=	9
+1 =	10
+2 =	11
+ 3 =	12
- 4 =	13
5 =	14
-6 =	15
-7=	16
-8=	17
0	10

43 volumes,
25 volumes,
add the 5 units of the lower number to the 3 units of the upper number, making 8 units, which we set down in unit's place.

We then proceed to the next column,
and add the 2 tens of the lower number
to the 4 tens of the upper number, making 6 tens, or 60, which we set down in
ten's place, and the work is done.

It now appears that Harry's whole number of volumes is 6 tens and 8 units, or 68 volumes; that is, 43+25=68.

14. A gentleman bought a carriage for 214 pounds, a horse for 30 pounds, and a saddle for 4 pounds; what was the whole amount?

Write the numbers as before directed, with units under units, tens under tens, &c.

OPERATION.

Carriage, 214 pounds, Add as before. The units will Horse, 30 pounds, be 8, the tens 4, and the hundreds Saddle, 4 pounds. 2, that is, 214+30+4=248.

Answer, 248 pounds.

After the same manner are performed the following examples:

15. A man had 15 sheep in one pasture, 20 in another pasture, and 143 in another; how many sheep had he in the three pastures? 15+20+143 = 15 how many?

16. A man has three farms, one containing 500 acres, another 213 acres, and another 76 acres; how many acres in the three farms? 500 + 213 + 76 = how many?

17. Bought a farm for 625 pounds, and afterward sold it so as to gain 150 pounds; what did I sell the farm for? 625 + 150 = how many?

Hitherto the amount of any one column, when added up, has not exceeded 9; consequently has been expressed by a single figure. But it will frequently happen that the amount of a single column will exceed 9, requiring two or more figures to express it.

18. There are three bags of money. The first contains B 2

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976 pounds, the second 653 pounds, the third 524 pounds; what is the amount contained in all the bags 1

OPERATION. First bag, 876 Second bag, 653 Third bag, 524

Amount. 2053

Writing down the numbers as already directed, we begin with the right hand, or unit column, and find the amount to be 13, that is, 3 units and 1 ten. Setting down the 3 units, or right hand figure, in unit's place, directly under the column, we reserve

the 1 ten, or left hand figure, to be added with the other tens, in the next column, saying, 1, which we reserved, to 2 makes 3, and 5 are 8, and 7 are 15, which is 5 units of its own order, and 1 unit of the next higher order, that is, 5 tens and 1 hundred. Setting down the 5 tens, or right hand figure, directly under the column of tens, we reserve the left hand figure, or 1 hundred, to be added in the column of hundreds, saying 1 to 5 is 6, and 6 are 12, and 8 are 20, which being the last column, we set down the whole number, writing the 0, or right hand figure, directly under the column, and carrying forward the 2, or left hand figure, to the next place, or place of thousands. Wherefore, we find the whole amount of money contained in the three bags to be 2053 pounds—the answer.

PROOF. We may reverse the order, and, beginning at the top, add the figures downward. If the two results are alike, the work is supposed to be right.

From the examples and illustrations now given, we derive the following

RULE.

I. Write the numbers to be added, one under another, placing units under units, tens under tens, &c. and draw a line underneath.

II. Begin at the right hand or unit column, and add together all the figures contained in that column: if the amount does not exceed 9, write it under the column; but if the amount exceed 9, so that it shall require two or more figures to express it, write down the unit figure only under the column; the figure or figures to the left hand of units, being tens, are so many units of the next higher order, which, being reserved, must be carried forward, and added to the first figure in the next column.

III. Add each succeeding column in the same manner, and set down the whole amount at the last column.

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EXAMPLES FOR PRACTICE.

19. A man bought four loads of hay; one load weighed 1817 pounds, another weighed 1950 pounds, another 2156 pounds, and another 2210 pounds; what was the amount of hay purchased?

20. A person owes A 100 pounds, B 522 pounds, C 785 pounds, D 92 pounds; what is the amount of his debts ?

21. A farmer raised in one year 1200 bushels of wheat, \$50 bushels of Indian corn, 1000 bushels of oats, 1086 bushels of barley, and 74 bushels of peas; what was the whole amount?

Ans. 4210.

22. St. Paul's Cathedral, in London, cost 800,000 pounds sterling; the Royal Exchange 80,000 pounds; the Mansion-House 40,000 pounds; Black Friars Bridge 152,840 pounds; Westminster Bridge 389,000 pounds, and the Monument 13,000 pounds; what is the amount of these sums?

Ans. 1,474,840 pounds.

23. If at the census in 1831, the population of the following counties was as follows:—Lower Canada: Gaspe, 4,171; Dorchester, 11,946; Nicolet, 12,504; Sherbrooke, 6,814; Stanstead, 8,272: Upper Canada: Gore, 23,552; Home, 32,871; Niagara, 21,974; London, 26,180; Ottowa, 4,456; what was the whole number of inhabitants in these counties at that time!

Ans. 152,740.

24. From the creation to the departure of the Israelites from Egypt was 2513 years; to the siege of Troy, 307 years more; to the building of Solomon's Temple, 180 years; to the building of Rome, 251 years; to the expulsion of the kings from Rome, 244 years; to the destruction of Carthage, 363 years; to the death of Julius Cesar, 102 years; to the christian era, 44 years; required the time from the creation to the christian era.

Ans. 4004 years.

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			6	2	5	3						2	6	0	8	1	2	7	5	3	0	6	2	1	7
					4		2	4	7	1	3	5	5	6	5	2	1	7	4	6	3	0	1	2	8
									8	6	7	3	8	7	0	3	2	6	3	4	7	2	0	1	3

						2	7.											2	8.						1
5	3	6	4	2	0	7	6	3	1	0	2	3	9	0	2	3	7	5	4	6	8	2	1	3	
2	8	1	2	3	4	5	6	7	2	9	4	8	2	8	3	4	9	6	7	3	2	6	7	0	
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29. What is the amount of 46723, 6742, and 986 pounds? 30. A man has three orchards; in the first there are 140 trees that bear apples, and 64 trees that bear peaches; in the second, 234 trees bear apples, and 73 bear cherries; in the third, 47 trees bear plums, 36 bear pears, and 25 bear cherries; how many trees in all the orchards?

SUPPLEMENT

TO NUMERATION AND ADDITION.

QUESTIONS,

EXERCISES.

- 1. Washington was born in the year of our Lord 1732; he was 67 years old when he died; in what year of our Lord did he die?
- 2. The invasion of Greece by Xerxes took place 481 years before Christ; how long ago is that this current year 1833?
- 3. There are two numbers, the less number is 8671, the difference between the numbers is 597; what is the greater number.
- 4. A man borrowed a sum of money, and paid in part 684 pounds; the sum left unpaid was 876 pounds, what was the sum borrowed?

28.

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1 986 pounds! there are 140 r peaches; in r cherries; in and 25 bear

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What is notaise? 4. How numeration? in addition? it, or number 11. —

Lord 1732 : ear of our

481 years ear 1833? 8671, the he greater

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5. There are four numbers, the first 317, the second 812, the third 1350, and the fourth as much as the other three; what is the sum of them all 1

6. A gentleman left his daughter 16 thousand, 16 hundred and 16 pounds; he left his son 1800 more than his daughter; what was his son's portion, and what was the Ans. Son's portion, 19,416. Whole estate, 37,032. amount of the whole estate?

7. A man, at his death, left his estate to his four children. who, after paying debts to the amount of 1476 pounds, received 4768 pounds each; how much was the whole estate 1

8. A man bought four hogs, each weighing 375 pounds; how much did they all weigh ?

9. The fore quarters of an ox weigh one hundred and eight pounds each, the hind quarters weigh one hundred and twenty-four pounds each, the hide seventy-six pounds, and the tallow sixty pounds; what is the whole weight of the ox ? 1 word 1 1 2 / Ans. 600.

10. A man, being asked his age, said he was thirty-four years old when his eldest son was born, who was then fifteen years of age; what was the age of the father?

11. A man sold two cows for five pounds each, twenty bushels of corn for three pounds, and one hundred pounds of tallow for two pounds; what was his due!

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OF SIMPLE NUMBERS.

16. 1. Charles, having 11 pence, bought a book, for which he gave 5 pence; how many pence had he left?

2. John had 12 apples; he gave 5 of them to his broth-

er; how many had he left?

3. Peter played at marbles; he had 23 when he began, but when he had done he had only 12; how many did he lose ?

4. A man bought an article for 17 shillings and sold it again for 22 shillings; how many shillings did he gain 1

5. Charles is 9 years old, and Andrew is 13; what is the

difference in their ages ?

6. A man borrowed 50 pounds, and paid all but 18; how many pounds did he pay? that is, take 18 from 50, and how many would there be left?

7. John bought several articles for 19 shillings; he gave for 4 books 6 shillings; what did the other articles cost

him 1

8. Peter bought a trunk for 17 shillings, and sold it for 22 shillings; how many shillings did he gain by the bargain?

9. Peter sold a waggon for 22 shillings, which was 5 shillings more than he gave for it; how many shillings did

he give for the waggon !

10. A boy, being asked how old he was, said that he was 25 years younger than his father, whose age was 33 years; how old was the boy 1

The taking of a less number from a greater (as in the foregoing examples) is called Subtraction. The greater number is called the minuend, the less number the subtracted, and what is left after subtraction is called the difference, or remainder.

11. If the minuend be 8, and the subtrahend 3, what is the difference or remainder?

Ans. 5.

12. If the subtrahend be 4, and the minuend 16, what is the remainder?

13. Samuel bought a book for 11 pence; he paid down 4 pence; how many pence more must he pay?

Sign. A short horizontal line, —, is the sign of subtraction. It is usually read minus, which is a faction word signifying less. It shows that the number after it is to be taken from the number before it. Thus, 8—3=5, is read 8 minus or less 3 is equal to 5; or 3 from 8 leaves 5. The latter expression is to be used by the pupil in committing the following

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SUBTRACTION TABLE.

2-2-0 3-2-1 4-2-2 5-3-3 6-3-4 7-3-5 8-3-7 10-3-8 3-3-9 4-3-1	6-3-3 7-3-4 8-3-5 9-3-6 10-3-7 4-4-0 5-4-1 6-4-2 7-4-3 8-4-4 9-4-5	5-5=0 6-5=1 7-5=2 8-5=3 9-5=4 10-5=5 6-6=0 7-6=1 8-6=2 9-6=3 10-6=4	7-7=0 8-7=1 9-7=2 10-7=3 8-8=0 9-8=1 10-8=2 9-9=0 10-9=1
43=1 53=2	9-4=5 10-4=6	10-6-4	

7-3 = now many:	10 - / = now many :
8-5 = how many 1	28-7 = how many ?
9-4 = how many 1	22 - 13 = how many ?
12-3 = how many?	33-5 = how many?
13-4 = how many?	41 - 15 = how many ?

¶ 7. When the numbers are small, as in the foregoing kamples, the taking of a less number from a greater is readified one in the mind; but when the numbers are large, the peration is most easily performed part at a time, and therefore it is necessary to write the numbers down before perming the operation.

14. A farmer having a flock of 237 sheep, lost 114 of seem by disease; how many had he left?

Here we have 4 units to be taken from 7 units, 1 ten to be taken from 3 tens, and 1 hundred to be taken from 2 undreds. It will therefore be most convenient to write be less number under the greater, observing, as in addition, be place units under units, tens under tens, &c. thus:

OPERATION.
From 237 the minuend,
Take 114 the subtrahend,

123 the remainder.

We now begin with the units, saying, 4 (units) from 7, (units,) and there remain 3, (units,) which we set down directly under the column in unit's place.

Then, proceeding to the next column we say 1 (ten) from 3, (tens,) and there remain 2 (tens,) which we set down in ten's place. Proceeding to the next column, we say, 1 (hundred) from 2, (hundreds,) and there remains 1, (hundred,) which we set down in hundred's place, and the work is done. It now appears, that the number of sheep left was 123: that is, 237—114—123.

After the same manner are performed the following examples:

15. There are two farms; one is valued at 973 pounds, and the other at 421 pounds; what is the difference in the value of the two farms?

16. A man's property is worth 2170 pounds, but he has debts to the amount of 1110 pounds; what will remain after paying his debts.

17. James, having 15 shillings bought a book for which he gave 7 shillings; how many shillings had he left?

OPERATION.

15 shillings.
7 shillings.
— A difficulty presents itself here; for we cannot take 7 from 5; but we can take 7 from 15, and there will remain 8.

8 shillings left.

18. A man bought several articles for 85 pounds, and other articles for 27 pounds; what did the former cost him more than the latter?

OPERATION. The same difficulty meets us here as in First articles, 85 the last example; we cannot take 7 from Other articles, 27 5; but in the last example the larger num-

— ber consisted of 1 ten and 5 units, which Difference, 58 together make 15; we therefore took 7 from 15. Here we have 8 tens and 5 units. We can now, in the mind, suppose 1 ten taken from the 8 tens, which would leave 7 tens, and this 1 ten we can suppose joined to the 5 units, making 15. We can now take 7 from 15, as before, and there will remain 8, which we set down. The taking of 1 ten out of 8 tens, and joining it with the 5 units, is called borrowing ten. Proceeding to the next higher order, or tens, we must consider the upper figure 8, from which we borrowed, 1 less, calling it seven; then, taking 2 (tens) from 7 (tens) there will remain five (tens,) which we set down, making the difference 58. Or, instead of mak-

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take 7 from larger numunits, which efore took 7 We can now, tens, which ose joined to from 15, as lown. The the 5 units, thigher orure 8, from then, taking tens,) which tead of making the upper figure 1 less, calling it 7, we may make the lower figure 1 more, calling it 3, and the result will be the same; for 3 from 8 leaves 5, the same as 2 from 7.

19. A man borrowed 713 pounds, and paid 471 pounds; how many pounds did he then owe! 713 - 471 = how many!

Ans. 242 pounds.

20. 1612 - 465 = how many?

Ans. 1147.

21. 43751 - 6782 = how many?

Ans. 36969.

¶ 8. The pupil will readily perceive, that subtraction is the reverse of addition.

22. A man bought 40 sheep, and sold 18 of them; how many had he left? 40 — 18 = how many?. Ans. 22 sheep.

23. A man sold 18 sheep, and had 22 left; how many

had he at first? 18×22 —how many?

24. A man bought some articles for 75 pounds, and others for 16 pounds; what was the difference of the costs?

75 — 16 = how many? Reversed, 59 + 16 = how many?

25. 114—103—how many? Reversed, 11+103—how

many ?

26. 143-76 how many? Reversed, 67+76 how many?

Hence, subtraction may be proved by addition, as in the

foregoing examples, and addition by subtraction.

To prove subtraction, we may add the remainder to the subtrahend, and, if the work is right, the amount will be

equal to the minuend.

To prove addition, we may subtract, successively, from the amount, the several numbers which were added to produce it, and, if the work is right, there will be no remainder. Thus 7+8+6=21; proof, 21-6=15, and 15-8=7, and 7-7=0.

From the remarks and illustrations now given, we deduce the following

RULE.

I. Write down the numbers, the less under the greater, placing units under units, tens under tens, &c. and draw a line under them.

II. Beginning with units, take successively each figure in the lower number from the figure over it, and write the remainder directly below.

III. When the figure in the lower number exceeds the figure over it, suppose 10 to be added to the upper figure,

but in this case we must add 1 to the lower figure in the next solumn before subtracting. This is called borrowing 19.

EXAMPLES FOR PRACTICE.

27. If a farm and the buildings on it be valued at 3000 pounds, and the buildings alone be valued at 1500 pounds, what is the value of the land?

28. The population of the two Canadas, at the last census, was 789,000, at the census before, the population was 648.000: what was the difference in the two enumerations?

29. What is the difference between 7,648,203 and

928,671 1

30. How much must you add to 358,642 to make 1,487,945?

31. A man bought an estate for 3798 pounds, and sold it again for 4137 pounds; did he gain or lose by it! and how much?

32. From 364,710,825,193 take 27,940,386,574.

33. From 831,025,405,270 take 651'308,604,782.

34. From 127,368,047,216,843 take 978,654,827,358.

SUPPLEMENT

TO SUBTRACTION.

QUESTIONS.

1. What is subtraction? 2. What is the greater number salled?
3. — the less number? 4. What is the result or answer called?
5. What is the sign of subtraction? 6. What is the rule? 7. What is understood by borrowing ten? 8. Of what is subtraction the reverse? 9. How is subtraction proved? 10 How is addition proved by subtraction?

EXERCISES.

1. How long from the discovery of America by Columbus, in 1492, to the period of the cession by France of all her possessions in North America to Great Britain, in 1763.

2. Supposing a man to have been born in the year 1773,

bow old was he in 1827?

3. Supposing a man to have been 80 years old in the year 1826, in what year was he born 1

4. There are two numbers, whose difference is 8764; the greater number is 15687; I demand the less?

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8764; the

5. What number is that which, taken from 3794, leaves 865?

6. What number is that to which if you add 789, it will

become 6350 !

7. In a certain city, there were 123,706 inhabitants; in another 43,940; how many more inhabitants were there in one than in the other?

8. A man possessing an estate of twelve thousand pounds, gave two thousand five hundred pounds to each of his two daughters, and the remainder to his son; what was his son's share?

9. From seventeen million take fifty-six thousand, and

what will remain?

10. What number, together with these three, vis. 1301,

2561, and 3120, will make ten thousand ?

11. A man bought a house for 35 pounds, and a chaise for 47 pounds; how much more did he give for the chaise than for the house?

12. A man borrows 7 ten dollar bills and three one dollar bills, and pays at one time 4 ten dollar bills and 5 one dollar bills; how many ten dollar bills and one dollar bills must be afterwards pay to cancel the debt?

Ans, 2 ten doll. bills and 8 one doll.

13. The greater of two numbers is 24, and the less is 16; what is their difference?

14. The greater of two numbers is 24, and their difference 8; what is the less number ?

15. The sum of two numbers is 40, the less is 16; what is the greater?

16. A tree, 68 feet high, was broken off by the wind; the top part, which fell, was 49 feet long; how high was the stump which was left?

17. Elizabeth became Queen of England in 1558; how

many years since !

18. A man carried his produce to market; he sold his pork for 14 pounds, his cheese for 11 pounds, and his butter for 9 pounds; he received, in pay, salt to the value of 6 pounds, 3 pounds worth of sugar, 2 pounds worth of molasses, and the rest in money; how much money did he receive?

Ans. 23 pounds.

19. A boy bought several sleds for 13 shillings, and gave 6 shillings to have them repaired; he sold them for 18 shill-

ings; did he gain or lose by the bargain? and how much?

20. One man travels 67 miles in a day, another man follows at the rate of 42 miles a day; if they both start from the same place at the same time, how far will they be apart at the close of the first day! — of the second! — of the third? — of the fourth!

21. One man starts from York Monday morning, and travels at the rate of 40 miles a day; another starts from the same place Tuesday morning, and follows at the rate of 70 miles a day; how far are they apart Tuesday night?

Ans. 10 miles.

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22. A man owing 379 pounds, paid at one time 47 pounds, at another time 84 pounds, at another time, 27 pounds, and at another 143 pounds; how much did he then owe?

Ans. 82 pounds.

23. A man has property to the amount of 34764 pounds, but there are demands against him to the amount of 14297 pounds; how many pounds will be left after the payment of his debts?

24. Four men bought a lot of land for 482 pounds; the first man paid 274 pounds, the second man 194 pounds less than the first, and the third man 20 pounds less than the second; how much did the second, third, and the fourth man pay?

(The second paid 80.

The third paid 60.
The fourth paid 68.

25. A man, having 10,000 pounds, gave away 9 pounds; how many had he left!

Ans. 9991.

MYLTIPLICATION

OF SIMPLE NUMBERS.

2. One bushel of apples cost 3 shillings; how many shillings must I give for 2 bushels? —— for 3 bushels?

3. One gallon contains 4 quarts; how many quarts in 2 gallons? — in 3 gallons? — in 4 gallons?

4. Three men bought a horse; each man paid 6 pounds

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6 pounds

for his share; how many pounds did the horse cost them !

5. A man has 4 farms worth 95 pounds each; how many pounds are they all worth !

6. In one pound there are 20 shillings; how many shil-

lings in 5 pounds?

7. How much will 4 pair of shoes cost at 9 shillings a pair?

8. How much will 3 pounds of tea cost at 5 shillings a

pound !

9. There are 24 hours in 1 day; how many hours in 2 days ! - in 3 days ! - in 4 days ! - in 7 days !

10. Six boys met a beggar and gave him 9 pence each;

how many pence did the beggar receive?

When questions occur, (as in the above examples,) where the same number is to be added to itself several times, the operation may be much facilitated by a rule, called Multiplication, in which the number to be repeated is called the multiplicand, and the number which shows how many times the multiplicand is to be repeated is called the multiplier. The multiplicand and multiplier, when spoken of collectively, are called the factors, (producers,) and the answer is called the product.

11. There is an orchard in which there are 5 rows of trees. and 27 trees in each row; how many trees in the orchard?

In the first row, 27 trees. " second " 27 " third " 27 " " fourth " 27 " " fifth " 27 "

In this example, it is evident that the whole number of trees will be equal to the amount of five 27's added together.

In adding, we find that 7 taken five times amounts to 35. We write

In the orchard 135 trees. down the five units, and reserve the 3 tens; the amount of 2 taken five times is 10, and the 3, which we reserved. makes 13, which, written to the left of units, makes the whole number of trees 135.

If we have learned that 7 taken 5 times amounts to 35, and that 2 taken 5 times amounts to 10, it is plain we need write the number 27 but once, and then, setting the multitiplier under it, we may say, 5 times 7 are 35, writing down

Product.

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 $\times 11$ \times 12

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the 5, and reserving the 3 (tens) as in addition. Again 5

Multiplicand. 27 trees in each row. Multiplier, 5 rows.

135 trees, Ans.

times 2 (tens) are 10 (tens,) and 3, (tens,) which we reserved, make 13, (tens.) as before.

12. There are on a board 3 rows of spots, and 4 spots in each row; how many spots on the board?

A slight inspection of the figure will SE SE SE SE show that the number of spots may be SH SH SH SH found either by taking 4 three times, (3 times 4 are 12.) or by taking 3 four times. # # # # (4 times 3 are 12;) for we may say there are three rows of 4 spots each, or 4 rows of 3 spots each; therefore, we may use either of the given numbers for a multiplier, as best suits our convenience. We generally write the numbers as in subtraction, the larger number uppermost, with units under units, tens under tens, &c. Thus,

Multiplicand, 4 spots. Note. 4 and 3 are the factors, which produce the product 12. Multiplier. 3 rows.

Product, . 12 Ans.

Hence,--Multiplication is a short way of performing many additions; in other words,—It is the method of repeating any number any given number of times.

Two short lines crossing each other in the form of the letter X, are the sign of multiplication. Thus, 3×4 = 12, signifies that 3 times 4 are equal to 12, or 4 times 3 are 12.

Before any progress can be made in this rule, the Note. following table must be committed perfectly to memory.

Again 5 (tens) are s,) and 3, which we, make 13, s before.

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MULTIPLICATION TABLE.

2 times 0 are $0.4 \times 10 = 40.7 \times .7 = 49.10 \times .4 = .42 \times .1 = .24 \times .11 = .44.7 \times .8 = .56.10 \times .5 = .52 \times .2 = .44 \times .12 = .48.7 \times .9 = .63.10 \times .6 = .62 \times .3 = .65 \times .0 = .07 \times .10 = .70.10 \times .7 = .52 \times .4 = .85 \times .1 = .57 \times .11 = .77.10 \times .8 = .85 \times .1 = .57 \times .11 = .77.10 \times .8 = .85 \times .12 \times .12 \times .12 \times .13 \times .13 \times .13 \times .13 \times .13 \times .14 \times .14$	40
$2 \times 1 = 24 \times 11 = 447 \times 8 = 5610 \times 5 = 3$	50
$2 \times 2 = 44 \times 12 = 487 \times 9 = 6310 \times 6 = 6$	60
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$3 \times 2 = 65 \times 12 = 608 \times 9 = 7211 \times 6 = 6$	
	7
	8
$1 \times 5 = 156 \times 2 = 128 \times 12 = 9611 \times 9 = 96$	9
$8 \times 6 = 186 \times 3 = 189 \times 0 = 0^{11} \times 10 = 11$	0
$1 \times 7 = 216 \times 4 = 249 \times 1 = 911 \times 11 = 12$	
\times 8=246 \times 5=309 \times 2= 18 ¹¹ \times 12=13	2
	<u>0</u> .
$3 \times 10 = 306 \times 7 = 429 \times 4 = 3612 \times 1 = 19$	
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$\begin{array}{c} \times & 5 = 207 \times & 2 = 149 \times 12 = 10812 \times & 9 = 108 \times \\ \times & 6 = 247 \times & 3 = 21 \times 10 \times 0 = & 012 \times 10 = 120 \times 10 $	
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$4 \times 8 = 327 \times 5 = 3510 \times 2 = 20^{12} \times 12 = 144$	
$4 \times 9 = 367 \times 6 = 4210 \times 3 = 30$	

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 $9 \times 2 = \text{how many }$ $4 \times 3 \times 2 = 24$. $4 \times 6 = \text{how many }$ $3 \times 2 \times 5 = \text{how many }$ $3 \times 2 \times 5 = \text{how many }$ $3 \times 7 = \text{how many }$ $3 \times 7 = \text{how many }$ $3 \times 2 \times 4 \times 5 = \text{how many }$ $3 \times 2 \times 4 \times 5 = \text{how many }$

13. What will 84 barrels of flour cost at 2 pounds a barrel?

Ans. 168 pounds.

14. A merchant bought 12 dozen hats at the rate of 12 pounds per dozen; what did they cost? Ans. 144 pounds.

15. How many inches are there in 253 feet, every foot

being 12 inches !

OPERATION.

253
cant figures or digits, having been committed to memory from the multiplication table, it is just as easy to multiply by 12 as by a single figure. Thus, 12 times 3 are 36, &c.

16. What will 476 barrels of fish cost at 3 pounds a barrel!

Ans. 1428 pounds.

17. A piece of very valuable land, containing 33 acres, was sold for 246 pounds an acre; what did the whole come to?

As 12 is the largest number, the product of which, with the nine digits, is found in the multiplication table, therefore, when the multiplier exceeds 12, we multiply by each figure in the multiplier separately. Thus:

OPERATION.

246 pounds, the price of one acre.
33 number of acres.

738 pounds, the price of three acres. 738 pounds, the price of thirty acres,

Ans. 8118 pounds, the price of 33 acres.

The multiplier consists of 3 tens and 3 units. First, multiplying by the 3 units gives us 738 pounds the

price of 3 acres. We then multiply by the 3 tens, writing the first figure of the product (8) in ten's place, that is, directly under the figure by which we multiply. It now appears that the product by the 3 tens consists of the same figures as the product by the 3 units; but there is this difference—the figures in the product by the 3 tens are all removed one place further to the left hand, by which their value is increased tenfold, which is as it should be, because the price

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of 30 acres is evidently ten times as much as the price of 3 acres, that is, 7380 pounds; and it is plain, that these two products, added together, give the price of 33 acres.

These examples will be sufficient to establish the fol-

lowing

RULE.

I. Write down the multiplicand, under which write the multiplier, placing units under units, tens under tens, &c., and draw a line underneath.

II. When the multiplier does not exceed 12, begin at the right hand of the multiplicand, and multiply each figure contained in it by the multiplier, setting down, and carry-

ing the same as in addition.

III. When the multiplier exceeds 12, multiply by each figure separately, first by the units, then by the tens, &c., remembering always to place the first figure of each product directly under the figure by which you multiply. Having gone through in this manner with each figure in the multiplier, add their several products together, and the sum of them will be the product required.

EXAMPLES FOR PRACTICE.

18. There are 320 rods in a mile; how many rods are there in 57 miles?

19. Suppose it to be 706 miles from Halifax to Quebec;

how many rods is it?

20. What will 784 chests of tea cost, at 17 pounds a chest?

21. If 1851 men receive 758 pounds apiece; how many pounds will they all receive?

Ans. 1403058 pounds.

22. There are 24 hours in a day; if a ship sail 7 miles in an hour, how many miles will she sail in 1 day, at that rate? how many miles in 36 days? how many miles in 1 year, or 365 days?

Ans. 61320 miles in 1 year.

23. A merchant bought 13 pieces of cloth, each piece containing 28 yards, at 2 pounds a yard; how many yards,

were there, and what was the whole cost?

Ans. The whole cost was 728 pounds.

24. Multiply 37864 by 235. *Product*, 8898040. 25. " 29831 " 952. " 28399112.

26. " 93956 " 8704. " 817793024.

CONTRACTIONS IN MULTIPLICATION.

1. When the multiplier is a composite number.

11. Any number, which may be produced by the multiplication of two or more numbers, is called a composite number. Thus, 15, which arises from the multiplication of 5 and 3, (5×3=15.) is a composite number, and the numbers 5 and 3, which, multiplied together, produce it, are called component parts or factors of that number. So, also, 24 is a composite number; its component parts, or factors, may be 2 and 12, (2×12=24;) or they may be 4 and 6, (4×6=24;) or they may be 2, 3, and 4. (2×3×4=24.)

60

Wherefore, If the multiplier be a composite number, we may, if we please, multiply the multiplicand first by one of the component parts; that product by the other, and so on, if the component parts be more than two; and, having in this way amultiplied by each of the component parts, the last product will be the product required.

2. What will 186 tems of potsshes some to, at 24 pounds

per ton 1

6×4=24. It follows, therefore, that 6 and 4 are com-

136 tons.

6 one of the component parts, or factors.

816 pounds, the price of 6 tons.

4 the other component part, or factor.

Ans. 3264 pounds, the price of 136 tons.

3. Supposing 342 men to be employed in a certain piece of work, for which they are to receive 28 pounds, each, how much will they all receive?

7×4-28

Ans. 9576 pounds.

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6 pounds.

 4. Multiply 367 by 48.
 Product, 17616.

 5. " 853 " 56.
 " 47768.

 6. " 1086 " 72.
 " 78192.

II. When the multiplier is 10, 100, 1000, &c.

¶ 12. It will be recollected, (¶ 3.) that any figure, on being removed one place towards the left hand, has its value increased tenfold; hence, to multiply any number by 10, it is only necessary to write a cypher on the right hand of it. Thus, 10 times 25 are 250; for the 5, which was units before, is now made tens, and the 2, which was tens, before, is now made hundreds. So, also, if any figure be removed two places towards the left hand, its value is increased 100 times, &c. Hence.

When the multiplier is 10, 100, 1000, or I with any number of ciphers annexed, annex as many ciphers to the multiplicand as there are ciphers in the multiplier, and the multiplicand, so increased, will be the product required. Thus,

Multiply 46 by 10, the product is 460.
" 83 " 100, " " 8300.
" 95 " 1000, " " 95000.

EXAMPLES FOR PRACTICE.

1. What will 76 loads of corn cost, at 10 pounds a load?

2. If 100 men receive 32 pounds each, how many pounds will they all receive?

3. What will 1000 pieces of broadcloth cost, estimating each piece at 78 pounds?

4. Multiply 5682 by 10000. 5, 82134 , 100000.

¶ 13. On the principle suggested in the last ¶, it follows,

When there are ciphere on the right hand of the multiplicand, multiplier, either or both, we may, at first, neglect these ciphers, multiplying by the significant figures only; after which we must annex as many ciphers to the product as there are ciphers on the right hand of the multiplicand and multiplier, counted together.

EXAMPLES FOR PRACTICE.

1. If 1300 men receive 460 pounds apiece, how many pounds will they all receive?

OPERATION. 460 1300	The ciphers in the multiplicand and multiplier, counted together, are three. Disregarding these, we
138 46	write the significant figures of the multiplier under the significant fig- ures of the multiplicand, and mul-
Ins, 598000 pounds.	tiply; after which we annex three ciphers to the right hand of the

product, which gives the true answer.

2. The number of distinct buildings in New England, appropriated to the spinning, weaving, and printing of cotton goods, was estimated, in 1826, at 400, running, on an average, 700 spindles each; what was the whole number of spindles?

3. Multiply 257 by 6300.

4. " 8600 " 17.

5. " 9340 " 460.

6. " 5200 " 410.

7. " 378 " 204.

OPERATION.

378

204

In the operation it will be seen, that multiplying by ciphers produces nothing. Therefore,

756

77112

III. When there are ciphers between the significant figures of the multiplier, we may omit the ciphers, multiplying by the significant figures only, placing the first figure of each product directly under the figure by which we multiply.

EXAMPLES FOR PRACTICE.

8. Multiply 154326 by 3007.

9. 10. 11.

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Product, 464058282

9. Multiply 543 by 206. 10. " 1620 " 2103. 11. " 36243 " 32004.

SUPPLEMENT

TO MULTIPLICATION.

QUESTIONS.

EXERCISES.

1. An army of 10700 men having plundered a city, took so much money, that, when it was shared among them, each man received 46 pounds; what was the sum of money taken?

2. Supposing the number of houses in a certain town to be 145, each house, on an average, containing two families. and each family 6 members, what would be the number of inhabitants in that town?

Ans. 1740.

3. If 46 men can do a piece of work in 60 days, how many men will it take to do it in one day?

4. Two men depart from the same place, and travel in opposite directions, one at the rate of 27 miles a day, the other 31 miles a day; how far apart will they be at the end of 6 days?

Ans. 348 miles.

5. What number is that, the factors of which are 4, 7, 6, and 20?

Ans. 3360.

6. If 18 men can do a piece of work in 90 days, how long will it take one man to do the same?

7. What sum of money must be divided between 27 men, so that each man may receive 115 pounds?

8. There is a certain number, the factors of which are 89 and 265; what is that number?

9. What is that number, of which 9, 12, and 14 are factors?

10. If a carriage wheel turn round 346 times in running 1 mile, how many times will it turn round in the distance from Quebec to Montreal it being 180 miles.

Ans. 62280.

11. In one minute are 60 seconds; how many seconds, in 4 minutes? —— in 5 minutes? —— in 20 minutes?——in 40 minutes?

12. In one hour are 60 minutes; how many seconds an hour? — in two hours? How many seconds from nine o'clock in the morning till noon?

13. In one pound are 4 dollars; how many dollars in 3 pounds? —— in 300 pounds? —— in 467 pounds?

14. Two men, A and B, start from the same place at the same time, and travel the same way; A travels 52 miles a day, and B 44 miles a day; how far apart will they be at the end of 10 days?

15. If the interest of 100 pounds, for one year, be six pounds, how many pounds will be the interest for 2 years?

for 4 years? — for 10 years? for 35 years? — for 84 years?

16. If the interest of one hundred pounds, for one year, be six pounds, what is the interest for two hundred pounds the same time? — 7 hundred pounds? — 8 hundred pounds?

17. A farmer sold 468 pounds of pork, at 3 pence a pound, and 48 pounds of cheese, at 4 pence a pound; how many pence must be receive in pay?

18. A boy bought 10 oranges; he kept 7 of them, and sold

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the others for 5 pence a piece; how many pence did he receive?

19. The component parts of a certain number are 4, 5, 7,

6, 9, 8, and 3; what is the number 1

20. In 1 hogshead are 63 gallons; how many gallons in 8 hogsheads? In 1 gallon are 4 quarts; how many quarts in 8 hogsheads? In 1 quart are 2 pints; how many pints in 8 hogsheads?

MODULATIO

OF SIMPLE NUMBERS.

¶ 14. 1. James divided 12 apples among four boys; how many did he give each boy?

2. James would divide 12 apples among three boys;

how many must he give each boy?

3. John had 15 apples, and gave them to his playmates, who received 3 apples each; how many boys did he give hem to?

4. If you had 20 pence, how many cakes could you buy

t 2 pence a piece?

5. How many yards of cloth could you buy for 30 pounds, it 2 pounds a yard?

6. If you pay 250 shillings for 10 yards of cloth, what one yard worth?

7. A man works 6 days for 42 shillings; how many nillings is that for one day?

8. How many quarts in 4 pints? — in 6 pints? — in 10 pints?

9. How many times is 8 contained in 88?

10. If a man can travel 4 miles an hour, how many hours yould it take him to travel 24 miles?

11. In an orchard there are 28 trees standing in rows, and there are 3 trees in a row; how many rows are there?

Remark. When any one thing is divided into two equal parts, one of those parts is called a half; if into 3 equal parts, one of those parts is called a third; if into four equal parts, one part is called a quarter or a fourth; if into five, one part is called a fifth, and so on.

12. A boy had two apples, and gave one half an apple to each of his companions; how many were his companions?

13. A boy divided four apples among his companions, by giving them one third of an apple each; among how many did he divide his apples?

14. How many quarters in 3 oranges?

15 How many oranges would it take to give 12 boys one quarter of an orange each?

16. How much is one half of 12 apples?

17. How much is one third of 12?

18. How much is one fourth of 12?

19. A man had 30 sheep, and sold one fifth of them; how many of them did he sell?

20. A man purchased sheep for 13 shillings apiece, and paid for them all 117 shillings; what was their number?

21. How many oranges, at 3 pence each, may be bought

for 12 pence?

It is plain, that as many times as 3 pence can be taken from 12 pence, so many oranges may be bought; the object, therefore, is to find how many times 3 is contained in 12.

First orange, 3 pence.

Second orange, 3 pence.

6

Third orange, 3 pence.

Fourth orange, 3 pence.

We see in this example, that we may take 3 from 12 four times, after which there is no remainder; consequently, subtraction alone is sufficient for the operation; but we may come to the same result by a process, in most cases much shorter, called Division.

(

multiplied by the number of oranges, (4,) is equal to the cost of all the oranges, (12 pence;) 12 is, therefore, a product, and 3 one of its factors; and to find how many times 3 is contained in 12 is to find the other factor, which, multiplied into 3, will produce 12. This factor we find, by trial, to be 4, (4×3=12;) consequently, is contained in 12 4 times.

Ans. 4 oranges.

22. A man would divide 12 oranges equally among 3 children; how many oranges would each child have?

Here the object is to divide the 12 oranges into 3 equal parts, and to ascertain the number of oranges in each of

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those parts. The operation is evidently as in the last example, and consists in finding a number, which, multiplied by 3, will produce 12. This number we have already found to be 4.

Ans. 4 oranges apiece.

As, therefore, multiplication is a short way of performing many additions of the same number; so division is a short way of performing many subtractions of the same number; and may be defined, The method of finding how many times one number is contained in another; and also of dividing a number into any number of equal parts. In all cases, the process of division consists in finding one of the factors of a given product, when the other factor is known.

The number given to be divided, is called the dividend, and answers to the product in multiplication. The number given to divide by is called the divisor, and answers to one of the factors in multiplication. The result, or answer sought, is called the quotient, (from the Latin word quoties. how many?) and answers to the other factor.

Sign. The sign for division is a short horizontal line between two dots, \div . It shows that the number before it is to be divided by the number after it. Thus $27 \div 9 = 3$ is read, 27 divided by 9 is equal to 3; or to shorten the expression, 27 by 9 is 3; or 9 in 27 3 times. In place of the dots, the dividend is often written over the line, and the divisor under it, to express division; thus, $\frac{2}{9}7 = 3$, read as before.

The reading used by the pupil in committing the following table may be 2 by 2 is 1, 4 by 2, &c. or 2 in 2 one time, 2 in 4 two times, &c.

DIVISION TABLE.

$\frac{2}{3} = 1$	$\frac{3}{3} = 1$	$\frac{1}{2} = 1$	$\frac{5}{5} = 1$	$\frac{6}{6} = 1$	7 = 1
$\frac{1}{2} = 2$	$\frac{6}{3} = 2$	$\frac{9}{4} = 2$	$\psi = 2$	$\mathcal{C}=2$	4 = 2
$\frac{6}{2} = 3$	$\frac{9}{3} = 3$	$\frac{1}{4} = 3$	$\psi = 3$	$\frac{1}{6} = 3$	$2^{1} = 3$
$\frac{1}{3} = 4$	$\frac{1}{3} = 4$	$^{16}_{4} = 4$	$\frac{20}{6} = 4$	$\frac{24}{6} = 4$	
$\tilde{y} = 5$	$\ddot{y} = 5$	$\frac{20}{4} = 5$	$\frac{25}{5} = 5$		35 = 5
$\hat{y} = 6$	$\frac{138}{3} = 6$	$\frac{24}{4} = 6$	$\frac{30}{5} = 6$	$\frac{3.6}{6} = 6$	$4^2 = 6$
y = 7	$\frac{2}{3}$ 1 = 7	$\frac{28}{4} = 7$	$\frac{35}{5} = 7$	42 = 7	$\frac{4.9}{7} = 7$
5 = 8	$\frac{24}{3} = 8$	$3^2 = 8$	40 = 8	4,8 = 8	50 = 8
$\dot{y} = 9$	$\frac{27}{3} = 9$	$\frac{36}{4} = 9$	$\frac{45}{5} = 9$	54 = 9	$\frac{63}{7} = 9$

DIVISION TABLE-CONTINUED.

1 == 1	2 = 1	18=1	41 = 11	$\frac{13}{2} = 1$
16 = 2	$\psi = 2$	$\frac{28}{18} = 2$	$\frac{22}{11} = 2$	$\frac{74}{2} = 2$
$\frac{3}{3} = 3$	$\frac{2J}{9} = 3$	$\frac{38}{18} = 3$	$\frac{33}{11} = 3$	$\frac{36}{12} = 3$
$^{3^{2}}_{9} = 4$	$\frac{36}{9} = 4$	$\frac{18}{18} = 4$	11-4	$\frac{13}{2} = 4$
40 = 5	$\psi = 5$	$\frac{10}{10} = 5$	11=5	$\frac{60}{12} = 5$
$\psi = 6$	¥ = 6	$\frac{1}{2}\frac{1}{2}$	$\hat{\epsilon}\hat{\epsilon} = 6$	$\frac{72}{12} = 6$
$^{5}8^{6} = 7$	63 = 7	$\frac{18}{18} = 7$	11-7	112 = 7
64 = 8	y = 8	18 = 8	198 -8	$\frac{96}{12} = 8$
$\frac{7}{8}^2 = 9$	$\psi = 9$		$\frac{99}{17} = 9$	$\frac{108}{12} = 9$
$^{7}5^{2}=9$	$ \hat{n}=0$	$\frac{18}{28} = 3$	1 1 = 9	$\frac{108}{12} = 9$

 $28 \div 7$, or 28 = how many ? $49 \div 7$, or 49 = how many ? $42 \div 6$, or 42 = how many ? $32 \div 4$, or 32 = how many ? $54 \div 9$, or 32 = how many ? $99 \div 11$, or 91 = how many ? $91 \div 11$, or 91 = how many ? $91 \div 11$, or 91 = how many ? $91 \div 11$, or 91 = how many ? $91 \div 11$, or 91 = how many ? $91 \div 11$, or 91 = how many ?

¶ 16. 23. How many yards of cloth, at 4 shillings a yard, can be bought for 856 shillings?

Here the number to be divided is 856, which therefore is the dividend; 4 is the number to divide by, and therefore the divisor. It is not evident how many times 4 is contained in so large a number as 856. This difficulty will be readily evercome, if we decompose this number, thus:

856=800+40+16.

Beginning with the hundreds, we readily perceive that 4 is contained in 8 2 times; consequently, in 800 it is contained 200 times. Proceeding to the tens, 4 is contained in 4 1 time, and consequently in 40 it is contained 10 times. Lastly, in 16 it is contained 4 times. We now have 200+10+4=214 for the quotient, or the number of times 4 is contained in 856.

Ans. 214 yards.

We may arrive to the same result without decomposing the dividend, except as it is done in the mind, taking it by parts, in the following manner:

Dividend. For the sake of convenience, we Divisor, 4) 856 write down the dividend with the divisor on the left, and draw a line between them; we also draw a line underneath. Then, beginning on the left hand, we seek how often the

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divisor (4) is contained in 8, (hundreds,) the left hand figure; finding it to be 2 times, we write 2 directly under the 8, which falling in the place of hundreds, is in reality 200. Proceeding to tens, 4 is contained in 5 (tens) 1 time, which we set down in ten's place, directly under the 5 (tens.) But after taking 4 times ten out of the 5 tens, there is 1 ten left. This 1 ten we join to the 6 units, making 16. Then, 4 into 16 goes 4 times, which we set down, and the work is done.

This manner of performing the operation is called Short Division. The computation, it may be perceived, is carried on partly in the mind, which it is always easy to do when the divisor does not exceed 12.

RULE.

From the illustration of this example, we derive this general rule for dividing, when the divisor does not exceed 12:

1. Find how many times the divisor is contained in the first figure, or figures, of the dividend, and, setting it directly under the dividend, carry the remainder, if any, to the next figure as so many tens.

II. Find how many times the divisor is contained in this dividend, and set it down as before, continuing so to do till

all the figures in the dividend are divided.

PROOF. We have seen, (¶ 15,) that the divisor and quotient are factors, whose product is the dividend, and we have also seen, that dividing the dividend by one factor is merely a process for finding the other.

Hence division and multiplication mutually prove each

other.

To prove division, we may multiply the divisor by the quotient, and, if the work be right, the product will be the same as the dividend; or we may divide the dividend by the quotient, and, if the work is right, the result will be the same as the divisor.

To prove multiplication, we may divide the product by one factor, and, if the work be right, the quotient will be the other factor.

EXAMPLES FOR PRACTICE.

24. A man would divide 13,462,725 pounds among 5 men; how many pounds would each receive?

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17.

OPERATION.

Dividend.

Divisor, 5)13,462,725

Quotient, 2,692,545

,545

Proof.

Quotient.

2,692,545 5 divisor.

13,462,725

In this example, as we cannot have 5 in the first figure, (1) we take two figures, and say, 5 in 13 will go 2 times, and there are 3 over, which, joined to 4, the next figure, makes 34; and 5 in 34 will go 6 times, &c.

In proof of this example, we multiply the quotient by the divisor, and, as the product is the same as the dividend, we conclude that the work is right. From a bare inspection of the above example and refere stated, that division is the re-

its proof, it is plain, as before stated, that division is the reverse of multiplication, and that the two rules mutually prove each other.

25. How many yards of cloth can be bought for 4,354,560 shillings, at 2 shillings a yard? —— at 3 shillings? —— at 4 shillings? —— at 5 shillings? —— at 6 shillings? —— at 7? —— at 8? —— at 9? —— at 10?

Note. Let the pupil be required to prove the foregoing, and all of the following examples.

26. Divide 1005903360 by 2, 3, 4, 5, 6, 7, 8, 9, 10, 11,

and 12.

27. If 2 pints make a quart, how many quarts in 8 pints?

— in 12 pints? — in 20 pints? — in 24 pints? — in 248 pints? — in 3674 pints? — in 47632 pints?

28. Four quarts make a gallon; how many gallons in 8 quarts? — in 12 quarts? — in 20 quarts? — in 36 quarts? — in 368 quarts? — in 4896 quarts? in 5436144 quarts?

29. A man gave 86 apples to 5 boys; how many apples

would each boy receive?

Dividend.

Divisor, 5) 86

Quotient, 17-1 Remainder.

Here, dividing the number of the apples (86) by the number of boys, (5,) we find, that

each boy's share would be 17 apples; but there is 1 apple left.

¶ 17. 5)86

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In order to divide all the apples equally among the boys, it is plain, we must divide this one remaining apple into 5

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es equalwe must e into 5 requal parts, and give one of these parts to each of the boys. Then each boy's share would be 17 apples, and one fifth part of another apple; which is written thus, 17 apples.

Ans. $17\frac{1}{5}$ apples each. The 17, expressing whole apples, are called integers, (that is, whole numbers.) The $\frac{1}{5}$ (one fifth) of an apple, expressing part of a broken or divided apple, is called a fraction, that is a broken number.)

Fractions as we here see, are written with two numbers, one directly over the other, with a short line between them, showing that the upper number is to be divided by the lower. The upper number, or dividend, is, in fractions, called the numerator, and the lower number, or divisor, is valled the denominator.

Note. A number like 17 $\frac{1}{6}$, composed of integers (17) and a fraction, ($\frac{1}{6}$,) is called a mixed number.

In the preceding example, the one apple, which was left after carrying the division as far as could be by whole numbers, is called the remainder, and is evidently a part of the dividend yet undivided. In order to complete the division, this remainder, as we before remarked, must be divided into 5 equal parts; but the divisor itself expresses the number of parts. If, now, we examine the fraction, we shall see, that it consists of the remainder (1) for its numerator, and the divisor (5) for its denominator.

Therefore, if there be a remainder, set it down at the right hand of the quotient for the numerator of a fraction, under which write the divisor for its denominator.

Proof the last example.

171 5 86 In proving this example, we find it necessary to multiply our fraction by 5; but this is easily done, if we consider, that the fraction $\frac{1}{5}$ expresses one part of an apple divided into

5 equal parts; hence, 5 times $\frac{1}{5}$ is $\frac{5}{5}$ —1, that is, one whole apple, which we reserve to be added to the units, saying, 5 times 7 are 35, and one we reserved makes 36, &c.

30. Eight men drew a bounty of 458 pounds from government, how many pounds did each receive?

19.

Divisor, 8) 453

Quotient, 56%

Here, after carrying the division as far as possible by whole numbers, we have a remainder of 5 pounds, which, written as above directed, gives for the answer 56 pounds and § (five eighths) of another pound, to each man.

¶ 18. Here we may notice, that the eighth part of 5 pounds is the same as 5 times the eighth part of 1 pound, that is, the eighth part of 5 pounds is § of a pound. Hence, § expresses the quotient of 5 divided by 8.

Proof. § is 5 parts, and 8 times 5 is 40, that is, \$9=5, which, reserved and added to the product of 8 times 6, makes 53, &c. Hence, to multiply a fraction, we may multiply the numerator, and divide the product by the denominator.

Or, in proving division, we may multiply the whole number in the quotient only, and to the product add the remainder; and this, till the pupil shall be more particularly taught in fractions, will be more easy in practice. Thus, $56 \times 8 = 448$, and 448 + 5, the remainder, =453, as before.

31. There are 7 days in a week; how many weeks in 365 days?

Ans. 524 weeks.

32. When flour is worth 2 pounds a barrel, how many barrels may be bought for 25 pounds? how many for 51 pounds? —— for 7631 pounds?

33. Divide 640 pounds among 4 men.

640÷4, or 640=160 pounds, Ans. 34. 678÷6 or 648 how many?

Ans. 113.

35. 5040 = how many !

36. $72^{34} = \text{how many ?}$

37. ${}^{3}4_{9}^{64} = \text{how many }$ Ans. 384_{9}^{8} .

38. ${}^{2}76^{4} = \text{how many ?}$ 39. ${}^{4}6{}^{2}0^{1} = \text{how many ?}$

40. 20 140 12 = how many ?

¶ 19. 41. Divide 4370 pounds equally among 21 men. When, as in this example, the divisor exceeds 12, it is evident that the computation cannot be readily carried on in the mind, as in the foregoing examples. Wherefore, it is more convenient to write down the computation at length, in the following manner:

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OPERATION. Divisor, Dividend, Quotient. 21) 4370 (2084.

> 42 170 168

> > 2 Remainder.

W: may write the divisor and dividend as in short division, but, instead of writing the quotient under the dividend, it will be found more convenient to set it to the right hand.

Taking the dividend by parts, we seek how often we can have 21 in 43 (hundreds;) finding it to be 2 times, we set down 2 on the right hand of the dividend for the highest figure in the quotient. 43 being hundreds, it follows, that the 2 must be hundreds. This, however, we need not regard, for it is to be followed by tens and units, obtained from the tens and units of the lividend, and will therefore, at the end of the operation, e in the place of hundreds, as it should be.

It is plain that 2 (hundred) times 21 pounds ought now o be taken out of the dividend; therefore, we multiply the livisor (21) by the quotient figure 2 (hundred) now found, naking 42, (hundred,) which, written under the 43 in the lividend, we subtract, and to the remainder, 1, (hundred,)

bring down the 7, (tens,) making 17 tens.

We then seek how often the divisor is contained in 17, tens;) finding that it will not go, we write a cipher in the uotient, and bring down the next figure, making the whole We then seek how often 21 can be contained in 170, and, finding it to be 8 times, we write 8 in the quotient, and, nultiplying the divisor by this number, we set the product, 168, under the 170; then subtracting, we find the remainder to be 2, which, written as a fraction on the right hand of the quotient, as already explained, gives 208,4 pounds, or the answer.

This manner of performing the operation is called Long Division. It consists in writing down the whole computation.

From the above example, we derive the following

RULE.

Place the divisor on the left of the dividend, separate them by a line, and draw another line on the right of the dividend to separate it from the quotient.

II. Take as many figures, on the left of the dividend, as

contain the divisor once or more; seek how many times they contain it, and place the answer on the right hand of the dividend for the first figure in the quotient.

III. Multiply the divisor by this quotient figure, and write the product under that part of the dividend taken.

IV. Subtract the product from the figures above, and to the remainder bring down the next figure in the dividend, and divide the number it makes up, as before. So continue to do, till all the figures in the dividend shall have been brought down and divided.

Note 1. Having brought down a figure to the remainder, if the number it makes up be less than the divisor, write a cipher in the quotient, and bring down the next figure.

Note 2. If the product of the divisor, by any quotient figure, be greater than the part of the dividend taken, it is an evidence that the quotient figure is too large, and must be diminished. If the remainder at any time be greater than the divisor, or equal to it, the quotient figure is too small, and must be increased.

EXAMPLES FOR PRACTICE.

- 1. How many hogsheads of molasses, at 7 pounds a hogshead, may be bought for 6318 pounds?
- Ans. 9024 hogsheads.

 2. If a man's income be 1248 pounds a year, how much

is that per week, there being 52 weeks in a year?

Ans. 24 pounds per week.

- 3. What will be the quotient of 153598, divided by 29?

 Ans. 529614.
- 4. How many times is 63 contained in 30131?

Ans. $478\frac{17}{13}$ times; that is, 478 times, and $\frac{17}{63}$ of another time.

- 5. What will be the several quotients of 7652, divided by 16, 23, 34, 86, and 92 !
- 6. If a farm, containing 256 acres, be worth 1850 pounds, what is that per acre?
 - 7. What will be the quotient of 974932, divided by 365?
- 8. Divide 3228242 pounds equally among 563 men; how many pounds must each man receive? Ans. 5734 pounds.
- 9. If 57624 be divided into 216,586, and 976 equal parts, what will be the magnitude of one of each of these equal parts?

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Ans. The magnitude of one of the last of these equal parts will be 59 40g.

10. How many times does 1030603615 contain 3215 1

Ans. 320561 times.

11. The earth in its annual revolution round the sun, is said to travel 596088000 miles; what is that per hour. there being 8766 hours in a year !

12. 1234567890 how many !

13. 40703020 how many?

14. 987619031 = how many ?

CONTRACTIONS IN DIVISION.

When the DIVISOR is a COMPOSITE

¶ 20. 1. Bought 15 yards of cloth for 30 pounds; how

much was that per yard?

15 yards are 3×5 yards. If there had been but 5 yards, the cost of ane yard would be 30=6 pounds; but as there are 3 times 5 yards, the cost of one yard will evidently be but one third part of 6 pounds; that is, \=2 pounds, Ans.

Hence, when the divisor is a composite number, we may, if we please, divide the dividend by one of the component parts, and the quotient, arising from that division, by the other; the last quotient will be the answer.

2. If a man can travel 24 miles in a day, how many days

will it take him to travel 264 miles?

It will evidently take him as many days as 264 contains 24. OPERATION.

$24=6\times4$.	6)264		24)264(11 days, Ans.	
		or,	24	
	4)44		-	
139 15 1 .			24	
1 21 13 1843 1114	11 day	8.	24	

3. Divide 576 by $48 = (8 \times 6.)$

4. Divide 1260 by $63 = (7 \times 9.)$

5. Divide 2430 by 81.

6. Divide 448 by 56.

II. To divide by 10, 100, 1000, &c.

1. A note of 2478 pounds is owned by 10 men; what is each man's share?

Each man's share will be equal to the number of tens contained in the whole sum, and, if one of the figures be cut off at the right hand, all the figures to the left may be considered so many tens; therefore, each man's share will be 247 % pounds.

It is evident, also, that if 2 figures had been cut off from the right, all the remaining figures would have been so many hundreds; if 3 figures, so many thousands, &c. Hence. we derive this general RULE for dividing by 10, 100, 1000. &c. : Cut off from the right of the dividend so many figures as there are ciphers in the divisor; the figures to the left of the point will express the quotient, and those to the right. the remainder.

2. How many 100 in 42400 ! Ans. 424. Here the divisor is 100; we therefore cut off 2 424 00 figures on the right hand, and all the figures to the left (424) express the number of hundreds. Ans. 345 57

3. How many 100 in 34567 ? 4. How many hundreds in 4567840 hundreds?

5. How many hundreds in 345600 hundreds!

6. How many 100 in 42604 hundreds ? Ans. 426 140 7. How many thousands in 4000 ! -- in 25000 !

8. How many thousands in 6487 thousands 1 Ans. 6487 9. How many thousands in 42863 thousands? —— in 368456 thousands ? -- in 96842378 thousands !

10. How many tens in 40? in 400? in 20? in 468? in 4784 ? in 34640 ?

III. When there are CIPHERS on the right hand of the divisor.

7 22, 1. Divide 480 pounds among 40 men ! OPERATION.

4|0)48|0

12 pounds, Ans.

In this example, our divisor, (40,) is a composite number.

 $(10\times4=40;)$ we may therefore, divide by one component part, (10,) and that quotient by the other, (4;) but to divide by 10, we have seen, is but to cut off the right hand figure, leaving the figures to the left of the point for the quotient, which we divide by 4, and the work is done. It is evident, that, if our divisor had been 400, we should have cut off 2 figures, and have divided in the same manner; if 4000, 3 figures, &c. Hence, this general RULE : When there are ciphers at the right hand

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of the divisor, cut them off, and also as many places in the dividend: divide the remaining figures in the dividend by the remaining figures in the divisor; then annex the figures cut off from the dividend, to the remainder.

2. Divide 748346 by 8000.

Dividend.

Divisor, 8|000)748|346.

Quotient, 93 .- 4346 Remainder. Ans. 934844

3. Divide 46720367 by 4200000.

Dividend.

42|00000)467|20367(11 420467 Quotient.

47

42

520367 Remainder.

4. How many pieces of cloth can be bought for 346500 pounds, at 20 pounds per piece ?

5. Divide 76428400 by 900000. 6. Divide 345006000 by 84000.

7. Divide 4680000 by 20, 200, 2000, 20000, 3000, 4000. 50, 600, 70000, and 80.

SUPPLEMENT TO DIVISION.

QUESTIONS.

1. What is division? 2. In what does the process of division consist? 3. Division is the reverse of what? 4. What is the number to be divided called, and to what does it answer in multiplication? 5. What is the number to divide by called, and to what does it answer, &c.? 6. What is the result or answer called, &c.? 7. What is the sign of division, and what does it show? 8. What is the other way of expressing division? 9. What is short division, and how is it performed? 10. How is division proved? 11. How is mustiplication proved? 12. What are integers, or whole numbers? 13. What are fractions, or broken numbers? 14. What is a mixed number? 15. When there is any thing left after division, what is it called, and how is it to be written? 16. How are fractions written? 17. What is the upper number called? 18. --the lower number? 19. How do you multiply a fraction? 20. To what do the numerator and the denominator of a fraction answer in division? 21. What is long division? 22. Rule? 23. When the divisor is a composite number, how may we proceed? 24. When the divisor is 10, 100, or 1000, &c. how may the operation be contracted? 25. When there are ciphers at the right hand of the divisor how may we proceed?

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EXERCISES.

1. An army of 1500 men, having plundered a city, took 2625000 pounds; what was each man's share?

2. A certain number of men were concerned in the payment of 18950 pounds, and each man paid 25 pounds; what was the number of men?

3. If 7412 eggs be packed in 34 baskets, how many in a basket 1

4. What number must I multiply by 135 that the product may be 505710?

5. Light moves with such amazing rapidity, as to pass from the sun to the earth in about the space of 8 minutes. Admitting the distance, as usually computed to be 95000000 miles, at what rate per minute does it travel?

6. If the product of two numbers be 704, and the multiplier be 11, what is the multiplicand?

Ans. 64.

7. If the product be 704, and the multiplicand 64, what is the multiplier?

8. The divisor is 18, and the dividend 144; what is the quotient?

9. The quotient of two numbers is 8, and the dividend 144; what is the divisor?

10. A man wishes to travel 585 miles in 13 days; how many miles must be travel each day?

11. If a man travels 45 miles a day, in how many days will he travel 585 miles?

12. A man sold 140 cows for 560 pounds; how much was that for each cow?

13. A man, selling his cows for 4 pounds each, received for all 560 pounds; how many cows did he sell?

14. If 12 inches make a foot, how many feet are there in 364812 inches 1

15. If 364812 inches are 30401 feet, how many inches make 1 foot?

17. If you would divide 48750 pounds among 50 men, how many pounds would you give to each one?

16. If you distribute 48750 pounds among a number of men, in such a manner as to give to each one 975 pounds, how many men receive a share?

18. A man has 17484 pounds of tea in 186 chests; how many pounds in each chest?

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19. A man would put up 17484 pounds of tea into chests containing 94 pounds each; how many chests must be have?

20. In a certain town there are 1740 inhabitants, and 12 persons in each house; how many houses are there? ——in each house are 2 families, how many persons in each family?

21. If 2760 men can dig a certain canal in one day, how many days would it take 46 men to do the same? How many men would it take to do the work in 15 days? —— in 5 days? —— in 20 days? —— in 120 days?

22. If a carriage wheel turns round 62280 times in running from Quebec to Montreal, a distance of 180 miles, how many times does it turn in running 1 mile?

Ans. 346.

24. Sixty minutes make one hour; how many hours in 1440 minutes? —— in 10080 minutes? —— in 40320 minutes? —— in 525960 minutes?

26. How many times can I subtract forty-eight from four hundred and eighty?

27. How many times 3478 is equal to 47854?

28. A bushel of grain is 32 quarts; how many quarts must I dip out of a chest of grain to make one half (1) of a bushel? —— for one fourth (1) of a bushel? —— for one eighth (1) of a bushel? —— for one

eighth ($\frac{1}{8}$) of a bushel?

29. How many is $\frac{1}{2}$ of 20? $\frac{1}{2}$ of 48? $\frac{1}{2}$ of 247? $\frac{1}{2}$ of 345878? $\frac{1}{2}$ of 204030648?

Ans. to the last, 1020153324.

30. How many walnuts are one third part (\frac{1}{3}) of 3 walnuts? \(\frac{1}{3} \) of 6 walnuts? \(\frac{1}{3} \) of 30? \(\frac{1}{3} \) of 45? \(\frac{1}{3} \) of 300? \(\frac{1}{3} \) of 3456320? \(\frac{1}{3} \) of the last, 1152(\text{0}62); \(\frac{1}{3} \) of 7843? \(\frac{1}{3} \) of 20? \(\frac{1}{3} \) of the last, 1860?

MISCELLANEOUS QUESTIONS,

Involving the principles of the preceding rules.

Note. The preceding rules, viz. Numeration, Addition.
E. 2

Subtraction, Multiplication, and Division, are called the Fundamental Rules of Arithmetic, because they are the foundation of all other rules.

 A man bought a chaise for 57 pounds, and a horse for 34 pounds; what did they both cost?

2. If a horse and chaise cost 91 pounds, and the chaise cost 57 pounds, what is the cost of the horse? If the horse cost 24 pounds, what is the cost of the chaise?

3. If the sum of 2 numbers be 487, and the greater number be 348, what is the less number? If the less number be

139, what is the greater number?

4. If the minuend be 7842, and the subtrahend 3481, what is the remainder? If the remainder be 4361, and the minuend be 7842, what is the subtrahend?

¶ 23. When the minuend and the subtrahend are given, how do you find the remainder?

When the minuend and remainder are given, how do you

find the subtrahend?

When the subtrahend and the remainer are given, how do you find the minuend?

When you have the sum of two numbers, and one of them given, how do you find the other?

When you have the greater of two numbers, and their difference given, how do you find the less number?

When you have the less of two numbers, and their difference given, how do you find the greater number?

5. The sum of two numbers is 48, and one of the numbers is 19; what is the other?

6. The greater of two numbers is 29, and their difference 10; what is the less number?

7. The less of two numbers is 19, and their difference is 10; what is the greater?

8. A man bought 5 pieces of cloth at 44 pounds a piece; 974 dozen of shoes, at 3 pounds a dozen; 600 pieces of calico, at 6 pounds a piece; what is the amount?

9. A man sold six cows at 5 pounds each, and a yoke of oxen, for 19 pounds; in pay, he received a chaise, worth 31 pounds, and the rest in money; how much money did he receive?

10. What will be the cost of 15 pounds of butter, at 7 pence per pound?

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11. How many bushels of wheat can you buy for 4870 shillings, at 8 shillings per bushel?

¶ 24. When the price of one pound, one bushel, &c. of any commodity is given, how do you find the cost of any number of pounds, or bushels, &c. of that commodity? If the price of the 1 pound, &c. be in shillings, in what will the whole cost be? If in pence, what?

When the cost of any given number of pounds, or bushels, &c. is given, how do you find the price of one pound or bushel, &c. In what kind of money will the answer be?

When the cost of a number of pounds, &c. is given, and also the price of one pound, &c. how do you find the number of pounds, &c.

12. When rye is 4 shillings per bushel, what will be the cost of 212 bushels ?

13. See 8 pounds of tea cost 173 pounds, (that is 41520 pence) what is the price of one pound?

When the factors are given, how do youfind the product?
When the product and one factor are given, how do you find the other factor?

When the divisor and quotient are given, how do you find the dividend?

When the dividend and quotient are given, how do you find the divisor?

14. What is the product of 754 and 25?

15. What number multiplied by 25, will produce 18850? 16. What number, multiplied by 754, will produce 18850?

17. If a man save 5 pence a day, how many pence would he save in a year, (365 days,)? —— how many in 45 years? How many cows could he buy with the money, at 742 pence each?

18. A boy bought a number of apples; he gave away ten of them to his companions, and afterwards bought thirty-four more, and divided half of what he then had among four companions, who received 8 apples each; how many apples did the boy first buy?

Let the pupil take the last number of apples, 8, and reverse the process.

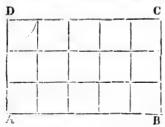
Ans. 40 apples.

19. There is a certain number, to which, if 4 be added, and 7 be subtracted, and the difference be multiplied by 8, and the product divided by 3, the quotient will be 64; what is that number?

Ans. 27.

20. A board has 8 rows of 8 squares each; how many squares on the board?

* 25. 21. There is a spot of ground 5 rods long, and 3 rods wide; how many square rods does it contain?



Note. A square rod is a square (like one of those in the annexed figure) measuring a rod on each side. By an inspection of the figure, it will be seen, that there are as many squares in a row as rods on one side, and that the number of

rows is equal to the number of rods, on the other side; therefore, $5 \times 3 = 15$, the number of squares. Ans. 15 square rods.

A figure, like A, B, C, D, having its opposite sides equal and parallel, is called a parallelogram or oblong.

22. There is an oblong field, 40 rods long, and 24 rods

wide; how many square rods does it contain?

23. How many square inches in a board 12 inches long, and 12 inches broad?

Ans. 144.

24. How many square feet in a board 14 feet long and 2 feet wide?

25. A certain township is six miles square; how many square miles does it contain?

Ans. 36.

26. A man bought a lot of land for 2246 pounds; he sold one half of it for 1175 pounds at the rate of 3 pounds per acre; how many acres did he buy! and what did it cost him per acre!

27. A boy bought a sled for 56 pence, and sold it again for 8 quarts of walnuts; he sold one half of the nuts at 8 pence a quart, and gave the rest for a penknife, which he sold for 18 pence; how many pence did he lose by his bargains?

28. In a certain school-house, there are 5 rows of desks; in each row are six seats, and each seat will accommodate 2 pupils; there are also two rows, of 3 seats each, of the same size as the others, and one long seat where 8 pupils may sit; how many scholars will this house accommodate?

Ans. 80.

20. How many square feet of boards will it take for the

floor of 12 squar 30. T

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floor of a room 16 feet long, and 15 feet wide, if we allow 12 square feet for waste ?

30. There is a room 6 yards long and 5 yards wide; how many yards of carpeting, a yard wide, will be sufficient to cover the floors, if the hearth and fireplace occupy 3 square yards ?

31. A board, 14 feet long, contains 28 square feet; what

is its breadth ?

32. How many pounds of pork, worth 4 pence a pound,

can be bought for 144 pence?

33. How many pounds of butter, at 9 pence per pound, must be paid for 25 pounds of tea, at 38 pence per pound?

34. 4+5+6+1+8 = how many 1

35. 4+3+10-2-4+6-7 = how many ?

36. A man divides 30 bushels of potatoes among 3 poor men; how many bushels does each man receive! What is 1 of thirty? How many are 2 (two thirds) of 30?

37. How many are one third (1) of 3?

- of 9! -- of 282! -- of 45674312!

38. How many are two thirds (4) of 3!

- of 9 ! - of 282 ! - of 45674312 !

39. How many are 1 of 40? —— 3 of 40? 60? — 3 of 60? — 1 of 80? — of 124? — of --- 3 of 246876 1

40. How many is \(\frac{1}{2} \) of 80? \(\lefta \) \(\frac{1}{2} \) of 100?

41. An inch is one twelfth part $(\frac{1}{12})$ of a foot; how many feet in 12 inches? — in 24 inches? — in 36 inches! -- in 12243648 inches?

42. If 4 pounds of tea cost 128 pence, what does 1 pound cost? —— 2 pounds ? —— 3 pounds? --- 100 pounds ?

43. When oranges are worth 4 pence apiece, how many

can be bought for 1464 pence?

44. The earth, in moving round the sun, travels at the rate of 68000 miles an hour; how many miles does it travel in one day, (24 hours?) how many miles in one year, (365 days?) and how many days would it take a man to travel this last distance, at the rate of 40 miles a day? how many years ? Ans, to the last, 40800.

45. How many pence can a man earn in 20 weeks, at

35 pence per day, Sundays excepted ?

46. A man married at the age of 23; he lived with his

wife 14 years; she then died, leaving him a daughter, 12 years of age; S years after the daughter was married to a man 5 years older than herself, who was 40 years of age when the father died; how old was the father at his death?

Ans. 60.

47. There is a field 20 rods long, and 8 rods wide; how many square rods does it contain?

Ans. 160 rods.

48. What is the width of a field, which is 20 rods long,

and contains 160 square rods.

49. What is the length of a field, 8 rods wide, and containing 160 square rods ?

50 What is the width of a piece of land, 25 rods long, and containing 400 square reds?

COMPOUND NUMBERS.

7 26. A number expressing things of the same kind is called a simple number; thus, 100 men, 56 years, 75 cents, are each of them simple numbers; but when a number expresses things of different kinds, it is called a compound number; thus, 46 pounds 7 shillings and 6 pence, is a compound number; so 4 years 6 months and 3 days, 43 dollars 25 cents and 3 mills, are compound numbers.

Note. Different kinds, or names, are usually called dif-

ferent denominations.

RIDD FOTION.

T 27. In this Province as in England, money is reckoned in pounds, shillings, pence and farthings. In the
United States, money is reckoned in dollars, cents and mills.
These are called denominations of money. Time is reckoned in years, months, weeks, days, hours, minutes, and
seconds, called denominations of time. Distance is reckoned in miles, rods, feet, and inches, called denominations
of measure, &c.

The relative value of these denominations is exhibited in tables, which the pupil must commit to memory.

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HALIFAX CURRENCY.

The present currency of Lower Canada, is called Halifax currency, having been introduced into this Province, after its cession to Great Britain, by France, in 1763, from Nova Scotia. The denominations are the same in name as the denominations of English money, i. e. pounds, shillings, pence, and farthings; and the ratios of the different denominations to each other are the same as in English money, i. e. the shilling is one twentieth of the pound, the perny one twelfth of the shilling, and the farthing one fourth of the penny. In value they are different, as will be seen in the ¶ upon reduction of currencies; where the ratio of each to the other, and of both to Federal Money is exhibited, with the method of ascertaining them in practice, for particular sums.

2 farthings	(qrs.)	maku	1	half-penny,	marked	₫đ.
4 "	"	**	1	penny,	**	d.
12 pence		**	1	shilling,	661	s.
20 shillings		"	1	pound,	***	£.

Note. Farthings are often written as the fraction of a penny; thus, I farthing is written 4d., 2 farthings, 2d., 3 farthings, 2d.

It will be proper to insert here a list of the gold and silver coins, made current by law in the Province of Lower Canada, with their several weights and values annexed.

GOLD COINS.

English, American, and Portuguese.

DENOMINATION.	WEIGHT.	VALUE.	ă.
A Guinea,	prots. grs. 6	1 3). 4
A Half Guinea,	2 15	0 11	8
A third Guinea,	1 18	0 7	9
A Johannes,	18 0	.4 .0	0
A half Johannes,	9 0	2 0	0
A Moidore,	6 18	1 10	0
An Eagle,	11 6	2 10	0
A half Eagle,	5 15	1 5	0.

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GOLD COINS-CONTINUED.

French and Spanish.

DENOMINATION.	WEL	GHT.	1	ALU	E.
A Doubloon,	picts.	grs.	£ 3	14	d. 6
A half Doubloon, -	8	12	1	17	3
A Louis d'Or, coined before 1793.	5	4	1	2	8
A Pistole, coined before 1793.	4	4	. 0	18	3
The 40 Francs piece, coined before 1792.	8	6	1	16	2
The 40 Francs piece, coined since 1792.	8	6	1	16	2
The 20 Francs piece, coined before 1792.	4	3	0	18	1
The 20 Francs piece, coined since 1792.	4	3	0	18	1
SILVER CO	INS.	1,			
A Crown,	-	Ī	0	5	6
An English shilling,	-	l	0	1	-1
A Dollar,	-		0	5	0
A Pistareen,	-		0 .	0	10
A half Pistareen,	-		0	0	5
The American Dollar,	-		0	5	0
A French piece of 4 livres 10 sols	Tour	nois,	0	4	2
A French piece of 6 livres, -	-		0	5	6

The statute provides, that "all the higher and lower denominations of the above gold and silver coins, shall also pass current, and be deemed a legal tender in payment of all debts, and demands whatsoever, in this Province, in the same proportions, respectively."

0.

The piece of 5 Francs Tournois, coined

The French piece of 36 sols Tournois,

The French piece of 24 sols Tournois,

since 1792,

Two pence furthing is allowed for every grain over, or under the legal weight, on English, American, and Portuguese gold; and two pence and one fifth, for every grain over or under the legal weight, on French and Spanish gold.

Payments in gold above twenty pounds shall be made in bulk, where one of the parties making or receiving the

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ain over, or and Portu y grain over ish gold.

be made in ceiving the

same shall require it; English, American, and Portuguese gold at eighty-nine shillings per ounce Troy; French, and Spanish gold at eighty-seven shillings and eight pence halfpenny per ounce Troy :-- and a deduction shall be made of 1 grain Troy, for each piece of gold coin so weighed, as a compensation to the receiver for the loss that may accrue in afterwards paying away the same by the single piece.

In copper coin no person is obliged to receive more than

one shilling at one payment.

How many farthings in 1 How many pence in 4 farpenny? — in 2 pence? things? — in 8 farthings? — in 3 pence? — in 6 — in 12 farthings? — in pence? — in 8 pence? — 24 farthings? — in 32 farin 9 pence? — in 12 pence? things? — in 36 farthings? - in 1 shilling ! - in 2 - in 48 qrs. ! How many shillings in 48 grs.? — in shillings ?

How many pence in 2 shil- 96 qrs. ? lings? — in 3 s.? — in How many shillings in 24
4 s.? — in 6 s.? — in pence? — in 36d.? —
8 s.? — in 10 s.? — in 2 in 48d.? — in 72d.? shillings and 2 pence ? - in 96d. ? - in 120d. ? in 2s. 3d. 1 — in 2s. 4d. 1 in 26d. 1 — in 27d. 1 in 28d, 1 --- in 30d, 1 -- in 4s. 3d. ?

How many shillings in 1 in 42d.? - in 51d.? pound? — in $2\mathcal{L}$.? — How many pounds in 20 shiltings? — in $4\mathcal{L}$.? — lings? — in 40 s.? — in in $4\mathcal{L}$. 6s? — in 80 s.? — in - in $3\pounds$. 10s. ? — in 86s. ? — in 128s. ? — in 2£s. ? — in 55s. ? 2£. 15s. ?

The changing of one kind, or denomination, into another kind, or denomination, without altering their value, is called Reduction. (¶ 27.) Thus, when we change shillings into pounds, or pounds into shillings, we are said to reduce them. From the foregoing examples, it is evident, that, when we reduce a denomination of greater value into a denomination of less value, the reduction is performed by multiplication; and it is then called Reduction Descending. But when we reduce a denomination of less value into one of greater value, the reduction is performed by division; it is then called Reduction Ascending. Thus, to reduce pounds

to shillings, it is plain, we must multiply by 20. And again, to reduce shillings to pounds, we must divide by 20. It follows, therefore, that reduction descending and ascending reciprocally prove each other,

1. In 17£. 13s. 63d. how many farthings?

OPERATION.

£. s. d. qrs. 17 13 6 3 20s.

353s. in 17£. 13s. 12d.

42424.

4q.

16971 grs. the Ans.

In the above example, because 20 shillings make pound, therefore we multiply product by the addition of the given shillings, (13,) which, it is evident, must always be done in like cases; then, because 12 pence make 1 shilling, we multiply the shillings (353) by 12, adding in the given pence, (6.) (4242) by 4, adding in the stitute the answer. then find, that in 17£. 13s. farthings.

2. In 16971 farthings, how many pounds?

OPERATION. Farthings in a penny, 4) 16971 3qrs.

Pence in a shilling, 12)4242 6d.

Shillings in a pound, 20353 13s.

17£. Ans. 17£. 13s. 63d.

Farthings will be reduced to pence, if we divide them by 4, because every 4 farthings make 1 penny. There-17£. by 20, increasing the fore, 16971 farthings divided by 4, the quotient is 4242 pence, and a remainder of 3, which is farthings, of the same name as the dividend. We then divide the pence (4242) by 12, reducing them to shillings; and the shillings Lastly, (353) by 20, reducing them to pounds. The last quotient, penny, we multiply the pence 17£., with the several re-

Note. In dividing 353s. by 64d., are contained 1697120, we cut off the cipher, &c., as taught ¶ 22.

¶ 28. The process in the foregoing examples, if carefully examined, will be found to be as follows, viz.

To reduce high denominations To reduce low denominations to lower,--Multiply the high-to higher,--Divide the lowest est denomination by that num-denomination given by that

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71 3qrs.

42 6d.

35|3 13s.

17£. 13s. 6¾d. reduced

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he pence sing them e shillings sing them quotient, everal resyrs. con-

g 353s. b**y** pher, &c.,

s, if carez.

ominations the lowest n by that ber which it takes of the next number which it takes of the less to make 1 of this higher, same to make 1 of the next (increasing the product by the higher. Proceed in the same number given, if any, of that manner with each succeeding less denomination.) Proceed denomination, until you have in the same manner with each brought it to the denomination required.

In the two examples, from which the above general rules are deduced, the denominations are pounds, shillings, pence and farthings, considered as in Halifax Currency; but it is obvious that these rules can be applied to all currencies where the denominations are the same; or to currencies in which the denominations are different; and in general to all compound numbers.

EXAMPLES FOR PRACTICE.

3.	Reduce	20£. 14s. 2d. to pence.	Ans. 4970.
4.		24£. to farthings.	Ans. 23040.
5.	**	66£. 6s. 6d. to pence.	Ans. 15912.
6.		158£. to farthings.	Ans. 151680.
7.	66	1234£. 15s. 7d. to farthings.	
8.	66	337587 farthings to pounds, &	C *
		Ans. 351	£. 13s. 0d. 3q.
9.	"	1185388 farthings to pounds,	&c.
			234£. 150. 7d.

10. Reduce 32£. 15s. 8d. 11. Reduce 31472 farthings to farthings.

12. In 29 guineas, at 1£. 13. In 38976 farthings, how 3s. 4d. each, how many qrs. 1 many guineas?

14. Reduce \$163, at 6s, each, to pence ?

15. Reduce 11736 pence to dollars.

16. In 15 guineas, how 17. Reduce 21£. to guinmany pounds?

Note. We cannot reduce guineas directly to pounds, but we may reduce the guineas to shillings, and then the shillings to pounds.

OLD CURRENCY.

12 deniers make 1 sou.
20 sous 1 livre, or franc.

The livre is 10d. Halifax currency.

In 32 livres 10 sous, how many sous?
In 97 livres 11 sous, how many sous?
In 650 sous, how many livres?
In 1951 sous, how many livres?
In 10 livres 6 sous 9 deniers, how many deniers?
How many pounds currency in 96 livres?

FEDERAL MONEY.

Tederal money is the coin of the United States. The kinds, or denominations, are eagles, dollars, dimes, cents, and mills.

TABLE.

	mills		••	-		are	equal	to	-	1	cent.
10	cents,	(=	:100	mills,)		-	-	-		=1	dime.
10	dimes,	(=	=100	cent=	=1000	m	ills,)	-		=1	dollar.
10	dollars	, (=	=100	dimes:	=1000	cen	to ==10	1000	nills)	=1	eagle.*

Sign. This character, \$, placed before a number, shows it to express federal money.

As 10 mills make a cent, 10 cents a dime, 10 dimes a dollar, &c. it is plain, that the relative value of mills, cents, dimes, dollars and eagles corresponds to the orders of units, tens, hundreds, &c. in simple numbers. Hence, they may be read either in the lowest denomination, or partly in a higher, and partly in the lowest denomination. Thus:

3 4 6 5 2 may be read, 34652 mills; or 3465 cents and 2 mills; or, reckoning the eagles tens of dollars, and the

may Fo is pla figure figure Thus dollar dollar quirin places point, but on with a 10 mi ceed 9 one pl

dime

Note tionally pressed

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ident (cents, cents a

Write and 2 m mills; mill; 2 cents an five cen

^{*}The eagle is a gold coin, the dollar and dime are silver coins, the cent is a copper coin. The mill is only imaginary, there being no coin of that denomination. There are half eagles, half dollars, half dimes, and half cents, real coins.

[†] The ch the comma comma us

dimes tens of cents, which is the usual practice, the whole may be read, 34 dollars 65 cents and 2 mills.

For ease in calculating, a point (1) called a separatrix, is placed between the dollars and cents, showing that all the figures at the left hand express dollars, while the two first figures at the right hand express cents, and the third, mills. Thus, the above example is written \$34.652; that is, 34 dollars 65 cents 2 mills, as above. As 100 cents make a dollar, the cents may be any number from 1 to 99, often requiring two figures to express them; for this reason, two places are appropriated to cents, at the right hand of the point, and if the number of cents be less than ten, requiring but one figure to express them, the ten's place must be filled with a cipher. Thus, 2 dollars and 6 cents are written 2.06. 10 mills make a cent, and consequently the mills never exceed 9, and are always expressed by a single figure. Only one place, therefore, is appropriated to mills, that is, the place immediately following cents, or the third place from the point. When there are no cents to be written, it is evident that we must write two ciphers to fill up the places of Thus, 2 dollars and 7 mills are written 2007. Six cents are written, 06, and 7 mills are written '007.

Note. Sometimes 5 mills = \frac{1}{2} a cent is expressed fractionally: thus, '125 (twelve cents and five mills) is expressed 124, (twelve and a half cents.)

Write down 470 dollars 2 cents; 342 dollars 40 cents and 2 mills; 100 dollars, 1 cent and 4 mills; 1 mill; 2 mills; 3 mills; 4 mills; ½ cent, or 5 mills; 1 cent and 1 mill; 2 cents and 3 mills; six cents and one mill; sixty cents and one mill; four dollars and one cent; three cents; five cents; nine cents.

ted States. rs, dimes,

l cent. =1 dime. =1 dollar. =1 eagle.*

ber, shows

10 dimes a nills, cents, rs of units, they may partly in a Thus:

ents and 2 s, and the

[†] The character used for the separatrix, in the "Scholars' Arithmetic," was the comma; the comma inverted is here adopted, to distinguish it from the comma used in punctuation

the cent is a function that denompalf cents, real

REDUCTION OF FEDERAL MONEY.

¶ ?9. How many mills in one cent ! — in 2 cents ? — in 3 cents ! — in 4 cents ! — in 6 cents ! — in 9 cents ! — in 10 cents ! — in 30 cents ! — in 78 cents ! — in 100 cents, (=1 dollar) ! — in 2 dollars ? — in 3 dollars ! — in 4 dollars ! — in 484 cents ! — in 563 cents ! — in 1 cent and 2 mills ! — in 4 cents and 5 mills !

How many cents in 2 dollars? — in 4 dollars? — in 8 dollars? — in 3 dollars and 15 cents? — in 5 dollars and 20 cents? — in 8 dollars and 20 cents? — in 4 dollars and 6 cents?

How many dollars in 400 cents? — in 600 cents? — in 380 cents? — in 40765 cents? How many cents in 1000 mills? — in 8000 mills? — in 4378 mills? — in 846732 mills?

As there are 10 mills in one cent, it is plain that cents are changed or reduced to mills by multiplying them by 10, that is, by merely annexing a cipher, (¶ 12.) 100 cents make a dollar; therefore dollars are changed to cents by annexing 2 ciphers, and to mills by annexing 3 ciphers. Thus, 16 dollars = 1600 cents = 16000 mills. Again, to change mills back to dollars, we have only to cut off the three right hand figures, (¶ 21;) and to change cents to dollars, cut off the two right hand figures, when all the figures to the left will be dollars, and the figures to the right, cents and mills.

Reduce 34 dollars to cents.

Reduce 240 dollars and 14 cents to cents.

Ans. 3400.

Ans. 24014 cents. Reduce \$748'143 to mills. Ans. 748143 mills. Reduce 748143 mills to dollars. Ans. \$748'143. Reduce 3467489 mills to dollars. dns. 3467'489. Reduce 48742 cents to dollars. Ans. \$487'42. Reduce 1234678 mills to dollars. Reduce 3469876 cents to dollars. Reduce \$4867'467 to mills. Reduce 984 mills to dollars. Ans. \$ '984. Reduce 7 mills to dollars. Ans. \$ '007. Reduce 8 '014 to mills. Reduce 17846 cents to dollars.

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— in 3
—in 563
15 mills !
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y 10, that ts make a mnexing 2 as, 16 dolange mills right hand out off the ne left will mills.

Ans. 3400.

014 cents. 3143 mills. \$748'143. 3467'489.

ns. \$ 1984. ns. \$ 1007. Reduce 984321 cents to mills.

Reduce 96174 cents to dollars.

Ans. \$96 171.

Reduce $2061\frac{1}{2}$ cents, 503 cents, 106 cents, $921\frac{1}{2}$ cents, 500 cents, $726\frac{1}{4}$ cents, to dollars.

Reduce 86753 mills, 96000 mills 6042 mills, to dollars.

TROY WEIGHT.

#31. It is established by law, that the pound Troy, with its parts, multiples, and proportions, shall be the standard weight for weighing gold* and silver in coin or bullion, drugs, and precious stones. The denominations of Troy weight are pounds, ounces, pennyweights and grains.

TABLE.

24 grains (grs.) make I pennyweight, marked pwt.

20 pennyweights -- 1 ounce, ---- oz.

12 ounces ---- 1 pound, ---- 1b.

1. How many grains in a 2. In 19680 grains how silver tankard weighing 3 lb. many pounds, &c. 5 oz.?

3. Reduce 210 lb. 8 oz. 12 4. In 50572 pwt. how mapwts, to pennyweights.

5. In 7 lb. 11 oz. 3 pwt. 6. Reduce 45681 grains to 9 grs. of silver, how many pounds. grains?

APOTHECARIES' WEIGHT.

Apothecaries' weight† is used by apothecaries and physicians, in compounding medicines. The denominations are pounds, ounces, drams, scruples, and grains.

TABLE.

20	grains	(0	re '	m	ake	1	scruple,	m	a rk	ho	a.
							dram,	111	ai K	cu	5.
	drams						ounce,				z.
12	ounces	_	-		1		round.	_			Ĭb.

The fineness of gold is tried by fire, and is reckoned in CARATS, by which is understood the 24th part of any quantity; if it lose nothing in the trial, it is said to be 24 carots fine; if it lose 2 carats, it is then 22 carats fine, which is the standard for gold.

Silver which abides the fire without loss is said to be 12 ounces fine. The standard for silver coin is 11 oz. 2 pwts. of fine silver, and 18 pwts. of copper melted together.

† The pound and ounce apothecaries' weight and the pound and ounce Troy, are the same, only differently divided, and subdivided. 7. In 9 lb 83. 1 3. 2 9. 8. Reduce 55799 grs. to 19 grs., how many grains. pounds.

AVOIRDUPOIS WEIGHT.*

It is established by law that the pound Avoirdupois with its parts, &c. shall be considered as the standard for weighing every thing commonly sold by weight, except those articles, in weighing which, Troy weight is used. The denominations are tons, hundreds, quarters, pounds ounces, and drams.

TABLE.

16	drams,	(dr	s.)	n	nal	(e	1	ounce,	-	ma	ırk	ed	-	oz.
16	ounces	**	-	~	-	-	1	pound,	-	-	•	-		ib.
28	pounds	-	**	-	-	-	.1	quarter,	-	-	-	-		qr.
. 4	quarters		-	-	**	-	1	hundred	w	eigh	t,	-	-	cwt.
20	hundred	W	eig	ht	-		1	ton, -	,-	-		· ·	•	T.

Note 1. In this kind of weight, the words gross and net are used. Gross is the weight of the goods, together with the box, bale, bag, cask, &c, which contains them. Net weight is the weight of the goods only, after deducting the weight of the box, bale, bag, or cask, &c., and all other allowances.

Note 2. A hundred weight, it will be perceived, is 112 lb. Merchants at the present time, in the principal sea ports of the United States, buy and sell by the 100 pounds.

9. A merchant would put 10. In 470 boxes of raisins, 109 cwt. 0 qrs. 12th. of raiscontaining 26th. each, how ins into boxes, containing 26th. each; how many boxes will it require?

11. In 12 tons, 15 cwt. 12. In 7323500 drams, how 1 qr. 19fb. 6 oz. 12 dr. how many tons 3 many drams?

13. In 28th. avoirdupois, 14. In 34th. 0 oz. 6 pwt. how many pounds Troy? 16 grs. Troy, how many pounds avoirdupois?

Cloth sold by English measur the English guarter

1131.

4 pails, 4 quart 3 quart 5 quart

6 quart

how m 18. many Note

> Long things, The de rods, y

> > 3 ba
> > 12 in
> > 3 fee
> > 5½ y
> > 40 ro

8 fu 3 m

360 de

^{* 175} oz Troy 192 oz. avoirdupois, and 175 lb. Trov 144 lb avoirdupois, 1 lb. Troy 5760 grains, and 1 lb. avoirdupois 7000 grains Troy.

grs. to

pirdupois ndard for t, except is used.

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6 pwt. w many

4 lb avoirduis Troy.

CLOTH MEASURE.

Cloth measure is used in selling cloths and other goods, sold by the yard, or ell. It is established by law that the English yard with its parts, &c. shall be the standard for measuring all kinds of cloth or stuffs made of wool flax, &c. the English ell, when there is a special contract for it may be used with its parts. The denominations are ells, yards, quarters, and nails.

TABLE.

4	pails, (na	.)	or 9	ine	ches,	1	make	1	qu	arter,	ma	rk	be	qr.
4	quarters,	or	36	in	ches,	,		1	ya	rd, -		-	-	yd.
3	quarters,		-	-		-	-	1	ell	Flemi	ish,		•	E. Fl.
5	quarters,	-		-	-	_	-	1	ell	Engli	sh,	-		E.E.
6	quarters,	-	-	-	-	-	-	1	ell	Frenc	h,	-	•	E. Fr.

16. In 573 yds. 1 qr. 1 na. 17. In 9173 nails, how how many nails?

18. In 151 ells Eng. how 19. In 1883 yards, how many yards?

Note. Consult 7 28. ex. 16.

LONG MEASURE.

Long measure is used in measuring distances, or other things, where length is considered without regard to breadth. The denominations are degrees, leagues, miles, furlongs, rods, yards, feet, inches, and barley-corns.

TABLE.

3 barley-corns, (bar.) make 1 inch, - marked - i	n.
12 inches, 1 foot,	t.
3 feet, 1 yard, 1	
5½ yards, or 16½ feet, - 1 rod, perch, or pole,	
40 rods, or 220 yards, 1 furlong, 1	ur.
8 furlongs, or 320 rods, - 1 mile, 1	M.
13 miles, harmana a 1 league, a 1	L.
60 geographical, or 69½ } 1 degree, - · · · deg. o	or °
360 degrees,	for-

It is established by law, that the Paris foot with its parts. &c, shall be the standard measure of length, for measuring land, wood, timber, stone, masons', carpenters', and joiners' work. The English foot may be used when there is a special contract for it.

TABLE.

12 lines make 1 inch. 3 toises make 1 rod. 10 rods - - - 1 arpent. 12 inches - · 1 foot. 6 feet - - - 1 toise. 84 arpens - - 1 league.

1 French foot = 1 250 English feet.

20. How many barley-corns 21. In 4755801600 barleywill reach round the globe, it corns, how many degrees ?

being 360 degrees !

Note. To multiply by 2 is Note. The barley-corns beto take the multiplicand 2 ing divided by 3, and that times; to multiply by 1 is to quotient by 12, we have take the multiplicand 1 time; 132106500 feet, which are to to multiply by 1 is to take be reduced to rods. We canthe multiplicand half a time, not easily divide by 161 on that is, the half of it. There account of the fraction 4; but fore, to reduce 360 degrees to 161 feet = 33 half feet, in 1 statute miles, we multiply rod; and 132105600 feet = first by the whole number, 264211200 half feet, which, 69, and to the product additioned by 33, gives 8006400 half the multiplicand. Thus : rods. 1)360 Hence, when the divisor is

> encumbered with a fraction, 1 or 1, &c., we may reduce

> the divisor to halves or fourths

&c., and reduce the dividend

to the same; then the quo-

tient will be the true answer.

23. In 30539520 inches,

694

3240 2160

180 half the multiplicand.

25020 statute miles in 360°.

22. How many inches from Quebec to Three Rivers, sup-how many miles ?

posing it to be 90 miles?

25. If a wheel 16 feet 6 in. 24. How many times will a wheel 16 feet and 6 inches in circumference, turn round in circumference, turn round, 19200 times in going from in the distance from Quebec Quebec to St. Annes, what is to St Annes, supposing it to the distance ? be 60 miles 1

Squar thing, w inations inches.

26. In

pens, ho

many to

¶ 32. it requir a yard i make 3 make 2 feet w will clea

3 feet

144 squa 12 es i 9 squa

in 04 squa 80 40 squ

640

Note. n lengtl nches in 625 squ

its parts, neasuring and jointhere is a

> rod. arpent. league.

0 barleyegrees !

-corns be-

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we have
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ion ½; but
feet, in 1
00 feet =
et, which,
\$8006400

e divisor is a fraction, nay reduce e or fourths e dividend a the quoue answer.

20 inches,

ifeet 6 in. urn round joing from es, what is 26. In 28 leagues, 43 arpens, how many feet? how rods? 1 how many arpens? 27. In 7000 feet how many arpens?

LAND OR SQUARE MEASURE.

Square measure is used in measuring land, and any other thing, where length and breadth are considered. The denominations are miles, acres, roods, perches, yards, feet and inches.

T 32. 3 feet in length make a yard in long measure; but it requires 3 feet in length, and 3 feet in breadth, to make a yard in square measure; 3 feet in length and 1 foot wide, make 3 square feet; 3 feet in length and 2 feet wide, make 2 times 3, that is, 6 square feet; 3 feet in length and 3 feet wide make 3 times 3, that is 9 square feet. This will clearly appear from the annexed figure.

3 feet=1yard.

It is plain, also, that a square foot, that is, a square 12 inches in length, and 12 inches in breadth, must contain 12×12—144 square inches.

TABLE.

	1 ADLE.
	44 square inches=12×12; that is, 12 inches in length and 12 inches in breadth,
	9 square feet=3×3; that is, 3 feet } in length and 3 feet in breadth - 1 square yard.
· 自己	$0\frac{1}{4}$ square yards= $5\frac{1}{4} \times 5\frac{1}{4}$, or $272\frac{1}{4}$ { 1square rod, perch or pole
	4 roods, or 160 square rods, 1 acre.
	Note. Gunter's chain, used in measuring land is 4 rods
	n length. It consists of 100 links, each link being 7.20 nches in length; 25 links make 1 rod, long measure, and
	625 square links make 1 square rod.

many acres?

FRENCH SQUARE MEASURE.

144 square inches make 1 square foot.

36 - feet - - 1 toise.

9 - toises - - 1 rod.

100 - rods - - 1 arpent.

7056 - arpens - 1 league.
62500 french feet = 71289 English feet.

Reduce 16 leagues to feet, — to toises, — to rods.

Reduce 98764321 feet to toises, — to rods, — to arpens, — to leagues.

28. In 17 acres 3 roods 12 29. In 776457 square feet,

sods, how many square feet ! how many acres !

Note. In reducing rods to Note. Here we have 776457 feet, the multiplier will be square feet to be divided by 2724. To multiply by 4, is to 2724. Reduce the divisor take a fourth part of the multiplicand. The principle is est denomination contained in the same as shown \$\quad 28\$, it; then reduce the dividend to fourths, that is, to the same denomination, as shown \$\quad 31\$, ex. 21.

30. Reduce 64 square miles 31. In 1,784,217,600 sq. to square feet. ? feet, how many square miles?

32. There is a town 6 miles 33. Reduce 23040 acres to square; how many square square miles. miles in that town? how

SOLID OR CUBIC MEASURE.

Solid or cubic measure is used in measuring things that have length, breadth, and thickness; such as timber, wood stone, bales of goods, &c. The denominations are cords tons, yards, feet, and inches.

¶ 33. It has been shown, that a square yard contains 3×3 = 9 square feet. A cubic yard is 3 feet long, 3 feet wide, and 3 feet thick. Were it 3 feet long, 3 feet wide and one foot thick, it would contain 9 cubic feet; if 2 feet thick, it would contain 2×9 = 18 cubic feet; and, as it is

1728

3 feet

1728 s tha 12

> 27 so 40 fe

128 s is width,

Note.
16 solid
foot i
cord.

32. I

34. low mag 36.

38. how m many s

40.

3 feet thick, it does contain 3×9=27 cubic feet. This will clearly appear from the an-1 yd=3A long nexed figure.

It is plain, also, that a cubic foot, that is, a solid 12 inches in length, 12 inches in breadth, and 12 inches in thickness, will contain $12 \times 12 \times 12 = 1728$ solid or cubic inches.

TABLE.

1728 solid inches,= $12\times12\times12$, make 1 solid foot. that is, 12 inches in length, 12 in breadth, 12 in thickness,

27 solid feet,= $3\times3\times3$ 1 solid yard.

40 feet of round timber, or 50 ? I ton or load. feet of hewn timber,

128 solid feet,= $8\times4\times4$, that is 8 feet in length, 4 feet in 1 cord of wood. width, and 4 feet in height,

Note. What is called a cord foot, in measuring wood, is 6 solid feet; that is, 4 feet in length, 4 feet in width, and foot in height, and 8 such feet, that is, 8 cord feet make cord.

FRENCH SOLID MEASURE.

17 olid inches make I solid foot. 216 - 1 toise. - - feet

1000 French feet = 1218 186432 English feet.

imber to cubic inches.

34. In 37 cord feet of wood,

ow many solid feet?

wood to cords. 38. In 16 cords of wood, many solid feet ?

40. In 12 toises how many nches !

G

32. Reduce 9 tons of round 33. In 622080 cubic inches how many tons of round timber 1

> 35. In 592 solid feet of wood, how many cord feet ?

36. Reduce 64 cord feet of 37. In 8 cords of wood, how many cord feet ?

39. In 2048 solid feet of how many cord feet? how wood, how many cord feet; how many cords ?

> 41. In 834692773 inches how many feet ! how many toises 1

o rods. - to ar-

quare feet.

ave 776457 divided by he divisor to the lowcontained in e dividend to the same hown ¶ 31.

17,600 sq. uare miles! 40 acres to

things that aher, wood. are cords.

rd contains ong, 3 feet 3 feet wide t; if 2 feet nd, as it is

WINE MEASURE.

It is established by law that the wine gallon with its parts, &c. shall be the standard liquid measure, for measuring wine, eider, beer, and all other liquids commonly sold by gauge, or measure of capacity. The denominations are tuns, pipes, hogsheads, barrels, gallons, quarts, pints, and gills.

TABLE.

			_						
4	gills (gi.)	- 1	make	-	- 1	pint,	mark	ed	pt.
24	pints -	-			- 1	quart,	-	-	qt.
4	quarts	·		7	1	gallon			gal.
314	gallons		~		1	barret,		-	bar.
63	gallons				1	hogsho	ead,	-	hhd.
2	hogsheads	-	•	-	1	pipe,	60	*	P .
2	pipes, or f	our l	iogshe	ads	1	tun,	~	-	T.
1	Vote. A gal	lon,	wine n	ieasu	re, c	ontains	231 с	ubic	inches.
4	2. Reduce	12 pi	pes of v	vine	43	. In 12	096 pi	nts o	f wine,
	pints.	•				many			
4	4. In 9 P.	1 hb	d. 22	gals.	45	. Redu	ce 39	032	gills to
	ts. how ma				pipes	1			
	6. In a tu			how	47	. Redu	ce 250	l gal	lons to
	ny gations				tuns.				

ALE OR BEER MEASURE.

Ale or beer measure is used in measuring ale, beer, and milk. The denominations are hogsheads, barrels, gallons, quarts, and pints.

TABLE.

2	pints (pt	5.)	ma	ike	1	quart,	mar	ked	qt.
4	quarts		•	-	1	gallon,		-	gal.
36	gallons	•		4	1	barrel,	•	+	bar.
54	gallons	-			1	hogshead,	-		bhd.

Note. A gallon, beer measure, contains 282 cubic inches.

48 Reduce 47 bar. 18 gal	49. In 13680 pints of ale,
of ale to pints?	how many barrels?
50. In 29 hbds. of beer	how many barrels? 51. Reduce 12528 pints to
how many nints t	horsheads 1

Dry grain,

chaldr

2 pir 8 qua 4 pe 36 bu *Not*

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parts,
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20

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Th for th

to be 52 how 54

coal

T day:

60 60 with its measurnly sold tions are ints, and

> pt. qt. gal. bar. hhd. P.

> > T.

ic inches. is of wine,

32 gills to gallons to

beer, and s, gallons,

d qt.
- gal.
- bar.
- bhd.

ints of ale,

28 pints to

DRY MEASURE.

Dry measure is used in measuring all dry goods, such as grain, fruit, roots, salt, coal, &c. The denominations are chaldrons, bushels, pecks, quarts, and pints.

TABLE.

2	pints (pt	S. \		ma	ke	-	1	quart,	_	ma	rk	ed	-	qt.
	quarts,	-						peck,	_ 1		-			pk,
4	pecks				-	-	1	bushel,	-	-	•	*		bu.
36	bushels	-	-	-		-	1	chaldron,	_		-	(i) an	-	ch.

Note. A gallon dry measure, contains 2684 cubic inches. A Winchester bushel is 184 inches in diameter, 8 inches

deep, and contains 2150% cubic inches:

It is established by law, that the Cana a Minot, with its parts, multiples, and proportions, shall be the standard in Dry Measure.

1 pot = 116.94589 English cubic feet.

20 pots make 1 minot.

OLD MEASURE.

16	litrons	4	ma	ke	100	1		+4-	, .	i.	boisseau.
8	boisseaux	ĸ	-	4,=	-	1		700		-	minot.
2	minots	-	100	-	-	1		69		-	mine.
2	mines	1		₹ ,₩	10	1.		40			setier.
12	setiers	70	-	() · · ·	- 1	1	2 3	-			muid.
	40 1	Fre	enc	h en	bic	incl	het	-	1	litro	0.

The standard measure for the sale and purchase of coal, for this Province, is the chaldron of 36 minots, each minot to be heaped up.

52. In 75 bushels of wheat 53. In 4800 pints, how ma-

54. Reduce 42 chaldrons of 55. In 6048 pecks, how coal to pecks.

TIME.

The denominations of time are years, months, weeks, days, hours, minutes, and seconds.

TABLE.

60 seconds 60 minutes	(q.)	•	make		1	minute,	MAT	ked m.
60 minutes	-			100	1	hour, -		h.

7 days 1 week, 1 month,	yr.
7 days 1 week,	mo.

¶ 84. The year is also divided into 12 calendar months, which in the order of their succession are numbered as follows, viz.

January, 1st month, has 31 days.

2d,	*	-	-	28
3d, #	-	-	-	31
4th,	-		-	30
5th.	-	-	-	31
6th,	-	-	-	30
7th,	_	-	-	31
8th,	-	-		:31
9th,	-		-	30
10th,		-	-	31
11th,		_	-	30
	3d, 4th, 5th, 6th, 7th, 8th, 9th, 10th,	3d, - 4th, - 5th, - 6th, - 7th, - 8th, - 9th, - 10th,	3d, 4th, 5th, 5th, 9th, 10th,	3d,

12th.

December,

Note. When any year can be divided by 4 without a remainder, it is called leap year, in which February has 29 days.

The number of days in each month may be easily fixed in the mind by committing to memory the following lines:

Thirty days hath September, April, June and November, February twenty-eight alone; All the rest have thirty-one.

The first seven letters in the alphabet, A, B, C, D, E, F, G, are used to mark the several days of the week, and they are disposed in such a manner, for every year, that the letter A shall stand for the 1st day of January, B for the 2d, &c. In pursuance of this order, the letter which shall stand for Sunday, in any year, is called the Dominical letter for that year. The Dominical letter being known, the day of the week on which each month comes in may be readily calculated from the following couplet:

At Dover Dwells George Brown, Esquire, Good Carlos Finch And David Fryer.

These words correspond to the 12 months of the year, and the first letter in each word marks the day of the week on

to fin year answ when No

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one for the 5

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hours
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Cir tude ; other cles, s

60 sec 60 mi 30 de 12 sig

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T 34.

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mo. yr.

ar months. red as fol-

any year by 4 withr. it is callin which 29 days.

sily fixed ing lines :

E. F. G. they are e letter A 1, &c. In for Sunthat year. the week calculated

rear, and week on

which each corresponding month comes in; whence any other day may be easily found. For example, let it be required to find on what day of the week the 4th of July falls, in the year 1827, the Dominical letter for which year is G. Good answers to July; consequently, July comes in on a Sunday; wherefore the 4th of July falls on Wednesday.

Note. There are two Dominical letters in leap years. one for January and February, and another for the rest of

the year.

56. Supposing your age to 57. Reduce 475047465 sebe 15v. 19d. 11h. 37m. 45s., conds to years. how many seconds old are you, allowing 365 days 6 hours to the year !

58. How many minutes from 59. Reduce 325440 minutes the 1st day of January to the to days.

14th day of August, inclu-

sively?

60. How many minutes from the commencement of the war between America and Eng-how many years? land, April 19th, 1775, to the settlement of a general peace, which took place Jan. 20th, 1783 ?

61. In 4079160 minutes.

CIRCULAR MEASURE, OR MOTION.

Circular measure is used in reckoning latitude and longtude: also in computing the revolution of the earth and other planets round the sun. The denominations are car cles, signs, degrees, minutes, and seconds.

TABLE.

60 seconds (")) ma	ke	1 minute,	marked	,
60 minutes	-	-	1 degree,	- To	
30 degrees		-	I sign,		8
12 signs, or 3	60 degree	es,	1 circle of th	e zodiac.	

Note. Every circle, whether great or small, is divisible into 360 equal parts, called degrees.

62. Reduce 9s. 13° 25' to 63. In 1020300" hew many seconds. degrees ?

G 2

The following are denominations of things not included in the tables :-

12 particular things make 1 dozen.

12 dozen - - 1 gross.

12 gross, or 144 dozen, - 1 great gross.

Also,

20 particular things make 1 score.

6 points make 1 line, { used in measuring the length of 12 lines - 1 inch, the rods of clock pendulums.

4 inches - 1 hand, { used in measuring the height of horses.

6 feet - 1 fathom, used in measuring depths at sea.

112 pounds - make - 1 quintal of fish.

24 sheets of paper make 1 quire.
20 quires - 1 ream.

SUPPLEMENT TO REDUCTION.

QUESTIONS.

1. What is reduction? 2 Of how many varieties is reduction? 3 What is understood by different denominations, as of money, weight. measure, &c.? 4. How are high denominations brought into lower? 5. How are low denominations brought into higher? 6. What are the denominations of Halifax currency? 7. What name is given to the currency of this Province? 8. And why? 9. Are the ratios of the different denominations to each other the same as in English money? 10. Will the rule for reduction of one denomination to another in Halifax currency, apply to all currencies in which the denominations are of the same name? 11. What is the use of Troy weight and what are the denominations? 12. — avoirdupoise weight? the denominations? 13. What distinction do you make between gross and net weight? 14. What distinctions do you make between long, square, and cubic measure? 15. What are the denominations in long measure? 16. — in square measure? 17. — in cubic measure? 18. How do you multiply by 1? 19. When the divisor contains a fraction, how do you proceed? 20. How is the superficial contents of a square figure found? 21. How is the solid contents of any body found in cubic measure? 22. How many soud or cubic feet of wood make a cord? 23. What is understood by a cord foot? 24. How many such feet make a cord ? 25. What are the denominations of dry measure? 26. -of wine measure? 27. - of time? 28 of circular measure? 29. For what is circular measure used? 30. How many rods in length is Gunter's chain? of how many links does it consist? how many links make a rod? 31. How many rods in a mile? 32. How many square rods in an acre? 33. How many pounds make I cwt.?

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EXERCISES.

In 154 dollars, at 5s. each, how many pounds, &c.
 Ans. 38£. 10s.

2. In 36 guineas, at 1£ 3s. 4d. each, how many crowns, at 5s. 6d. t

Ans. 131 crowns and 2s. 10d. over.

3. How many rings, each weighing 5pwt. 7grs., may be made of 3lb. 5oz. 16pwt. 2grs. of gold?

Ans. 158.

4. Suppose a bridge to be 212 rods in length, how many times will a chaise wheel, 18 feet 6 inches in circumference, turn round in passing over it?

Ans. 189 18 242 times.

5. In 470 boxes sugar, each 26lb., how many cwt. 1

6. In 10lb. of silver, how many spoons, each weighing toz. 10pwt. 1

7. How many shingles, each covering a space 4 inches one way and 6 inches the other, would it take to cover 1 square foot? How many to cover a roof 40 feet long, and 24 wide? (See § 25.)

Ans. to the last, 5760 shingles.

8. How many cords of wood in a pile 26 feet long 4 feet wide, and 6 feet high?

Ans. 4 cords, and 7 cord feet.

9. There is a room 18 feet in length, 16 feet in width, and 8 feet in height; how many rolls of paper, 2 feet wide, and containing 11 yards in each roll, will it take to cover the walls 1

Ans. $8\frac{1}{16}$

10. How many cord feet in a load of wood $6\frac{1}{4}$ feet long. 2 feet wide, and 5 feet high?

Ans. $4\frac{1}{16}$ cord feet.

11. If a ship sail 7 miles an hour, how far will she sail, at that rate, in 3w. 4d. 16h?

12. A merchant sold 12 hhds. of brandy, at \$3 a gallon; how much did each hogshead come to, and to how much in currency did the whole amount?

13. How much cloth, at 7s. a yard, may be bought for 29£ 1s?

14. A goldsmith sold a tankard for 10£8s. at the rate of 5s. 4d. per ounce; how much did it weigh?

15. An ingot of gold weighs 2lb. 8oz. 16pwt; how much is it worth at 3d. per pwt?

16. At 11 pence a pound, what will 1 T. 2cwt. 3qrs. 16lb. of lead come to?

17. Reduce 14445 ells Flemish to ells English.

18. There is a house, the roof of which is 44½ feet in length, and 20 feet in width, on each of the two sides; if 3 shingles in width cover one foot in length, how many

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ney, weight. t into lower? 6. What are is given to the ratios of English moon to another ie denomina-Proy weight. pise weight? ake between ake between enomination& - in cubic the divisor he superficial d contents of or cubic feet d foot ? 24. enominations of time? 28 casure used; many links w many rods . How many

shingles will it take to lay one course on this roof? if 3 courses make one foot, how many courses will there be on one side of the roof? how many shingles will it take to cover one side? —— to cover both sides?

Ans. 16020 shingles.

19. How many steps, of 30 inches each, must a man take in travelling 541 miles?

20. How many seconds of time would a person redeem in 40 years, by rising each morning \(\frac{1}{2} \) hour earlier than he now does?

21. If a man lay up ½ dollar each day, Sundays excepted, how many pounds would he lay up in 45 years?

22. If 9 candles are made from 1 pound of tallow, how many dozen can be made from 24 pounds and 10 ounces?

23. If one pound of wool make 60 knots of yarn, how many skeins, of ten knots each, may be spun from 4 pounds 6 ounces of wool?

ADDUTION .

OF COMPOUND NUMBERS.

T 35. 1. A boy bought a knife for 9 pence, and a comb for 3 pence; how much did he give for both? Ans. 1 shilling.

2. A boy gave 2s. 6d. for a slate, and 4s. 6d. for a book;

how much did he give for both?

3. Bought one book for 1 s. 6 d., another for 2 s. 3 d., another for 7 d.; how much did they all cost?

Ans. 4 s. 4 d.

4. How many gallons are 2 qts. +3 qts. +1 qt. !

5. How many gallons are 3 qts. +2 qts. +1 qt. +3 qts. +2qts. ?

6. How many shillings are 2d. + 3d. + 5d. + 6d. + 7d.

7. How many pence are 1qr. + 2qrs. + 3qrs, + 2qrs. + 1qr.?

8. How many pounds are 4s. + 10s. + 15s. + 1s.

9. How many minutes are 30 sec. + 45sec. + 20sec. ?

10. How many hours are 40 min. + 25 min. + 6min. ?

11. How many days are 4h. +8h. +10h. +20h. ?

12. How many yards in length are 1f. +2f. + 1f.?

¶ 35.

13. 1in. 1

14. 1 ft. 8

15. 16. wine;

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Next, the 1s. $v = 1\pounds$. the $1\pounds$. be $41\pounds$.

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s. 3 d., ans. 4 s. 4 d. qt. ?

1 qt. +3

6d. + 7d. ! 6, + 2qrs.

- 1s. ! 20sec. ! - 6min. ! 20h. !

- 1f. 1

13. How many feet are 4in. + 8in. + 10in. + 2in. + 1in. 1

14. How much is the amount of 1yd. 2ft. 6in. + 2yds.

l ft. 8 in. 1

1 35.

15. What is the amount of 2s. 6d. +4s. 3d. +7s. 8d.?

16. A man has 2 bottles, which he wishes to fill with wine; one will contain 2 gal. 3 qts. 1 pt. and the other 3 qts.; how much wine can be put in them?

17. A man bought a horse for 15£. 14s. 6d., a pair of oxen for 20£. 2s. 8d., and a cow for 5£. 6s. 4d.; what did

he pay for all ?

When the numbers are large, it will be most convenient to write them down, placing those of the same kind, or denomination, directly under each other, and, beginning with those of the least value, to add up each kind separately.

OPERATION.

£. d. In this example, adding up the 15 14 6 column of pence, we find the amount 20 2 8 to be 18 pence, which being = 1s. 6 4 6d., it is plain that we may write down the 6d. under the column of 3 Ans. 41 pence, and reserve the 1s. to be added in with the other shillings.

Next, adding up the column of shillings, together with the 1s. which we reserved, we find the amount to be 23s. $=1\pounds$. 3s. Setting the 3s. under its own column, we add the $1\pounds$. with the other pounds, and, finding the amount to be $41\pounds$. we write it down, and the work is done.

Ans. 41£. 3s. 6d.

Note. It will be recollected, that, to reduce a lower into higher denomination, we divide by the number which it takes of the lower to make one of the higher denomination. In addition, this is usually called carrying for that number thus, between pence and shillings, we carry for 12, and between shillings and pounds, for 20, &c.

The above process may be given in the form of a general Rule for the Addition of Compound Numbers.

I. Write the numbers to be added so that those of the same denomination may stand directly under each other.

II. Add together the numbers in the column of the lowest denomination, and carry for that number which it takes of

the same to make 1 of the next higher denomination. Proceed in this manner with all the denominations, till you come to the last, whose amount is written as in simple num-

Proof. The same as in addition of simple numbers.

EXAMPLES FOR PRACTICE.

HALIFAX CURRENCY.

£ 46 16	8. 11 7	d. 3	qr. 2		72	s. d. 9 6 <u>1</u> 0 10 <u>1</u>		€ 83	8. 19	d.
538	19	7	2 4 1		18 36 1	6 53	_	8	17 15	10
£.	8.	d.	_	£.	s.	d.	£.	s.		d .
£. 14 8 62 4 23 6	0 15	71 3 7 8 4		37	15	8 93	61	3 16	5	d. 2 <u>1</u> 8 0 <u>1</u> 2 5 1 0
8	15	3		14 17	12	93	7	16	- 1	3
62	4	7		17	12 14	9	29	13	10	01
4	17	8		23	10	94	12	16		2
23		4	4	8	6	0	0	7		54
6	6	7	•	14	0	51	24	13	4	0~
91	6	10	1	23 8 14 54	0 2	0 5 <u>1</u> 7]	0 24 5	0	1	03

No examples in Federal Money are here introduced, al though the general rule for the addition of all compound numbers is precisely applicable to the addition of Federa. Money, since that consists of different denominations. In Federal Money the denominations increase and decrease in a decimal ratio. The pupil is therefore referred to the rules for the Addition, Subtraction, Multiplication and Division of Decimals, which are the same absolutely with the rules for the addition, subtraction, multiplication and division of Fed eral money.

TROY WEIGHT.

lb. 36	oz. 7	prot. 10	gr. 11	6z.	puot.	gr. 9	oz.	prot.	18
		9		. 8	6	16		13	16
81	7	16	15	3	11	10	3	. 7	. 4

Boug cup, we 2 pwt.

> T. 14 25

A ma 23 cwt. 19 cwt. how ma

> yds. g 36 41 65

Ther viz. 36 3 na.;

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oduced, al compound of Federa actions. In decrease in to the rules Division of the rules for

sion of Fed

Bought a silver tankard, weighing 2lb. 3 oz., a silver cup, weighing 3 oz. 10 pwt. and a silver thimble, weighing 2 pwt. 13 grs.; what was the weight of the whole 3

AVOIRDUPOIS WEIGHT.

				oz. 5 8				oz. 6 8	
7	18	0	25	11	9		22	11	10
						 			-

A man bought 5 loads of hay, weighing as follows, viz. 23 cwt. (=1 T. 3 cwt.) 2 qrs. 17 lb.; 21 cwt. 1 qr. 16 lb; 19 cwt. 0 qr. 24 lb.; 24 cwt. 3 qrs.; 11 cwt. 0 qr. 1 lb.; how many tons in the whole?

CLOTH MEASURE.

yds. 36	qr.	n. 2	E. Fl. 41	qr.	na.	E. E. 4	7. 4	na.
41	-		18	_		31		
65	3	1	57	0	2	28	3	1

There are four pieces of cloth, which measure as follows, viz. 36 yds. 2 qrs. 1 na.; 18 yds. 1 qr. 2 na.; 46 yds. 3 qrs. 3 na.; 12 yds. 0 qr. 2 na.; how many yards in the whole?

LONG MEASURE.

	Deg. 59							Mi.	fur.	pol.
	216	39	1	36	14	6	1			
	678	53	7	24	9	8	1	8	6	27
-					-		-	-		

LAND OR SQUARE MEASURE.

Pol.	ft.	in.	A.	rood	. pol.	ft.	278.
36	ft. 179	137	56	3	37	ft. 245	228
19	248	119				93	
12	96	75	416	2	31	128	119

There are 3 fields, which measure as follows, viz. 17 A. 3r. 16 p.: 28 A. 5r. 18p.; 11A. 0r. 25p.; how much land in the three fields?

SOLID OR CUBIC MEASURE.

		in. 1229			in. 1412		
12	19	64	9	26	195	4	110
8	11	917	3	19	1091	48	127
-	-						

WINE MEASURE.

	53 39 13	3	0	19	2 1	gal. 37 50 0	2
C)			-				

A merchant bought two casks of brandy, containing as follows, viz. 70 gal. 3 qts.; 67 gal. 1qt.; how many hogsheads, of 63 gal. each, in the whole?

DRY MEASURE.

Bus. 36	$\frac{p}{2}$	qt.	<i>pt.</i> 1	Ch. 48	bus. 27	p . 3	9t. 5
19					29		
				-			_

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	γ. •57	mo.	w. 3	d. 6	23	$\frac{m}{55}$	s. 11	Y. 40	$\frac{m}{3}$		
					16			16	7	0	4
8	32	6	0	5	5	18	5	27	5	2	0
			4								

SUBTRA OTTOM

OF COMPOUND NUMBERS.

¶ 36. 1. A boy bought a knife for 9 pence, and sold it for 1s. 4d.; how much did he gain by the bargain?

2. A boy bought a slate for 2s. 6d., and a book for 3s. 6d.; how much more was the cost of the book than of the slate?

3. A boy owed his playmate 2s.; he paid him 1s. 64.; how much did he then owe him?

4. Bought two books; the price of one was 4s. 6d., the price of the other 3s. 9d.; what was the difference of their costs?

5. A boy lent 5s. 3d.; he received in payment 2s. 6d.; how much was then due?

6. A man has a bottle of wine containing 2 gallons and 3 quarts; after turning out 3 quarts, how much remained?

7. How much is 4 gal. less 3 gal? 4 gal. — (less) 2qts? 4 gal. — 1qt? 4 gal. — 1 gal. 2qts? 4 gal. — 1 gal. 3qts? 4 gal. — 2 gal. 3qts? 4 gal. 1qt. — 1 gal. 3qts.?

8. How much is 1ft. — (less) 6in? 1ft. — Sin? 6ft. 3 inches, — 1ft. 6in? 7ft. Sin. — 4ft. 2in? 7ft. Sin. — 50. 10in?

9. What is the difference between 4£ 6s. and 1£ 8s?

10. How much is $3\pounds - (less)$ 1s? $3\pounds - 2s$? $3\pounds - 3s$. $3\pounds - 15s$? $3\pounds$ 4s. $-2\pounds$ 6s? $10\pounds$ 4s. $-5\pounds$ 8s?

11. A man bought a horse for 30£ 4s. 8d., and a cow for 5£ 14s. 6d.; what is the difference of their costs?

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taining as any hogs OPERATION. £. s. d.

Minuend, 30 4 8 Subtrahend, 5 14 6

Ans. 24 10

As the two numbers are large, it will be convenient to write them down, the less under the greater, pence under pence, shillings under shillings, &c. We may now take 6d. from 8d., and

there will remain 2d. Proceeding to the shillings, we cannot take 14s. from 4s., but we may borrow, as in simple numbers, 1 from the pounds,=20s., which joined to the 4s. makes 24s, from which taking 14s. leaves 10s, which we set down. We must now carry 1 to the $5\mathcal{L}$ making $6\mathcal{L}$ which taken from $30\mathcal{L}$ leaves $24\mathcal{L}$ and the work is done.

Note. The most convenient way in borrowing is, to subtract the subtrahend from the figure borrowed, and add the difference to the minuend. Thus, in the above example, 14

from 20 leaves 6, and 4 is 10.

The process in the foregoing example may be presented in the form of a Rule for the Subtraction of Compound Num-

1. Write down the sums or quantities, the less under the greater, placing those numbers which are of the same denom-

mation directly under each other.

II. Begining with the least denomination, take successively the lower number in each denomination from the upper, and write the remainder underneath, as in subtraction of simple numbers.

III. If the lower number of any denomination be greater than the upper, borrow as many units as make one of the next higher denomination, subtract the lower number therefrom, and to the remainder add the upper number, remembering always to add 1 to the next higher denomination for that which you borrowed.

Proof. Add the remainder and the subtrahend together, as in subtraction of simple numbers; if the work be right,

the amount will be equal to the minuend.

EXAMPLES FOR PRACTICE.

HALIFAX CURRENCY.

t.	3.	d.	1	1 .	£.	18.	·'d.
79.	17	8		()	103	-3	2
35	12	4	1.1.	1.0	71.	19	15

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3. A 19£ 12s

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 520	11	3	631	14	7
109		4	·· 6	19	8

MISCELLANEOUS EXAMPLES.

1. A merchant sold goods to the amount of 136£ 7s. 6½d and received in payment 50£ 10s. 4½d; how much remained due?

Ans. 85£ 17s. 1½d.

2. A man bought a farm for 1256£ 10s, and, in selling it, lost 87£ 10s. 6d; how much did he sell it for?

Ans. 1168£ 19s. 6d

3. A man bought a horse for 27£ and a pair of oxen for 19£ 12s. 8½d; how much was the horse valued more than the oxen?

4. A merchant drew from a hogshead of molasses, at one time, 13gal. 3qts; at another time, 5gal. 2qts. 1pt; what quantity was there left?

Ans. 43gal. 2qts. 1pt

5. A pipe of brandy, containing 118gal. sprang a leak, when it was found only 97gal. 3qts. 1pt. remained in the

eask; how much was the leakage?

6. There was a silver tankard which weighed 3lb. 4oz; the lid alone weighed 5oz. 7pwt. 13grs; how much did the he tankard weigh without the lid?

7. From 15lb. 2oz. 5pwt. take 9oz. 8pwt. 10grs.

8. Bought a hogshead of sugar, weighing 9cwt. 2qrs. 17lb; sold at three several times as follows, viz. 2cwt. 1qr. 11b. 5oz; 2qrs. 18lb. 10oz; 25lb. 6oz; what was the reight of sugar which remained unsold?

Ans. 6cwt. 1qr. 17lb. 11oz.

9. Bought a piece of black broadcloth, containing 36 yds. 2qrs; two pieces of blue, one containing 10 yds. 3qrs. 2na, he other, 18yds. 3qrs. 3na; how much more was there of he black than of the blue?

10. From 28 miles, 5 fur. 16r. take 15 m. 6 fur. 26 r. 12ft.

11. A farmer has two mowing fields; one containing 13

acres 6 roods; the other, 14 acres 3 roods: he has two pastures also; one containing 26 A. 2 r. 27p; the other, 45 A. 5 r. 33 p: how much more has he of pasture than of mowing !

12. From 64A, 2r. 11p. 29ft, take 26A, 5r. 34p. 132ft.

13. From a pile of wood, containing 21 cords, was sold, at one time, 8 cords 76 cubic feet; at another time, 5 cords 7 cord feet; what was the quantity of wood left?

14. How many days, hours and minutes of any year will be future time on the 4th day of July, 20 minutes past 3 o'clock, P. M?

Ans. 180 days, 8 hours, 40 minutes.

15. On the same day, hour and minute of July, given in the above example, what will be the difference between the past and future time of that month?

16. A note, bearing date Dec. 28th, 1826, was paid Jan.

2d, 1827; how long was it at interest?

The distance of time from one date to that of another may be found by subtracting the first date from the last, observing to number the months according to their order. (¶ 34.)

17. A note, bearing date Oct. 20th, 1823, was paid April 25th, 1825; how long was the note at interest?

18. What is the difference of time from Sept. 29, 1816 to April 2d, 1819?

Ans. 2v. 6m. 3d.

19. London is 51° 32′, and Montreal 45° 30′, N. latitude; what is the difference of latitude between the two places?

Ans. 6° 2′

20. Montreal is 73° 20′, and the city of Washington is 77° 43′ W. longitude; what is the difference of longitude between the two places?

Ans. 4° 23

21. The island of Cuba lies between 74° and 85° W. longitude; how many degrees in longitude does it extend

¶ 37. 1. When it is 12 o'clock at the most easterly extremity of the island of Cuba, what will be the hour at the most westerly extremity, the difference in longitude being 11°?

Note. The circumference of the earth being 360°, and the earth performing one entire revolution in 24 hours, it

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t. 29, 1816. 2y. 6m. 3d. 30', N. latieen the two Ans. 6° 2. (ashington is of longitude Ans. 4° 23.

and 85° W.
es it extend?
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longitude be

g 360°, and 24 hours, it follows, that the motion of the earth, on its surface. from west to east, is

150 of motion in 1 hour of time; consequently.

10 of motion in 4 minutes of time, and

I' of motion in 4 seconds of time.

From these premises it follows, that, when there is a difference in longitude between two places, there will be a corresponding difference in the hour, or time of the day. The difference in longitude being 15°, the difference in time will be one hour, the place easterly having the time of the day I hour earlier than the place westerly, which must is particularly regarded.

If the difference in longitude be 1°, the difference in tune

will be 4 minutes, &c.

Hence,—If the difference in longitude, in degrees and minutes, between two places, be multiplied by 4, the product will be the difference in time, in minutes and seconds which may be reduced to hours.

We are now prepared to answer the above question.

Hence, when it is 12 o'clock at the most easterly extremity of the island. it will be 16 minutes past 11 o'clock at the most western extremity.

2. Montreal being 73° 20′ W. longitude and Washington. 77° 43′; when it is 3 o'clock at the city of Washington what is the hour at Montreal?

Ans. 17 minutes 32 seconds past 3 o'cleck

3. Lower Canada being about 73°, and the Sandwick Islands about 155° W. longitude, when it is 28 minutes past 6 o'clock, A. M. at the Sandwich Islands, what will be the hour in Lower Canada?

Ans. 12 o'clock at noon, lacking 4 minutes

AUCHTIPAIGATION & DIC PIOURION

OF COMPOUND NUMBERS.

¶ 38. 1. A man bought 2 yards of cloth, at 1s. 6d. per yard; what was the cost?

2. If 2 yards of cloth cost 3 shillings, what is that per yard?

3. A man has three pieces of cloth, each measuring 10 yds. 3qrs; how many yards in whole ?

4. If 3 equal pieces of cloth contain 32 yds. 1 qr., how much does each piece contain ?

5. A man has five bottles, each containing 2 gal. 1 qt. 1 pt; how much wine do they all contain?

6. A man has 11gal. 3qts. 1pt. of wine, which he would divide equally into 5 bottles; how much must he put into each bottle?

7. How many shillings are 3 times 8d? $-3\times9d$? $-3\times10d$? $-4\times7d$? $-7\times6d$? $-10\times9d$? $-2\times3qrs$? $-5\times2qrs$?

8. How much is one third of 2 shillings? $-\frac{1}{3}$ of 2s. 3d? $-\frac{1}{3}$ of 2s. 6d? $-\frac{1}{3}$ of 2s. 6d? $-\frac{1}{10}$ of 7s. 6d? $-\frac{1}{4}$ of $\frac{1}{2}$ d? $-\frac{1}{4}$ of $\frac{2}{3}$ d?

9. At 1£5s. S₂³d. per yard, 10. If 6 yards of cloth cost what will 6 yards of cloth 7£ 14s. 4½d, what is the cost?

Here, as the numbers are large, it will be most convenient to was a them down before multiplying and dividing.

OPERATION. OPERATION.

£ s. d. qr.

1 5 8 3 price of 1 yard. 6)7 14 4 2 cost of 6 yards.

Ans. 7 14 4 2 cost of 6 yards.

Proceeding after the man-

6 times 3qrs. are 18qrs. — ner of short division, 6 is con4d. and 2qrs. over; we set tained in 7£ 1 time, and 1£down the 2qrs; then, 6 times over; we write down the
3d. are 48d, and 4 to carry quotient, and reduce the remakes 52d. — 4s. and 4d. mainder (1£) to shillings,
over, which we write down; (20s,) which, with the given
again, 6 times 5s. are 30s. shillings, (14s,) make 34s;
and 4 to carry makes 34s — 6 in 34s. goes 5 times, and 1£ and 14s. over; 6 times 4s. over; 4s. reduced to pence 1£ are 6£, and 1 to carry — 48d, which, with the giv-

makes 7£, which we write en pence, (4d,) make 52d; 6 down, and it is plain, that in 52d, goes 8 times, and 4d.

the united products arising over; 4d. = 16qrs, which,

from tions ing from number

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of 5 p
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15.

each of qts,

cloth coats, 3 na.

each egills,

21 weigh weigh

hogsh 9cwt.

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ne would put into

 $3 \times 9d$? 9d?

of 2s. 3d?

cloth cost t is the

nvenient ng.

6 yards. f 1 yard.

the man-

, 6 is cone, and $1\pounds$ down the ce the reshillings, the given ake 34s; times, and ed to pence th the givke 52d; 6 es, and 4d.

rs, which,

tions is the real product aris-qrs; 6 in 18qrs. goes 3 times; ing from the whole compound and it is plain, that the unitnumber.

11. Multiply 3£ 4s. 6d.

13. What will be the cost of 5 pairs of shoes at 10s. 6d. pairs of si a pair?

15. In 5 barrels of wheat, 6 qts, how many bushels?

17. How many yards of coats, allowing 4 yds. 1qr. coat contain? 3 na. to each?

19. In 7 bottles of wine, gills, how many gallons?

21. What will be the 22. If 8 silver cups weigh weighing 5oz. 12pwt. 17grs? is the weight of each?

9cwt. 3qrs. 21lb ?

how many tons?

from the several denomina-with the given qrs. (2) = 18ed quotients arising from the several denominations, is the real quotient arising from the whole compound number.

12. Div; 2£ 11s. 6d by 7.

14. A. for 5 is that a pair 1

16. If 14bus. 2pks. 6qts. of each containing 2 bus. 3 pks. wheat be equally divided into 5 barrels, how many bushels will each contain?

18. If 9 coats contain 39 cloth will be required for 9 yds. 3grs. 3na, what does 1

20. If 5 gal. I gill of wine each containing 2qts. 1pt. 3 be divided equally into 7 bottles, how much will each contain?

weight of 8 silver cups, each 3lb. 9oz. 1pwt. 16grs, what 24. If 119cwt. 1qr. of su-

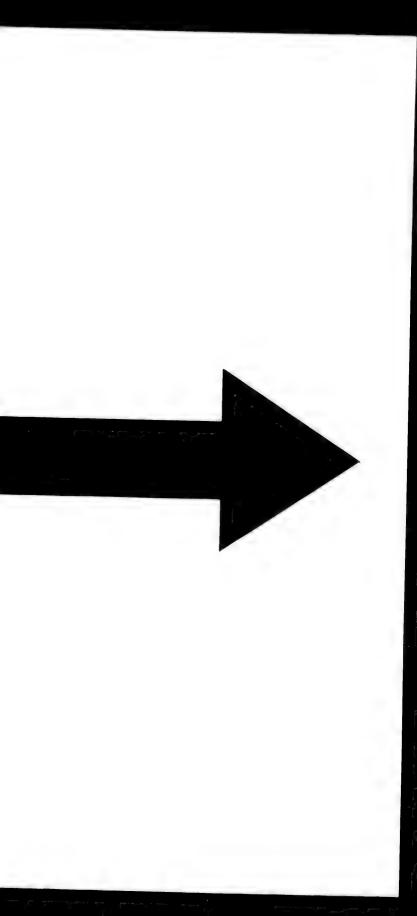
23. How much sugar in 12 gar be divided into 12 hogshogsheads, each containing heads, how much will each hogshead contain?

25. In 15 loads of hay, each 26. If 15 teams be loaded weighing 1T. 3cwt. 2qrs, with 17T. 12cwt. 2qrs. of hay, how much is that to each team?

When the multiplier, or divisor, exceeds 12, the operations of multiplying and dividing are not so easy, unless they be composite numbers; in that case, we may make use of the component parts, or factors, as was done in simple numbers.

Thus 15, in the example 15 being a composite numabove, is a composite number ber, and 3 and 5 its compoproduced by the multiplica-nent parts, or factors, we may





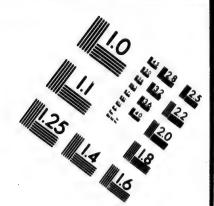
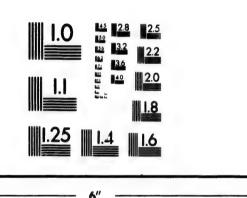


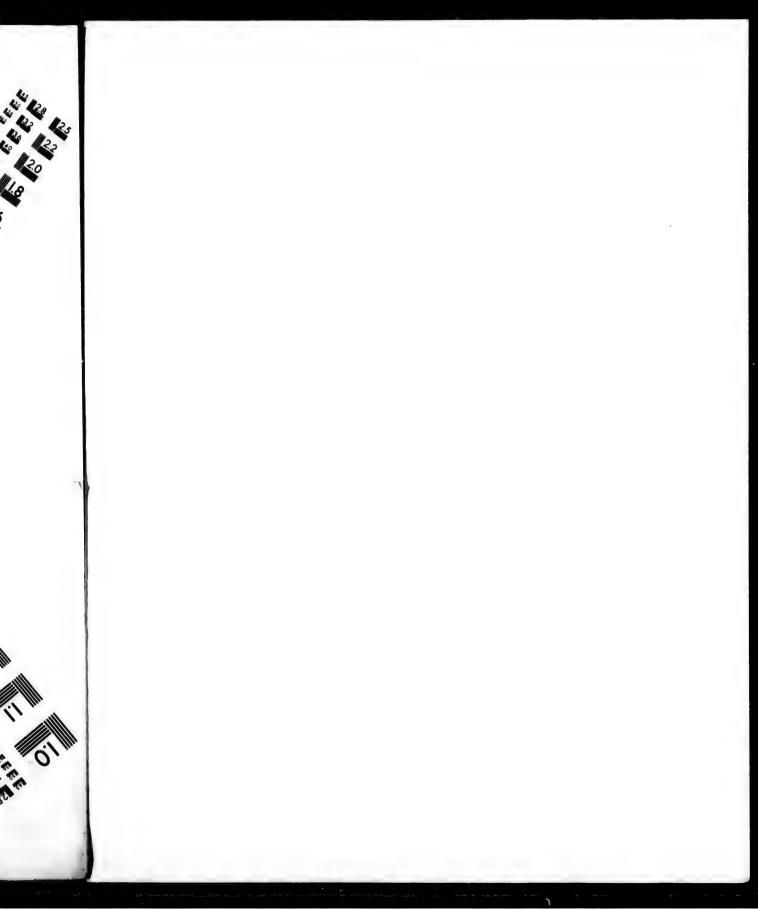
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tion of 3 and 5, (3×5 = divide 17T. 12cwt. 2qrs. by 15.) We may, therefore, one of these component parts, multiply 1T. 3cwt. 2qrs. by or factors, and the quotient one of those component parts, thence arising by the other, or factors, and that product by which will give the true the other, which will give the answer, as already taught, true answer, as has been al-(¶ 20.) ready taught, (¶ 11.)

OPERATION.

T. cwt. qr.

1 3 2
3 one of the factors.

The other factor, 5)5 17 2

The other factor, 5)5 17 2

17 12 2 the answer.

27. What will 24 barrels 28. Bought 24 barrels of flour cost, at 2£ 12s. 4d flour for 62£ 16s; how much a barrel?

29. What will 112lb. of 30. If I cwt. of sugar cost sugar cost 74d. per lb! 3£ 7s. 8d, what is that per

Note. 8, 7, and 2, are fac-lb?

31. How much brandy in 32. Bought 84 pipes of 84 pipes, each containing 112 brandy, containing 9468 gal. gal. 2qts. 1pt. 3g! 1qt. 1pt; how much in a pipe?

33. What will 139yds of 34. Bought 139 yards of cloth cost, at 3£ 6s. 5d. percloth for 461£ 11s. 11d; yard?

139 is not a composite number. When the divisor is such a ber. We may, however, de-number as cannot be produced compose this number thus, by the multiplication of small 139—100+30+9.

We may now multiply the divide after the manner of price of 1 yard by 10, which long division, setting down will give the price of 10 yards, the work of dividing and reand this product again by 10, ducing in manner as follows: which will give the price of

to an in the control or one to the confidence of the control on

11 11 (3.6

wt. 2grs. by onent parts, the quotient y the other. e the true dy taught.

PERATION. T. cwt. qr. 17 12)5 17 2

barrels of how much el ?

sugar cost is that per

pipes of 9468 gal. n in a pipe? yards of 11s. 11d; yard ? r is such a produced n of small way is to nanner of ng down and refollows :

We may then multiply the price of 10 yards by 3, which will give the price of 30 yards, and the price of 1 yard by 9, which will give the price of 9 yards, and these three products, added together, will evidently give the price of 189 yards; thus:

3 6 5 price of 1 yard.

33 4 2 price of 10 yards.

332 1 8 price of 100 yds. 6 price of 30 yds.

44

20

834

891 (6.

The divisor, 139, is contained in 461£ 3 times, (3£,) and a remainder of 44£, which must now be reduced to shil-29 17 9 price of 9 yde. lings, multiplying It by 20, and bringing in the given shil-461 11 11 price of 139 yds. lings, (11s.) making 891s, in which the divisor is contained.

Note. In multiplying the 6 times, (6s,) and a remainder price of 10 yards (33.6 4a of 57s, which must be reduc-2d.) by 3, to get the price of ed to pence, multiplying it by 30 yards, and in multiplying 12, and bringing in the given the price of 1 yard (3£ 6s. pence, (11d,) together mak-5d.) by 9, to get the price of ing 695d, in which the divi-9 yards, the multipliers, 3 sor is contained 5 times, (5d,) and 9, need not be writtenand no remainder. down, but may be carried in The several quotients, S.E. the mind. fla. 5d. evidently make the

answer.

The processes in the foregoing examples may now be presented in the form of a

RULE for the Multiplication of RULE for the Division of Comcompound Numbers. pound Numbers.

I. When the multiplier does I. When the divisor does not exceed 12, multiply suc-not exceed 12, in the manner cessively the numbers of each of short division, find how denomination, beginning withmany times it is contained in the least, as in multiplication the highest denomination, unof simple numbers, and carry der which write the quotient. as in addition of compound and if there be a remainder. numbers, setting down the reduce it to the next less dewhole product of the highest nomination, adding thereto the

denomination. number given, if any, of that denomination, and divide as before: so continue to do through all the denominations and the several quotients will

be the answer

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3. It

II. If the multiplier exceed II. If the divisor exceed 12. 12. and be a composite num-and be a composite, we may diber, we may multiply first by vide first by one of the comone of the component parts, ponent parts, that quotient by that product by another, and another, and so on, if the comso on, if the component parts ponent parts be more than be more than two; the last two, the last quotient will be product will be the product re-the quotient required. quired one and the met are

III. When the multiplier HI. When the divisor exexceeds 12, and is not a com-ceeds 12, and is not a composposite, multiply first by 10, posite number, divide after the and this product by 10, which manner of long division, setwill give the product for 100; ting down the work 200

and if the hundreds in the mul-ding and reducing.

tiplier, be more than one, multiply the product of 100 by the second and the seco numbers of hundreds; for the seed place and seed of fent, multiply the product of the state of the state of the state of 10 by the number of tent; for the set of the set the units, multiply the multiplicand; and these several proslucts will be the product required.

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EXAMPLES FOR PRACTICE. TOWN TO THE HALIFAX CURRENCY TO A STATE OF

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MISCELLANEOUS EXAMPLES.

1. What will 359 yards of 2. Pought 359vds. of cloth cloth cost, at 4s. 7id. per for 83£ 0s. 4id; what was vard? in to min to that a yard? have, but?

3. In 241 barrels of flour, 4 If 441cwt. 13lb. of flour ach containing lowt. 3qr. be contained in 241 barrely, lb; how many cwt? how much in a barrel 1.

5. How many bushels of 6. If 37Ibu. lpk. of wheat

wheat in 135 bags, each con-be divided equally into 135 aining 2 bu. 3 pks ? ... bags, how much will each! $3\times9\times5=135$. bag contain?

7. What will 35ewt. of to- 8. At 759£ 10s, for 35cwt. acco cost, at 3s. 10id. periof tobacco, what is that per b 1. of war I thoo I women it I the the the or

9. If 14 men build 19 rods 10. If 14 men build 92 rods feet of wall in one day, 12 feet of stone wall in 71 pany rods will they build in days, how much is that per day ! days !

¶ 39. 1. At 10s per yard, what will 17849 yards of oth cost ? ... y ... his we are well is the

Note. Operations in multiplication of pounds, shillings, ence, or of any compound numbers, may be facilitated by taking aliquot parts of a higher denomination. Thus, in this last example, if the price had been 20s. i. c. Let per yard, it is clear, the price of the whole would have been equal to the whole number of yards in pounds, 17849; but the price is 10s, i. c. Let per yard, and so the price of the whole will be equal to the number of yards, 17449 in pounds; 89244£, or 8924£ 10s.

When one quantity is contained in another exactly 2, 3, 4, 5, &c. times, it is called an aliquot or even part of that quantity; thus 64. is an aliquot part of a shilling, because 64. ×2=1 shilling; so 3d. is an aliquot part of a shilling; 3d.×4=1s. So 5s is an aliquot part of a pound, for 5s. ×4=1£; and 8s. 4d. is and aliquot part of a pound, for

3a. 4d.×6=1£, &c.

From the illustration of the last example it appears, that, when the price per yard, pound, &c. is one of these aliquot parts of a shilling, or a pound, the cost may be found by dividing the given number of yards, pounds, &c. by that number which it takes of the price to make 1s. or 1£. If the price be 6d. we divide by 2; if 5s. we divide by 4; if 3s. 4d. by 6, &c. &c. This manner of calculating by aliquot parts, is called Practice.

2. What sort 34648 yards of cloth, at 10s. or 12 per ard?—— at 5s.—12 per yard?—— at 4s.—12 per yard?—— at 2s.—10£ per yard?—— at 2s.—10£ per yard?

Ans. to leat, 3464£ 16s.

3. What cost 7430 pounds of sugar, at 6d,—is. per lb?

at 4d,—is. per lb? — at 3d,—is. per lb?

at 2d,—is. per lb? — at 1id,—is. per lb?

Ans. to the last, 7400 .- 9280, 9d = 46£ 8n. 9d.

4. At 3£ 16s. per cwt, what will 2qrs.—jcwt. cost!
— what will 1qr.—jcwt. cost! — what will 16lb.—
jcwt. cost! — what will 14lb.—jcwt. cost! — what will 8lb.—jcwt. cost!

will 8lb.—jcwt. cost!

816.—12 cwt. cost \$

5. What cost 340 yards of clean at 12s. 6d. per yard \$

12s. 6d.—10s. (—1£) and 2s. 6d. (—1£); therefore,

1)1)340

170£ = cost at 10s. per yard. 42£ 10s.= at 2s. 6d. per yard.

Inc. 2128 10s. at 12s. 6d. per yard.

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s. or i£ per 4s—i£ per at 2s.—i£ . 3464£ 16s.—is. per lb?

46£ 8s. 9d. =|cwt. cost! will 16lb.= ! — what last, 5s. 5|d. . per yard! therefore,

yard. yard. yard. 10a.—J£)340

2s. 6d = 4 of 10s.)170£ at 10s. per yard.
42£ 10s. at 2s. 6d. per yard.

Ans. 212£ 10s. at 12s. 6d. per yard.

SUPPLEMENT TO COMPOUND NUMBERS.

QUESTIONS.

1. What distinction do you make between simple and compound numbers? (§ 26.) 2. What is the rule for addition of compound numbers? 3. — for subtraction of &c.? 4. There are three conditions in the rule given for multiplication of compound numbers; what are they, and the methods of procedure under each? 5. To same questions in respect to the division of compound numbers? 6. When the multiplier or divisor is encumbered with a fraction, how do you proceed? 7. How is the distance of time from one date to another found? 8. How many degrees does the earth revolve from west to east in 1 hour? 9. In what time does it revolve 1°? Where is the time or hour of the day earlier—at the place most ensterly or most westerly? 10. The difference in longitude between two places being known, how is the difference in time calculated? 11. How may operations, in the multiplication of compound numbers, be facilitated? 12. What are some of the aliquot parts of 1£? — of 1s.? — of 1cwt.? 13. What is this manner of operating usually called?

EXERCISES.

1. Agentleman is possessed of 1½ dozen of silver spoons, each weighing 3oz. 5pwt; 2 doz. of tea spoons, each weighing 15pwt. 14gr; 3 silver cans, each 9oz. 7pwt; 2 silver tankards, each 2loz. 15pwt; and 6 silver porringers, each 1loz. 18pwt; what is the weight of the whole?

Ans. 18lb. 40z. 3pwt.

Note. Let the pupil be required to reverse and prove the following examples:

2. An English guines should weigh 5pwt. 6gr; a piece of gold weighs 3pwt. 17gr; how much is that short of the weight of a guines?

3. What is the weight of 6 chests of tea, each weighing 3cwt. 2ars. 9 lb?

4. In 35 pieces of cloth, each measuring 27 yards, how many yards?

5. How much brandy in 9 casks, each containing 45gal.

6. If 31cwt. 2qrs. 20 lb. of sugar be distributed equally

into 4 casks, how much will each contain?

7. At 41d. per lb., what costs 1cwt. of rice? —— 2cwt.;

Note. The pupil will recollect, that 8, 7 and 2 are factors of 112, and may be used in place of that number.

8. If 800cwt. of cocoa cost 182 13s. 4d. what is that per cwt 1 what is it per lb 1.

9. What will 94cwt. of copper cost at 5s. 9d. per lb?

10. If 64cwt. of chocolate cost 72£ 16s. what is that per lb?

11. What cost 456 bushels of potatoes, at 2s. 6d. per

bushel ?

Note. 2s. 6d. is 1 of 1£ (See ¶ 39.)

12. What cost 86 yards of broadcloth, at 15s. per yard? Note. Consult ¶ 39, ex. 5.

13. What cost 7846 pounds of tea, at 7s. 6d. per lb?

- at 14s. per lb ? -- 13s. 4d ?

14. At \$94.25 per cwt. what will be the cost of 2qrs. of tea? — of 3 qrs? — of 14 lbs.? — of 21 lbs? — of 16 lbs? — of 24 lbs?

Note. Consult ¶ 39, ex. 4 and 5.

15. What will be the cost of 2 pks. and 4qts. of wheat,

at Ss. 6d. per bushel ?

16. Supposing a meteor to appear so high in the heavens as to be visible at Montreal, 73° 20', at the city of Washington, 77° 43', and at the Sandwich Islands, 155° W. longitude, and that its appearance at the city of Washington be at 7 minutes past 9 o'clock in the evening; what will be the hour and minute of its appearance at Montreal and at the Sandwich Islands?

PBALOTIONS.

THE WALLETING

T 40. We have seen, (¶ 17,) that numbers expressing phole things are called integers, or whole numbers; but that, in division, it is often necessary to divide or break a whole thing into parts, and that these parts are called fractions, or broken numbers.

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It will be recollected, (7 14, ex. 11,) that when a thing or unit is divided into 3 parts, the parts or fractions are called thirds; when into four parts, fourths; when into six parts, sixths; that is, the fraction takes its name or denomination from the number of parts, into which the unit is divided. Thus, if the unit be divided into 16 parts, the parts are called sixteenths, and 5 of these parts would be 5 sixteenths, expressed thus, T_{18}^{0} . The number below the short line, (16,) as before taught, (¶ 17,) is called the denominator, because it gives the name or denomination to the parts; the number above the line is called the sumerator, because it numbers the parts.

The denominator shows how many parts it takes to make a unit or whole thing; the numerator shows how many of

these parts are expressed by the fraction.

1. If an orange be cut into 5 equal parts, by what fraction is 1 part expressed? 2 parts? 3 parts? 3 parts? 4 parts? 5 parts? how many parts make unity or a whole orange?

2. If a pie be cut into 8 equal pieces, and 2 of these pieces be given to Harry, what will be his fraction of the pie? if 5 pieces be given to John, what will be his fraction?

what fraction or part of the pie will be left ?

It is important to bear in mind, that fractions arise from division, (§ 17.) and that the numerator may be considered a dividend, and the denominator a divisor, and the value of the fraction is the quotient; thus, ½ is the quotient of 1 (the numerator) divided by 2, (the denominator;) ½ is the quotient arising from 1 divided by 4, and ½ is 3 times as much, that is, 3 divided by 4; thus, one fourth part of 3 is the same as 3 fourths of 1.

Hence, in all cases, a fraction is always expressed by the sign of division.

2 expresses the quotient, of which a is the divisor, or denominator.

3. If 4 oranges be equally divided among 6 boys, what part of an orange is each boy's share had your world.

A sixth part of Forange is 1, and a sixth part of 4 oranges is 4 such pieces, = 1. Ans. 1 of an orange.

4. If 3 apples be equally divided among 5 boys, what part of an apple is each boy's share 1 if 4 apples, what 1 if 2 apples, what 1 if 5 apples, what 1

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5. What is the quotient of 1 divided by 31 — of 2 by 3? — of 1 by 47 — of 2 by 41 — of 3 by 41 — of 5 by 71 — of 6 by 81 — of 4 by 51 — of 2 by 14?

6. What part of an orange is a third part of 2 oranges 1

one fourth of 2 oranges 1 — 1 of 3 oranges 1 —

t of three oranges 1 — 1 of 4 1 — 1 of 2 1 — 1 of 5 1

of 3 1 — 1 of 2 7

A proper fraction. Since the denominator shows the number of parts necessary to make a whole thing, or 1, it is plain, that, when the numerator is less than the denominator, the fraction is less than a unit, or whole thing; it is then called a proper fraction. Thus, 1, 2, &c. are proper fractions.

An improper fraction. When the numerator equals or ex-

An improper fraction. When the numerator equals or exceeds the denominator, the fraction equals or exceeds unity, or 1, and is then called an improper fraction. Thus, §, §,

4, 4, are improper fractions.

A mixed number, as already shown, is one composed of a whole number and a fraction. Thus, 141, 137, &c. are mixed numbers.

7. A father bought 4 oranges, and cut each orange into 6 equal parts; he gave to Samuel 3 pieces, to James 5 pieces, to Mary 7 pieces, and to Nancy 9 pieces; what was each one's fraction 1

Was James' fraction proper, or improper ? Why ! Was Nancy's fraction proper, or improper ? Why !

To change an improper fraction to a whole or mixed number.

¶ 41. It is evident, that every improper fraction must contain one or more whole ones, or integers.

How many whole apples are there in 4 halves (4) of an apple 1 — in § 1: — in § 1 — in § 1 — in § 1 — in § 1 — in § 1.

2. How many yards in § of a yard! — in § of a yard!
— in § ! — in § ! — in U ! — in U ! — in U!
— in V ! — in V !

3. How many bushels in 8 pecks 1 that is, in 4 of a busheld in 10 1 in 11 in 13 1 in 12 ! in 12 1 in 12 1 in 12 1

This finding how many integers, or whole things, are contained in any improper fraction, is called reducing as improper fraction to a whole on mixed number.

of 2 by 3?
11 — of 5
12 by 14!
2 oranges 1
13 — + of 5!

vs the numl, it is plain, hinator, the then called ractions. equals or ex-

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orange into to James 5 s; what was

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halves (4) of ______ in 30 !

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4. If I give 27 children 4 of an orange each, how many oranges will it take 1 It will take 37; and it is evident, OPERATION. that dividing the numerator, 27, (== the

1)27

number of parts contained in the fraction,) by the denominator, 4, (= the number of parts in 1 orange,) will give the number of whole oranges.

Hence, To reduce an improper fraction to a whole ar mixed number,—Ruln: Divide the numerator by the denominator; the quotient will be the whole or mixed number.

EXAMPLES FOR PRACTICE.

5. A man, spending $\frac{1}{2}$ of a pound a day, in 83 days would spend $\frac{1}{6}$ of a pound; how many pounds would that be !

Ans. 134£.

6. In 1417 of an hour, how many whole hours ?

The 60th part of an hour is a minute: therefore the question is evidently the same as if it had been, in 1417 minutes, how many hours?

Ans. 2333 hours.

7. In ⁸78 of a shilling, how many units or shillings?

Ans. 730 A shillings

8. Reduce 14978 to a whole or mixed number.

9. Reduce 38, 706, 875, 4788, 3465, to whole or mixed numbers.

To reduce a whole or mixed number to an improper fraction.

4 ¶ 42. We have seen, that an improper fraction may be changed to a whole or mixed number; and it is evident, that, by reversing the operation, a whole or mixed number may be changed to the form of an improper fraction.

1. In 2 whole apples, how many halves of an apple ? Ans. 4 halves; that is, 4. In 3 apples, how many halves? in 4 apples? in 6 apples? in 10 apples? in 24? in 60? in 170? in 492? the particle of a p

2. Reduce 2 yards to thirds. Ans. §. Reduce 23 yards to thirds. Ans. §. Reduce 3 yards to thirds — 34 yards. — 5 yards. — 54 yards. — 6 4 yards.

8. Reduce 2 bushels to fourths. — 2½bu. — 6 bushels. — 6½ bushels. — 7½ bushels. — 25½ bushels.

4. In $16\frac{1}{12}$ pounds, how many $\frac{1}{12}$ of a pound ?

that is, multiply the whole number by the denominator, the

product will be the number of 12ths in 16£: 16×12=192, and this, increased by the numerator of the fraction, (5,) evidently gives the whole number of 12ths; that is, \$\frac{1}{2}\$ of a pound, Ans.

OPERATION.

16 pounds

192 = 12ths in 16 pounds, or the whole number.

5 = 12ths contained in the fraction.

197 = W, the answer.

Hence, To reduce a mixed number to an improper fraction,— RULE: Multiply the whole number by the denominator of the fraction, to the product add the numerator, and write the result over the denominator.

EXAMPLES FOR PRACTICE.

5. What is the improper fraction equivalent to $23\frac{2}{6}$ hours?

Ans. $\frac{1}{4}$ of an hour.

6. Reduce 730 A shillings to 12ths.

As 1/2 of a shilling is equal to 1 penny, the question is evidently the same as, in 730s. 3d., how many pence 1

Ans. \$\frac{976}{4}\$ of a shilling; that is \$763 pence.

7. Reduce $1\frac{1}{26}$, $17\frac{26}{26}$, $8\frac{7}{100}$, $4\frac{7}{1000}$, and $7\frac{3}{2}\frac{1}{2}\frac{5}{6}$ to improper fractions.

8. In 15617 days, how many 24ths of a day?

Ans. 3 761 = 3761 hours.

9. In 3424 gallons, how many 4ths of a gallon ?

Ans. 1371 of a gallon = 1371 quarts.

To reduce a fraction to its lowest or most simple terms.

¶ 48. The numerator and the denominator, taken to-

gether, are called the terms of the fraction.

If $\frac{1}{2}$ of an apple be divided into 2 equal parts, it becomes $\frac{3}{4}$. The effect on the fraction is evidently the same as if we had multiplied both of its terms by 2. In either case, the parts are made 2 times as MANY as they were before; but they are only HALF AS LARGE; for it will take 2 times as many fourths to make a whole one as it will take halves; and hence it is that $\frac{3}{4}$ is the same in value or quantity as $\frac{1}{4}$.

? is 2 parts; and if each of these parts be again divided into 2 equal parts, that is, if both terms of the fraction be

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multiplied by \mathfrak{D} , it becomes $\frac{1}{2}$. Hence, $\frac{1}{2} = \frac{2}{4} = \frac{1}{4}$, and the reverse of this is evidently true, that $\frac{1}{2} = \frac{1}{4}$.

It follows therefore, by multiplying or dividing both terms of the fraction by the same number, we change its terms with-

out altering its value.

7 43.

Thus, if we reverse the above operation, and divide both terms of the fraction \(\frac{1}{2} \) by \(2 \), we obtain its equal, \(\frac{2}{4} \); dividing again by \(2 \), we obtain \(\frac{1}{2} \), which is the most simple form of the fraction, because the terms are the least possible by which the fraction can be expressed.

The process of changing & into its equal &, is called reducing the fraction to its lowest terms. It consists in dividing both terms of the fraction by any number which will divide them both without a remainder, and the quotient thence arising in the same manner, and so on, till it appears that no number greater than 1 will again divide them.

A number, which will divide two or more numbers without a remainder, is called a common divisor, or common measure of those numbers. The greatest number that will do this is called the greatest common divisor.

1. What part of an acre are 128 rods !

One rod is $\frac{1}{160}$ of an acre, and 128 rods are $\frac{128}{60}$ of an acre. Let us reduce this fraction to its lowest terms. We find, by trial, that 4 will exactly measure both 128 and 160, and, dividing, we change the fraction to its equal $\frac{28}{16}$. Again, we find that 8 is a divisor common to both terms, and, dividing, we reduce the fraction to its equal $\frac{4}{5}$, which is now in its lowest terms, for no greater number than 1 will again measure them. The operation may be presented thus:

2. Reduce \$50, 257, 168, and 1984 to their lowest terms.

Ans. 1, 1, 7, and 2.

Note. If any number ends with a cipher, it is evidently divisible by 10. If the two right hand figures are divisible by 4, the whole number is also. If it ends with an even number, it is divisible by 2; if with a 5 or 0, it is divisible by 5.

3. Reduce \$88, 450, 198, and 31 to their lowest terms.

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Any fraction may evidently be reduced to its lowest terms by a single division, if we use the greatest common divisor of the two terms. The greatest common measure of any two numbers may be found by a sort of trial easily made. Let the numbers be the two terms of the fraction $\frac{128}{180}$. The common divisor cannot exceed the less number, for it must measure it. We will try, therefore, if the less number, 128, which measures itself, will also divide or measure 160.

160(1 128 in 160 goes 1 time, and 32 remain; 128, therefore, is not a divisor of 160. We will now try whether this remainder be not the divisor sought; for if 32 be a divisor of 128, the former divi-

sor, it must also be a divisor of 160, which consists of 128 + 32. 32 in 128 goes 4 times, without any remainder. Consequently, 32 is a divisor of 128 and 160. And it is evidently the greatest common divisor of these numbers; for it must be contained at least once more in 160 than in 128, and no number greater than their difference, that is, greater than 32, can do it.

Hence, the rule for finding the greatest common divisor of two numbers:—Divide the greater number by the less, and that divisor by the remainder, and so on, always dividing the last divisor by the last remainder, till nothing remain. The last divisor will be the greatest common divisor required.

Note. It is evident, that, when we would find the greatest common divisor of more than two numbers, we may first find the greatest common divisor of two numbers, and then of that common divisor and one of the other numbers, and so on to the last number. Then will the greatest common divisor last found be the answer.

4. Find the greatest common divisor of the terms of the fraction 31, and, by it, reduce the fraction to its lowest terms.

OPERATION. 21)35(1 21 14)21(1

Greatest divis. 7)14(2. Then, 7) $\frac{21}{35} = \frac{3}{5}$

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5. Reduce 95 to its lowest terms.

Ans. A.

Note. Let these examples be wrought by both methods; by several divisors, and also by finding the greatest common divisor.

6. Reduce 1154 to its lowest terms.	Ans. 1.
7. Reduce 114 to its lowest terms.	Ans. 7.
8. Reduce 468 to its lowest terms.	Ans. 117.
9. Reduce 1421 to its lowest terms.	Ans. 1.

To divide a fraction by a whole number.

¶ 45. 1. If 2 yards of cloth cost \(\frac{3}{3} \) of a pound, what does 1 yard cost? how much is \(\frac{3}{3} \) divided by 2?

2. If a cow consume $\frac{3}{4}$ of a bushel of meal in 3 days, how much is that per day? $\frac{3}{4} \div 3 =$ how much?

3. If a boy divide $\frac{1}{2}$ of an orange among 2 boys, how much will be give each one $\frac{1}{2}$ $\frac{1}{2}$ = how much ?

4. A boy bought 5 cakes for 19 of a shilling; what did 1 cake cost 1 +9 ÷ 5 == how much?

5. If 2 bushels of apples cost 10 of a pound, what is that per bushel? I program will be not full program of

1 bushel is the half of 2 bushels; the half of $\frac{1}{18}$ is $\frac{1}{18}$. Ans. $\frac{1}{18}$. pound.

6. If 3 horses consume 13 of a ton of hay in a month, what will 1 horse consume in the same time?

13 are 12 parts; if 3 horses consume 12 such parts in a month, as many times as 3 are contained in 12, so many parts 1 horse will consume.

Ans. 43 of a ton.

7. If §§ of a barrel of flour be divided equally among 5 families, how much will each family receive?

The process in the foregoing examples is evidently dividing a fraction by a whole number; and consists, as may be seen, in dividing the numerator, (when it can be done without a remainder,) and under the quotient writing the denominator. But it not unfrequently happens, that the numerator will not contain the whole number without a remainder.

8. A man divided 4 of a pound equally among 2 persons; what part of a pound did he give to each 1

description of a pound divided into 2 equal parts will be 4ths.

He gave 1 of a pound to each.

ve may first s, and then imbers, and test common

terms of the lowest terms.

= 3 Ans.

9. A mother divided $\frac{1}{2}$ a pie among 4 children; what part of the pie did she give to each $\frac{1}{2} \div 4 = 1$ how much 1

10. A hoy divided $\frac{1}{3}$ of an orange equally among 3 of his companions; what was each one's share! $\frac{1}{3} \div 3 =$ how much!

11. A man divided \$\frac{3}{4}\$ of an apple equally between 2 children; what part did he give to each \$\frac{3}{4}\$ divided by 2 ==

what part of a whole one?

‡ is 3 parts: if each of these parts be divided into 2 equal parts, they will make 6 parts. He may now give 3 parts to one, and 3 to the other: but 4ths divided into 2 equal parts, become 8ths. The parts are now twice so many, but they are only half so large; consequently, ‡ is only half so much as ‡.

Ans. ‡ of an apple.

In these last examples, the fraction has been divided by multiplying the denominator, without changing the numerator. The reason is obvious; for, by multiplying the denominator by any number, the parts are made so many times smaller, since it will take so many more of them to make a whole one; and if no more of these smaller parts be taken than were before, taken of the larger, that is, if the numerator be not changed, the value of the fraction is evidently made so many times less.

146. Hence, we have Two ways to divide a fraction by a whole number:

I. Divide the numerator by the whole number, (if it will contain it without a remainder,) and under the quotient write, the denominator. Otherwise,

II. Multiply the denominator by the whole number, and

over the product write the numerator.

EXAMPLES FOR PRACTICE.

1. If 7 pounds of tobacco cost $\frac{21}{25}$ of a pound, what is that per pound? $\frac{21}{21}$ —how much? Ans. 2 of a pound.

2. If \$\frac{1}{2}\$ of an acre produce 24 bushels, what part of an acre will produce 1 bushel 1 \$\frac{1}{2}\$ \tag{-24} how much !

3. If 12 yards of silk cost 19 of a pound, what is that a yard; 19:12 how much?

4. Divide \$ by 16. pp base, a to, a rith and a ic

Note. When the divisor is a composite number, the intelligent pupils will perceive, that he can first divide by one component part, and the quotient thence arising by the oth-

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er; thus he may frequently shorten the operation. In the last example, $16 = 8 \times 2$, and $\frac{1}{9} \div \frac{2}{9}$, and $\frac{1}{4} \div 2 = \frac{1}{18}$.

Ans. $\frac{1}{18}$.

5. Divide 10 by 12. Divide 10 by 21. Divide 16 by 24.
6. If 6 bushels of wheat cost £14 what is it per bushel?

Note. The mixed number may evidently be reduced to an improper fraction, and divided as before.

Ans. $\frac{1}{4}\frac{4}{3} = \frac{7}{24}$ of a pound, expressing the fraction in its lowest terms. (¶ 43.)

7. Divide £4+3 by 9.

8. Divide 125 by 5. 9. Divide 143 by 8.

10. Divide 1841 by 7.

Quot. $\frac{7}{13}$ of a pound. Quot. $\frac{1}{2}$ =24.

Quot. 137.

Note. When the mixed number is large, it will be most convenient, first, to divide the whole number, and then reduce the remainder to an improper fraction; and, after dividing, annex the quotient of the fraction to the quotient of the whole number; thus, in the last example, dividing $184\frac{1}{2}$ by 7, as in whole numbers, we obtain 26 integers, with $2\frac{1}{2}$ remainder, which, divided by 7, gives $\frac{1}{14}$ and $26 + \frac{1}{14}$ $= 26\frac{1}{14}$, Ans.

11. Divide 27861 by 6. Ans. 4648

12. How many times is 24 contained in 764611!

Ans. 318347.

13. How many times is 3 contained in 4621!

Ans. 1541?

To multiply a fraction by a whole number.

¶ 47. 1. If 1 yard of cloth cost $\frac{1}{3}$ of a pound, what will 2 yards cost? $\frac{1}{4} \times 2 = \text{how much}$?

2. If a cow consume $\frac{1}{2}$ of a bushel of meal in 1 day, how much will she consume in 3 days? $\frac{1}{2} \times 3 =$ how much?

3. A boy bought 5 cakes, at $\frac{2}{3}$ of a shilling each; what did he give for the whole $\frac{1}{3} \times 5 = \text{how much } \frac{1}{3}$

4. How much is 2 times \(\frac{1}{3} \) 1 \(\ldots \) 2 times \(\frac{1}{2} \) 1

5. Multiply # by 3. — # by 2. — # by 7.

6. If a man spend 2 of a shilling per day, how much will he spend in 7 days?

3 is 3 parts. If he spend 3 such parts in 1 day, he will evidently spend 7 times 3, that is, \$\frac{1}{2}\$ in 7 days.

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Hence, we perceive, a fraction is multiplied by multiplying the numerator, without changing the denominator.

But it has been made evident, (¶ 46,) that multiplying the denominator produces the same effect on the value of the fraction, as dividing the numerator: hence, also, dividing the denominator will produce the same effect on the value of the fraction, as multiplying the numerator. In all cases, therefore, where one of the terms of the fraction is to be multiplied the same result will be effected by dividing the other; and where one term is to be divided, the same result may be effected by multiplying the other.

This principle, borne distinctly in mind, will frequently enable the pupil to shorten the operations of fractions. Thus, in the following example:

At 2 of a pound, for 1 pound of sugar, what will 11 pounds cost?

Multiplying the numerator by 11, we obtain for the product 22-1 of a pound for the answer.

I 48. But by applying the above principle, and dividing the denominator, instead of multiplying the numerator we at once come to an answer, $\frac{2}{6}$, in much lower terms. Hence, there are two ways to multiply a fraction by a whole number:

1. Divide the denominator by the whole number, (when it can be done without a remainder,) and over the quotient write the numerator.—Otherwise,

II. Multiply the numerator by the whole number, and under the product write the denominator. If then it be an improper fraction, it may be reduced to a whole or mixed number.

EXAMPLES FOR PRACTICE.

1. If one man consume $\frac{5}{36}$ of a barrel of flour in a month, how much will 18 men consume in the same time? — 6 men? — 9 men? Ans. to the last. 11 barrels.

2. What is the product of $\frac{71}{120}$ multiplied by 40? $\frac{71}{120} \times 40 = \text{how much}$?

3. Multiply 13 by 10. — by 18. — by 21. — b 36. — by 48. — by 60.

Note. When the multiplier is a composite number, the pupil will recollect (7 11,) that he may multiply first by one component part, and that product by the other. Thus,

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number, the tiply first by ther. Thus, in the last example, the multiplier 60 is equal to 12×5 ; therefore, $\frac{13}{12} \times 12 = \frac{13}{13}$, and $\frac{13}{12} \times 5 = \frac{6}{12} = \frac{1}{12}$. Ans.

4. Multiply 54 by 7. Ans. 401.

Note. It is evident, that the mixed number may be reduced to an improper fraction, and multiplied, as in the preceding examples; but the operation will usually be shorter, to multiply the fraction and whole number separately, and add the results together. Thus, in the last example, 7 times 5 are 35; and 7 times 4 are 2 = 54, which, added to 35, make 404, Ans.

Or, we may multiply the fraction first, and, writing down the fraction, reserve the integers, to be carvied to the

product of the whole number.

5. What will 913 tons of hay come to at 32 per ton?

Ans. 28£. 19s.

Note. The fraction is here reduced to its lowest terms; the same will be done in all the following examples.

To multiply a whole number by a fraction!

¶ 49. 1. If 36 pounds be paid for a piece of cloth, what

costs 3 of it 1 36×3-how much?

a of the quantity will cost a of the price; a time 36 pounds, that is a of 36 pounds, implies that 36 be first divided into 4 equal parts, and then that 1 of these parts be taken 3 times; 4 into 36 goes 9 times, and 3 times 9 is 27.

From the above example it plainly appears that the object in multiplying by a fraction, whatever may be the multiplicand, is to take of the multiplicand a part, denoted by the multiplying fraction; and that this operation is composed of two others, viz. a division by the denominator of the multiplying fraction, and a multiplication of the quotient by the numerator. It is a matter of indifference, as it respects the result, which of these operations precedes the other, for 36 $\times 3 \div 4 - 27$, the same as $36 \div 4 \times 3 - 27$.

Hence,—To multiply by a fraction, whether the multiplicand be a whole number or a fraction,—RULE.

Divide the multiplicand by the denominator of the multi-

plying fraction, and multiply the quotient by the numerator; or, (which will often be found more convenient in practice,) first multiply by the numerator, and divide the product by the denominator.

Multiplication, therefore, when appplied to fractions, does not always imply augmentation or increase, as in whole numbers; for, when the multiplier is less than unity, it will always require the product to be less than the multiplicand, to which it would be only equal if the multiplier were 1.

We have seen, (\P 10,) that, when two numbers are multiplied together, either of them may be made the multiplier, without effecting the result. In the last example, therefore, instead of multiplying 16 by $\frac{3}{4}$, we may multiply $\frac{3}{4}$ by 16, ($\frac{9}{4}$, and the result will be the same.

EXAMPLES FOR PRACTICE.

2. What will 40 barrels of meal come to at $\frac{3}{4}$ of a pound per barrel 1 $40 \times \frac{3}{4}$ —how much 1

3. What will 24 yards of cloth cost at # of a pound per yaid? 24×4=how much?

4. How much is 1 of 90 ! — 2 of 369 ! — 70 of 45 ?

5. Multiply 45 by To: Multiply 20 by 1.

To multiply one fraction by another.

¶ 50. 1. A man owning $\frac{4}{3}$ of a farm, sold $\frac{2}{3}$ of his share; what part of the whole farm did he sell? $\frac{2}{3}$ of $\frac{4}{5}$ is hew much?

We have just seen, (¶ 49,) that to multiply by a fraction, is to divide the multiplicand by the denominator, and to multiply the quotient by the numerator. $\frac{4}{5}$ divided by 3, the denominator of the multiplying fraction, (¶ 46,) is $\frac{4}{15}$, which, multiplied by 2, the numerator, (¶ 48,) is $\frac{4}{15}$, Ans.

The process, if carefully considered, will be found to consist in multiplying together the two numerators for a new numerator, and the two denominators for a new denominator.

EXAMPLES FOR PRACTICE.

2. A man, having 4 of a pound, gave 10 of it for a dinner what did the dinner cost him?

Ans. 25 pound.

3. Multiply 7 by 9. Multiply 9 by 2. Product, 9

4. How much is \$ of \$ of \$ of \$?

Note. Fractions like the above, connected by the word

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of, are sometimes called compound fractions. The word or implies their continual multiplication into each other.

Ans. 188 = 70.

When there are several fractions to be multiplied continually together, as the several numerators are factors of the new numerator, and the several denominators are factors of the new denominator, the operation may be shortened by dropping those factors which are the same in both terms, on the principle explained in ¶ 43. Thus, in the last example, $\frac{1}{5}$, $\frac{3}{4}$, $\frac{3}{4}$, we find a 4 and a 3 both among the numerators and among the denominators; therefore we drop them multiplying together only the remaining numerators, $2 \times 7 = 14$, for a new numerator, and the remaining denominators, $5 \times 8 = 40$, for a new denominator, making $\frac{1}{40} = \frac{7}{40}$, Ans. as before.

5. \$\frac{2}{3}\$ of \$\frac{2}{3}\$ of \$\frac{2}{3}\$ of \$\frac{2}{3}\$ of \$\frac{2}{3}\$ of \$\frac{2}{3}\$ of \$\frac{2}{3}\$ and \$\frac{2}{3}\$. What is the continual product of 7, \$\frac{1}{3}\$, \$\frac{2}{3}\$ and \$\frac{2}{3}\$!

Note. The integer 7 may be reduced to the form of an improper fraction, by writing a unit under it for a denominator, thus, ‡.

Ans. 241.

7. At 25 of a pound a yard, what will 7 of a yard of cloth cost 1

8. At $1\frac{3}{8}$ pounds per barrel for flour, what will $\frac{7}{16}$ of a barrel cost ?

13 U then UX To Line. Ans.

9. At $\frac{1}{6}$ of a pound, per yard, what cost $7\frac{1}{2}$ yards?

Ans. $6\frac{1}{2}$

10. At \$21 per yard, what cost 64 yards 1 Ans. \$1432.

11. What is the continued product of 3, \(\frac{2}{5}\), \(\frac{1}{5}\) of \(\frac{2}{5}\), \(\frac{1}{5}\) of \(\frac{2}{5}\), \(\frac{1}{5}\) of \(\frac{2}{5}\), \(\frac{1}{5}\) of \(\frac{2}{5}\), \(\frac{1}{5}\).

¶ 51. The Rule for the multiplication of fractions may now be presented at one view:

1. To multiply a fraction by a whole number, or a whole number by a fraction,—Divide the denominator by the whole number, when it can be done without a remainder; otherwise, multiply the numerator by it, and under the product write the denominator, which may then be reduced to a whole or mixed number.

II. To multiply a mixed number by a whole number,—Multiply the fraction and integers, separately, and add their products together.

III. To multiply one fraction by another, Multiply togeth-

er the numerators for a new numerator, and the denominators for a new denominator.

Note. If either or both are mixed numbers, they may first be reduced to improper fractions.

EXAMPLES FOR PRACTICE.

1. At A£ per yard, what cost 4 yards of cloth ? -- 5 yds. 1 — 6 yds. 1 — 8 yds. 1 — 20 yds. 1

Ans. to the last, 15£.

2. Multiply 148 by $\frac{1}{2}$. — by $\frac{3}{4}$. — by $\frac{3}{20}$. — by $\frac{3}{10}$. Last product, 444.

3. If 2 70 tons of hay keep 1 horse through the winter. how much will it take to keep 3 horses the same time !-7 horses? —— 13 horses? Ans. to the last, $37\frac{7}{10}$ tons. 4. What will $8\frac{7}{12}$ barrels of cider come to, at 7 shillings

per barrel 1

5. At 149£ per cwt. what will be the cost of 147 cwt.?

6. A owned \$ of a note; B owned 6 of the same; the note amounted to 1000.5; what was each one's share of the money !

7. Multiply 1 of 2 by 2 of 1. 8. Multiply 71 by 2 15.

Product. 1. Product. 151.

9. Multiply 2 by 22.

Product. 24. Product, 1.

10. Multiply 2 of 6 by 2. 11. Multiply 2 of 2 by 1 of 4.

Product, 3.

12. Multiply continually together 4 of 8, 2 of 7, 3 of 9, Product, 20. and 1 of 10.

13. Multiply 1000000 by 4. Product, 5555558.

To divide a whole number by a fraction,

We have already shown, (¶ 46,) how to divide a fraction by a whole number; we now proceed to show how to divide a whole number by a fraction.

1. A man divided 92. among some poor people, giving them f of a pound each; new many were the persons who

received the money ! 9-1-1-how many !

1 pound is 4, and 9 pounds is 9 times as many, that is, 4, then 2 is contained in 4 as many times as 3 is contained in 36. Ans. 12 persons,

That is, Multiply the dividend by the denominator of the dividing fraction, (thereby reducing the dividend to parts of the same magnitude as the divisor,) and divide the prothat by the memorator, we also as the Resemble the

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OPERATION.

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5 Denominator.

Numerator, 3)40

Quotient, 131 times, the answer.

To multiply by a fraction, we have seen, (¶ 49,) implies two operations—a division and a multiplication; so, also, to divide by a fraction implies two operations—a multiplication and a division.

¶ 53. Division is the reverse of multiplication.

To multiply by a fraction, whether the multiplicand be a whole number or a fraction, whole number or a fraction, as has already been shown, we multiply by the denominator of the multiplying and divide the product by the fraction, and multiply the quotient by the numerator.

Note. In either case, it is matter of indifference, as it respects the result, which of these operations precedes the other; but in practice it will frequently be more convenient, that the multiplication precede the division.

12 multiplied by \$\frac{2}{3}\$, the product is 9.

In multiplication, the multiplier being less than unity, ing less than unity, or 1, will or 1, will require the product be contained a greater number to be less than the multipli-of times; consequently will recand, (¶ 49,) to which it is quire the quotient to be great-only equal when the multiplier is 1, and greater when it will be equal when the ditter than 1. visor is 1, and less when the divisor is more than 1.

EXAMPLES FOR PRACTICE.

1. How many times is $\frac{1}{2}$ contained in 7? $7 \div \frac{1}{2} = \text{how many ?}$

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2. How many times can I draw f of a gallon of wine out of a cask containing 26 gallons?

3. Divide 3 by 2. — 6 by 2. — 10 by 2.

4. If a man drink p_0 of a quart of rum a day, how long will 3 gallons last him ?

5. If $2\frac{3}{4}$ bushels of oats sow an acre, how many acres will 22 bushels sow ? $22 \div 2\frac{3}{4} = \text{how many times ?}$

Note. Reduce the mixed number to an improper fraction, 22 = 2.

6. At 13£ a yard, how many yards of cloth may be bought for 37£?

Ans. 264 yards.

7. How many times 103 contained in 84 1

Ans. 901 times.

8. How many times is % contained in 61

Ans. 4 of 1 time.

9. How many times is 84 contained in 53 !

Ans. 614 times.

10. At $\frac{2}{6}$ of a pound for building 1 rod of stone wall, how many rods may be built for 87£? $87 \div \frac{2}{6} = \text{how many times}$?

To divide one fraction by another.

¶ 54. 1. At $\frac{2}{3}$ of a pound per barrel, how much rye may be bought for $\frac{3}{5}$ of a pound? $\frac{3}{4}$ is contained in $\frac{3}{5}$ how many times 1

Had the rye been 2 whole pounds per barrel, instead of $\frac{2}{3}$ of a pound, it is evident, that $\frac{3}{3}$ of a pound must have been divided by 2, and the quotient would have been $\frac{3}{10}$; but the divisor is 3ds, and 3ds will be contained 3 times where a like number of whole ones are contained 1 time; consequently the quotient $\frac{3}{10}$ is 3 times too small, and must therefore, in order to give the true answer, be multiplied by 3, that is, by the denominator of the divisor; 3 times $\frac{3}{10} = \frac{3}{10}$ barrel, unsuer.

The process is that already described, ¶ 52 and ¶ 53. If carefully considered, it will be perceived, that the numerator of the divisor is multiplied into the denominator of the dividend, and the denominator of the divisor into the numerator of the dividend; wherefore, in practice, it will be more convenient to invert the divisor; thus, ⅔ inverted becomes ⅗; then multiply together the two upper terms for a numerator, and the two lower terms for a denominator, as in the multi-

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nany acres mes ? roper frac-

ne. 8 acres. th may be 264 yards.

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. 614 times. stone wall, $\frac{\cdot}{\cdot}$ = how

uch rye may h & how ma-

instead of st have been een at; but times where ime; conse-, and must e multiplied or: 3 times

nd 1 53. If ne numerator of the divie numerator ne more conbecomes 3: numerator. n the multiplication of one fraction by another. Thus, in the above example, 3 × 3 $\overline{2} \times \overline{5} = \overline{10}$, as before, 9

EXAMPLES FOR PRACTICE.

2. At 1 of a pound per bushel for wheat, how many bushels may be bought for I of a pound I How many times is 1 contained in 7? Ans. 34 bushels.

3. If \$\frac{7}{4}\$ of a yard of cloth cost \$\frac{9}{4}\$ of a pound, what is that per yard? It will be recollected, (¶ 24,) that when the cost of any quantity is given to find the price of a unit, we divide the cost by the quantity. Thus, & (the cost) divided by I (the quantity) will give the price of 1 yard.

Ans. 24 of a pound per yard.

PROOF. If the work be right, (¶ 16, "Proof,") the product of the quotient into the divisor will be equal to the dividend; thus, $\frac{24}{4} \times \frac{7}{4} = \frac{3}{4}$. This, it will be perceived, is multiplying the price of one yard ($\frac{34}{2}$) by the quantity ($\frac{7}{2}$) to find the cost (2;) and is, in fact, reversing the question, thus, if the price of 1 yard be 24 of a pound, what will 7 of a yard cost? Ans. 7 of a pound.

Note. Let the pupil be required to reverse and prove the succeeding examples in the same manner.

4. How many bushels of wheat, at 3 of a pound per bushel, may be bought for $\frac{7}{8}$ of a pound? Ans. $4\frac{2}{3}$ bushels.

5. If 42 pounds of butter serve a family I week, how many weeks will 367 pounds serve them?

The mixed numbers, it will be recollected, may be reduced to improper fractions. Ans. 8 3 weeks.

6. Divide & by & Quot. 1 Divide 4 by 1. Quot. 2. 7. Divide 2 by 1. Quat. 3 Divide 7 by 10. Quot. 36.

8. Divide 21 by 11. Divide 103 by 21.

Quot. 11. 12 155 9. How many times 10 contained in 2?

Ans. 4 times. 10. How many times is 3 contained in 47?

Ans. 114 times. Quot. 4.

11. Divide of 1 by 7 of 1. # 55. The RULE for division of fractions may now be

presented at one view : 46 2000 of deaso of I. To divide a fraction by a whole number - Divide the numerator by the whole number, when it can be done without a remainder, and under the quotient write the denominator; otherwise, multiply the denominator by it, and over the product write the numerator.

11. To divide a whole number by a fraction,—Multiply the dividend by the denominator of the fraction, and divide

the product by the numerator.

III. To divide one fraction by another,—Invert the divisor, and multiply together the two upper terms for a numerator, and the two lower terms for a denominator.

Note. If either or both are mixed numbers, they may be

reduced to improper fractions.

EXAMPLES FOR PRACTICE.

1. If 7 lb. of tobacco cost $\frac{1}{100}$ of a pound, what is it per pound? $\frac{1}{100}$:7= how much? $\frac{1}{100}$ is how much?

2. At 12. for # of a barrel of cider, what is that per bar-

rel?

3. If 4 pounds of sugar cost 13, of a pound, what does 1 pound cost?

4. If $\frac{7}{4}$ of a yard cost 13s, what is the price per yard ?

5. If 144 yards cost 43£. what is the price per yard 1

Ans. 2444.

6. At 44 pounds for 104 barrels of cider, what is that per barrel?

Ans. \$\frac{1}{2}\mathcal{L}\$.

7. How many times is \$\frac{2}{3}\$ contained in 746? Ans. 1989\$.

8. Divide $\frac{1}{2}$ of $\frac{2}{3}$ by $\frac{3}{4}$.

Quot. $\frac{1}{4}$.

Divide $\frac{7}{4}$ by $\frac{4}{5}$ of $\frac{2}{5}$.

Quot. $\frac{343}{2}$.

9. Divide 1 of 1 by 2 of 3. Quot. 12.

10. Divide 1 of 4 by 15. Quot. 3.

11. Divide 4g by g of 4. Quot. 210.
12. Divide 2 of 4 by 4g. Quot. 29. Quot. 29.

ADDITION AND SUBTRACTION OF FRACTION

¶ 56. 1. A boy gave to one of his companions g of an orange, to another g, to another g; what part of an orange did he give to all? 2+1+1= how much? Ass. 7.

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er yard 1 er yard 1 Ans. 2++1. at is that Ans. 3£. Ins. 1989 . of 2

Quot. 3\frac{3}{4}.
Quot. \frac{1}{2}\frac{1}{2}.
Quot. \frac{1}{2}\frac{1}{2}.

Quot. 21. Quot. 29.

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an orange
Ass. \(\frac{1}{2}\).

of hay; a
and a pair
how much
the oxen

than the horse 1 25 + 15 15 = how much? 1 - 15 = how much 1

3. 1+4+1= how much ! 1-1= how much !

4. 20+20+20+26+26 how much 1 14 A= how much 1

5. A boy, having \$ of an apple, gave \$ of it to his sister; what part of the apple had he left 1 \$ \frac{1}{2} = how much !

When the denominators of two or more fractions are alike (as in the foregoing examples,) they are said to have a common denominator. The parts are then in the same denomination, and, consequently, of the same magnitude or value. It is evident, therefore, that they may be added or subtracted, by adding or subtracting their numerators, that is, the number of their parts, care being taken to write under the result their proper denominator. Thus, \(\frac{1}{11} + \frac{1}{12} = \frac{1}{12} \);

6. A boy, having an orange, gave ‡ of it to his sister, and ‡ to his brother; what part of the orange did he give awar?

4ths and 8ths, being parts of different magnitudes, or value, cannot be added together. We must therefore first reduce them to parts of the same magnitude, that is, to a common denominator. A are 3 parts. If each of these parts be divided into 2 equal parts, that is, if we multiply both terms of the fraction by 2, (¶ 43,) it will be changed to his and hare h.

7. A man had $\frac{2}{3}$ of a hogshead of melasses in one cask, and $\frac{2}{3}$ of a hogshead in another; how much more in one cask than in the other?

Here, 3ds cannot be so divided as to become 5ths, nor can 5ths be so divided as to become 3ds; but if the 3ds be eath divided into 5 equal parts, and the 5ths each into 3 equal parts, they will all become 15ths. The $\frac{2}{3}$ will become $\frac{1}{15}$, and the $\frac{3}{4}$ will become $\frac{1}{15}$; then, $\frac{9}{15}$ taken from $\frac{1}{15}$ leaves $\frac{1}{15}$, Ans.

T 57. From the very process of dividing each of the parts, that is, of increasing the denominators by multiplying them, it follows, that each denominator must be a factor of the common denominator; now, multiplying all the denominators together will evidently produce such a number.

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Hence,-To reduce fractions of different denominators to equivalent fractions, having a common denominator, -RULE: Multiply together all the denominators for a common denominator; and, as by this process each denominator is multiplied by all the others, so, to retain the value of each fraction, multiply each numerator by all the denominators, except its own, for a new numerator, and under it write the common denominator.

EXAMPLES FOR PRACTICE.

1. Reduce 3, 2 and 4 to fractions of equal value, having a common denominator.

 $3\times4\times5=60$, the common denominator.

 $2\times4\times5=40$, the new numerator for the first fraction.

 $3\times3\times5=45$, the new numerator for the second fraction.

 $3\times4\times4=48$, the new numerator for the third fraction.

The new fractions, therefore, are \$9, \$5, and \$8. By an inspection of the operation, the pupil will perceive, that the pemerator and denominator of each fraction have been mulwolled by the same numbers; consequently, (¶ 43,) that their value has not been altered.

3. Reduce to equivalent fractions of a common denominator, and add together, $\frac{1}{2}$, $\frac{3}{5}$, and $\frac{1}{2}$.

Ans. $\frac{20}{60} + \frac{36}{60} + \frac{1}{60} = \frac{7}{60} = 1\frac{1}{60}$, amount.

4. Add together ? and \$. Amount, 117.

5. What is the amount of 1+1+1+1!

Ans. 347-1270.

6. What are the fractions of a common denominator equivalent to # and # ? Ans. 12 and 32, or 12 and 12.

We have already seen, (¶ 56, ex. 7,) that the common denominator may be any number, of which each given denominator is a factor, that is, any number which may be divided by each of them without a remainder. Such a number is called a common multiple of all its common divisors, and the least number that will do this is called their least common multiple; therefore, the least common denominator of any fractions is the least common multiple of all their denominators. Though the rule already given will always find a common multiple of the given denominators, yet it will not always find their least common multiple. In the last example, 24 is evidently a common multiple of 4 and 6, for it will exactly measure both of them; but 12 will do the same, and as 12 is ora to

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the least number that will do this, it is the least common multiple of 4 and 6. It will therefore be convenient to have a rule for finding this least common multiple. Let the numbers be 4 and 6.

It is evident, that one number is a multiple of another, when the former contains all the factors of the latter. The factors of 4 are 2 and 2, $(2\times2=4)$. The factors of 6 are 2 and 3, $(2\times3=6)$. Consequently, $2\times2\times3=12$ contains the factors of 4 that is, 2×2 ; and also contains the factors of 6, that is, 2×3 . 12, then, is a common multiple of 4 and 6 and it is the *least* common multiple, because it does not contain any factor, except those which make up the numbers 4 and 6; nor either of those repeated more than is necessary to produce 4 and 6. Hence it follows, that when any two numbers have a factor common to both, it may be once omitted; thus, 2 is a factor common both to 4 and 6, and is consequently once omitted.

T 58. On this principle is founded the Rule for finding the least common multiple of two or more numbers. Write down the numbers in a line, and divide them by any number that will measure two or more of them; and write the quotients and undivided numbers in a line beneath. Divide this line as before, and so on, until there are no two numbers that can be measured by the same divisor; then the continual product of all the divisors and numbers in the last line will be the least common multiple required.

Let us apply the rule to find the least common multiple of 4 and 6.

2)4 . 6 quotients are 2 and 3. There is no number greater then 1, which will measure 2 and 3. Therefore, $2\times2\times3=12$ is the least common multiple of 4 and 6.

If the pupil examine the process, he will see that the divisor 2 is a factor common to 4 and 6, and that dividing 4 by this factor gives for a quotient its other factor, 2. In the same manner, dividing 6 gives its other factor, 3. Therefore the divisor and quotients make up all the factors of the two numbers, which, multiplied together, must give the common multiple.

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7. Reduce $\frac{3}{4}$, $\frac{1}{2}$, $\frac{2}{3}$ and $\frac{1}{6}$ to equivalent fractions of the least common denominator.

OPERATION 2)4.2.3.6 denominator. It is evident we need 3)2.1.3.3 not multiply by the 1s, as this would not alter the number.

To find the new numerators that is, how many 12ths each fraction is, we may take 2, 1, 3, and 4 of 12. Thus:

$\frac{3}{1}$ of $12-9$ $\frac{1}{2}$ of $12-6$ $\frac{3}{4}$ of $12-8$ $\frac{1}{6}$ of $12-8$ $\frac{1}{6}$ of $12-2$ New numerators, which, written over the common denominators, give $\begin{pmatrix} \frac{1}{12} & \frac{1}{4} & \frac{1}{12} & \frac{1}{4} &$	% of 12-8 (mam denominators give	0 - Carta - 10
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8. Reduce $\frac{1}{2}$, $\frac{3}{8}$, and $\frac{5}{8}$ to fractions having the least common denominator, and add them together.

Ans. $\frac{12}{24} + \frac{2}{24} + \frac{2}{24} = \frac{1}{24} = \frac{1}{24}$, amount. 9. Reduce $\frac{1}{4}$ and $\frac{1}{4}$ to fractions of the least common de-

9. Reduce \(\frac{1}{6} \) and \(\frac{1}{9} \) to fractions of the least common denominator, and subtract one from the other.

10. What is the least number that 3, 5, 8 and 10 will measure?

Ans. $\frac{1}{18} - \frac{2}{18} = \frac{1}{18}$, difference.

11. There are 3 pieces of cloth, one containing 7½ yards, another 13½ yards, and the other 15½ yards; how many yards in the 3 pieces.

Before adding, reduce the fractional parts to their least common denominator; this being done, we shall have,

Adding together all the 24ths, viz. 18+20 $7\frac{1}{4}=7\frac{1}{2}\frac{8}{4}$ $13\frac{1}{6}=13\frac{2}{2}\frac{1}{4}$ We write down the fraction $\frac{1}{2}\frac{1}{4}$ under the other fractions, and reserve the 2 integers to be carried to the amount of the other integers, making in the whole $37\frac{1}{2}\frac{1}{4}$ Ans.

12. There was a piece of cloth containing 344 yards, from which were taken 124 yards; how much was there left!

We cannot take 16 twenty-fourths $34\frac{3}{8} = 34\frac{9}{24}$ ($\frac{16}{24}$) from 9 twenty-fourths, ($\frac{9}{24}$;) we 12 $\frac{2}{3} = 12\frac{16}{24}$ must, therefore, borrow 1 integer, =24 twenty-fourths, ($\frac{3}{24}$,) which, with $\frac{9}{24}$, makes $\frac{3}{24}$; we can now take $\frac{16}{24}$ from $\frac{3}{24}$, and there will remain $\frac{1}{24}$; but, as we borrowed, so also

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nany 12ths 12, Thus:

 $\frac{8}{12}$, and $\frac{2}{12}$. least com-

17, amount. common de-

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and 10 will

Ans. 120.

ng 7½ yards,

how many

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under the 2 integers the other in-

343 yards, was there

enty-fourths as, ($\frac{1}{24}$;) we integer,—24 ch, with $\frac{1}{24}$; from wed, so also

we must carry 1 to the 12, which makes it 13, and 13 from 34 leaves 21.

Ans. 2117.

13. What is the amount of 1 of 2 of a yard, 2 of a yard,

and 1 of 2 yards 1

Note. The compound fraction may be reduced to a simple fraction; thus, $\frac{1}{2}$ of $\frac{3}{4} = \frac{3}{4}$; and $\frac{1}{4}$ of $2 = \frac{2}{4}$; then, $\frac{3}{4} + \frac{3}{4} + \frac$

 $\frac{2}{4} + \frac{2}{5} = \frac{173}{120} = 1\frac{53}{120}$ yds., enswer.

¶ 59. From the foregoing examples we derive the following Rule:—To add or subtract fractions, add or subtract their numerators, when they have a common donominator; otherwise, they must first be reduced to a common denominator.

Note. Compound fractions must be reduced to simple

fractions before adding or subtracting.

EXAMPLES FOR PRACTICE.

1. What is the amount of \$, 43 and 12! Ans. 1711.

2. A man bought a farm, and sold \(\frac{2}{4} \) of \(\frac{1}{2} \) of it; what part of the farm had be left?

Ana. \(\frac{2}{4} \)

3. Add together 1, 1, 1, 70, 1 and 11 1 Amount. 28

4. What is the difference between 14. and 16.7.

Ans. 148.

Rem. 370.

5. From 1½ take 2... 6. From 3 take 4. Remainder, 3.
Remainder, 24.

7, From 1471 take 484.

Rem. 98 8.

8. From $\frac{1}{4}$ of $\frac{4}{10}$ take $\frac{1}{2}$ of $\frac{2}{4}$.
9. Add together 112 $\frac{1}{2}$, 311 $\frac{2}{3}$, and 1000 $\frac{3}{4}$.

9. Add together 1123, 3113, and 1000 $\frac{1}{4}$. 10. Add together 14, 11, $\frac{4}{3}$, $\frac{1}{18}$ and $\frac{1}{2}$.

11. From 3 take 1. From 3 take 3.

12. What is the difference between 1 and 1? 3 and 1? 1 and 2? 4 and 2? 4 and 2?

13. How much is 1-11 1-11 1-11 1-1 2-3?

2-4! 21-3! 34-10! 1000-14!

REDUCTION OF FRACTIONS.

T 60. We have seen (7 27,) that integers of one denomination may be reduced to integers of another denomination. It is evident, that fractions of one denomination, after the same manner, and by the same rules, may be reduced to fractions of another denomination; that is, fractions, like integers, may be brought into lower denomina-

tions by multiplication, and into higher deflominations by division.

To reduce higher into LOWER To reduce lower into HIGHER denominations.

(RULE, See ¶ 28.)

1. Reduce 2 to of a pound 2. Reduce \$ of a penny to to pence, or the fraction of a the fraction of a pound.

penny.

Note. that a fraction is multiplied ei-merator, or by multiplying the ther by dividing its denomin-denominator. ator, or by multiplying its nu- f d. \div 12 = 14 s. \div 20 =erator.

280£. $\times 20 = \frac{1}{14}$ b. $\times 12 = \frac{1}{14}$ 4 d. Ans.

Or thus: 240 of 40 of 4= 348-9 of a penny, Ans.

to the fraction of a farthing 1 to the fraction of a pound.

 $=\frac{240}{280}$ d. $\times 4=\frac{960}{1280}=\frac{3}{4}$ q. Or thus:

Num. 1

20 s. in 1 £.

12 d. in 1 s.

240

4 q. in 1 d.

960

P Later

ea to the fraction of a penny, the fraction of a guinea.

the fraction of a pound.

Consult ¶ 28, ex. 12. at 1£. 10s. to the fraction of to the fraction of a moidore.

11. Reduce & of a pound, 12. Reduce # of an ounce Truy, to the fraction of anto the fraction of a pound

ounce.

denominations.

(RULE, See ¶ 28.)

Note. Division is perform-Let it be recollecteded either by dividing the nu-

Ans.

Or thus: $\frac{6}{7}$ of $\frac{1}{12}$ of $\frac{1}{20}$ 1680 280£. Ans.

Reduce 1280 of a pound 4. Reduce 4 of a farthing

 $7280£. \times 20 = 7280 s. \times 12$ } q. $4 = 78d. \div 12 = 729s.$ -20=3840=1280£.

Or thus :

Denom. 4

4 q. in 1 d.

16

12 d. in I s.

192

20 s. in 1 £.

3840

Then, $\frac{960}{1280} = \frac{3}{4}$ q. Ans. Then $\frac{3}{3840} = \frac{2}{1280} \pounds$. Ans. 5. Reduce $\frac{3}{2688}$ of a guin- 6. Reduce $\frac{3}{8}$ of a penny to

7. Reduce 4 of a guinea to 8. Reduce 4 of a pound to the fraction of a guinea.

9. Reduce 3 of a moidore, 10. Reduce 34 of a guinea

Trov.

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 $- \div 20 =$

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a farthing pound. 12-13-8. £.

Bot. Ans. penny to inea. pound to inea. 3 24 7 1

f a guinea moidore.

an ounce a pound

13. Reduce 1 of a pound, 14. Reduce 4 of an ounce avoirdupois, to the fraction of to the fraction of a pound avoirdupois. an ounce. .:

15. A man has 728 of a 16. A man has 18 of a pint hogshead of wine; what part of wine; what part is that of

is that of a pint? a hogshead?

17. A cucumber grew to the 18. A cucumber grew, to part is that of a foot 1

length of 32 kg of a mile; what the length of I foot 4 inches -18-4 of a foot; what part is that of a mile ?

19. Reduce of of a of a 20. 39 of a shilling is a of pound to the fraction of a shil-what fraction of a pound? ling.

21. Reduce 1 of 2 of 3 22, 40 of a penny is 1 of pounds to the fraction of a what fraction of 3 pounds ! penny. 180 of a penny, is 2 of what part of 3 pounds ? 149 of a penny is 1 of 2 of how many pounds ?

T 61. It will frequently It will frequently be requirbe required to find the value of ed to reduce integers to the a fraction, that is to reduce a fraction of a greater denominfraction to integers of less de-ation, and state as a per to the nominations, appoint is what tracion second ever v.

1. What is the value of 3 . 2. Reduce 13 a. 4 d. to the of a pound ? In other words fraction of a pound.

Reduce 4 of a pound to shil- 13s. 4d. is 160 pence; there

2 of a £ is 40 = 131 shil therefore, 13e, 4d. is 168=2 lings; it is evident from 4 of of a pound. That is, - Rea shilling may be obtained duce the given sum or quansome pence; 1 of a shilling istity to the least denomination 2=4d. That is, Multiply mentioned in it, for a numerthe numerator by that num-ator; then reduce an integer ber which will reduce it toof that greater denomination the next less denomination, to a fraction of which it is and divide the product by the required to reduce the given denominator; if there be a re-sum or quantity) to the same mainder, multiply and divide denomination, for a denomias before, and so on; the sev-nator, and they will form the eral quotients, placed one af-fraction required and W ter another, in their order, willing 111 gloon & south I II be the answer.

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EXAMPLES FOR PRACTICE.

3. What is the value of # of a shilling ! fr	4. Reduce 4d. 2q. to the raction of a shilling. OPERATION.
Numer. 8 Kill name to the 12 house and	4 d. 2q. 1 s.
Denom.8)36(4d. 2q. Ans.	18 Numer. 12
A still to the still sti	48 Denom.
16(2q. 1675)	ede via far. #= Ans.

5. What is the value of ? of a pound Troy ?

7. What is the value of 4 of a pound avoirdupois ?

6. Reduce 7 oz. 4 pwt. to the fraction of a pound Troy.

8. Reduce 8 oz. 142 dr. to the fraction of a pound avoirdupois.

Note. Both the numerator and the denominator must be reduced to 9ths of a dr.

9. 4 of a month is how many days, hours, and minutes is what fraction of a month?

11. Reduce 4 of a mile to its proper quantity.

10. 3 weeks, 1d. 9h. 36m. 12. Reduce 4 fur. 125 yds.

2ft. I in. 24 bar, to the fraction of a mile.

13. Reduce To of un acre to its proper quantity. to the fraction of an acre.

15. What is the value of 16. Reduce 4s. 81d. to the 14 of a dollar in shillings, fraction of a dollar. pence, &c. 1

14. Reduce 1 rood 30 poles

of a yard !

of a ton.

17. What is the value of 10 18. Reduce 2 ft. 8 in. 11b. to the fraction of a yard.

19. What is the value of 20. Reduce 4 cwt. 2gr. 12 lb. 14 oz. 12- dr. to the fraction of a ton.

Note. Let the pupil be required to reverse and prove the following examples:

21. What is the value of a guinea?

22. Reduce 3 roods 174 poles to the fraction of an acre.

Т 61.

2q. to the

g.

1 s. 2

4

8 Denom.

Ans.

4 pwt. to and Troy.
14g dr.
pound a-

numerator r must be i dr.

9h. 36m. a month? 125 yds. the frac-

30 poles acre. d. to the

in. 14b. ard. 2qr. 12 the frac-

rove the

n acre.

23. A man bought 27 gal. 3 qts. 1 pt. of molasses; what part is that of a hogshead?

24. A man purchased 5 of 7 cwt. of sugar; how much

sugar did he purchase !

25. 13h. 42m. 514s. is what part or fraction of a day ?

SUPPLEMENT TO FRACTIONS.

1. What are fractions? 2. Whence is it that the parts into which any thing or any number may be divided, take their name? 3. How are fractions represented by figures? 4. What is the number above the line called? — Why is it so called? 5. What is the number below the line called? - Why is it so called? - What does it show? 6. What is it which determines the magnitude of the parts? - Why? 7. What is a simple or proper fraction? — an improper fraction — a mixed number? 8. How is an improper fraction reduced to a whole or mixed number? 9. How is a mixed number reduced to an improper fraction? — a whole number? 10. What is understood by the terms of the fraction? 11. How is a fraction reduced to its most simple or lowest terms? 12. What is understood by a common divisor? by the greatest common divisor? 13. How is it found? 14. How many ways are there to multiply a fraction by a whole number? 15. How does it appear, that dividing the denominator multiplies the fraction? 16. How is a mixed number multiplied? 17. What is implied in multiplying by a fraction? 18. Of how many operations does it consist? - What are they? 19. When the multiplier is less than a unit, what is the product compared with the multiplicand? 20. How do you multiply a whole number by a fraction? 21. How do you multiply one fraction by another? 22. How do you multiply a mixed number? 23. How does it appear, that in multiplying both terms of the fraction by the same number the value of the fraction is not altered? 24. How many ways are there to divide a fraction by a whole number? - What are they? 25. How does it appear that a fraction is divided by multiplying its denominator? 26. How does dividing by a fraction differ from multiplying by a fraction: 27. When the divisor is less than a unit, what is the quotient compared with the dividend? 28. What is understood by a common denominator? ——— the least common denominator? 20. How does it appear, that each given denomination must be a factor of the common denominator? 30. How is the common denominator to two or more fractions found? 31. What is understood by a multiple? - by a common multiple? — by the least common multiple? — What is the process of finding it? 32. How are fractions added and subtracted? 33. How is a fraction of a greater denomination reduced to one of a less? - of a less to a greater? 34. How are fractions of a greater denomination reduced to integers of a less? ---- integers of a less denomination to the fraction of a greater? L 2

EXERCISES.

1. What is the amount of \(\frac{1}{2} \) and \(\frac{1}{2} \)? — of 12\(\frac{1}{2} \), 3\(\frac{1}{2} \) and 4\(\frac{1}{2} \)? — Ans. to the last, 20\(\frac{1}{2} \).

2. To $\frac{7}{4}$ of a pound add $\frac{3}{4}$ of a shilling. Amount, 184s. Note. First reduce both to the same denomination.

3. § of a day added to § of an hour, make how many hours? — what part of a day? Ans. to the last, § § d.

4. Add 1 lb. Troy to Ta of an oz.

Amount, 6 oz. 11 pwt. 16 gr.

5. How much is 1 less 17 199-1 of 3 of 1?

Ans. to the lust, 198.

6. From 1 shilling take 2 of a penny. Rem. 51d.

7. From # of an ounce take # of a pwt.

Rem. 11 pwt. 3 grs.

8. From 4 days 7 hours, take 1 d. 9 h.

Rem. 2 d. 22 h. 20 m.

9. At &£. per yard, what costs ‡ of a yard of cloth !

T 62. The price of unity, or 1, being given, to find the cost of any quantity, either less or more than unity, multiply the price by the quantity. On the other hand, the cost of any quantity, either less or more than unity, being given, to find the price of unity, or 1, divide the cost by the quantity.

Ans. 11£,

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1. If $\frac{1}{13}$ lb. of sugar cost $\frac{7}{15}$ of a shilling, what will $\frac{32}{13}$

of a pound cost?

This example will require two operations: first, as above, to find the price of 1 lb.; secondly, having found the price of 1 lb. to find the cost of $\frac{32}{4}$ of a pound. $\frac{7}{15}s. \div \frac{11}{13}$ ($\frac{13}{13}$ of $\frac{7}{15}s. \mp 54$)= $\frac{91}{165}s.$ the price of 1 lb. Then, $\frac{91}{165}s. \times \frac{32}{43}$ ($\frac{32}{13}$ of $\frac{91}{165}s. \mp \frac{13}{165}s. \pm \frac{32}{165}s. \pm \frac{34}{165}s. \pm \frac{34$

Or we may reason thus: first to find the price of 1 lb: $\frac{11}{13}$ lb. costs $\frac{7}{15}$ s. If we knew what $\frac{1}{13}$ lb. would cost, we might repeat this 13 times, and the result would be the price of 1 lb. $\frac{1}{13}$ is 11 parts. If $\frac{1}{13}$ lb. costs $\frac{7}{15}$ s. it is evident $\frac{1}{13}$ lb. will cost $\frac{1}{11}$ of $\frac{7}{16} = \frac{7}{165}$ s. and $\frac{13}{3}$ lb. will cost 13 times as much, that is, $\frac{9}{165}$ s.— the price of 1 lb. Then, $\frac{32}{165}$ of $\frac{21}{165}$ s.— $\frac{2912}{169}$ s. the cost of $\frac{32}{43}$ of a pound. $\frac{29123}{169}$ s.—4 d. $3\frac{4}{9}\frac{915}{16}$ q. as before. This process is called solving the question by analysis.

After the same manner let the pupil solve the following

questions:

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mount, 181s.
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e how many

he last, §§ d.

pwt. 16 gr. § ? the last, }§§.

Rom. 51d.

pwt. 3 grs.

22 h. 20 m. of cloth!

n, to find the unity, multid, the cost of being given, the quantity.

Ans. \frac{1}{2}\mathcal{E}, \text{yhat will }\frac{2}{3}

st, as above, and the price s.: \frac{1}{13} (\frac{1}{13}), \frac{1}{13} \frac{1}{13}, \frac{1}{13} \frac{1}

ould be the 75 s. it is evilb. will cost lb. Then, nd. \$85.5s.

e following

2: If 7 lb. of tobacco cost \$\fo\$ of a pound, what is that a pound 1 \$\fo\$ of \$\fo\$ how much 1 What is it for 4 lb. 1 \$\fo\$ of \$\fo\$ how much 1 What for 12 lb. 1 \$\fo\$ of \$\fo\$ how much 1 Ans. to the last, 1\$\fo\$.

3. If 6½ yds of cloth cost 3£. what cost 9½ yards ?

Ans. 4£. 5s. 41d.

4. If 2 oz. of silver cost 11s. 3d. what costs 4 oz.?

Ans. 4s. 2d. 24 q.

5. If \$ oz. costs 4s. 1d. what costs 1 oz. Ans. 5s. 8ad.

If \(\frac{1}{3} \) lb. less by \(\frac{1}{6} \) costs 13\(\frac{1}{6} \) d. what costs 14 lb. less by \(\frac{1}{6} \) of 2 lb.?
 Ans. 4\(\mathcal{L} \). 9s. 9\(\frac{3}{5}\(\frac{1}{6} \) d.

7. If 3 yd cost 7£., what will 401 yds. cost.

Ans. 59£. 1s. 23d.

8. If 15 of a ship costs 251£. what is 32 of her worth?

Ans. 53£. 15s. 84d.

9. At 3a£. per cwt. what will 93 lb. cost 1

10. A merchant, owning 4 of a vessel, sold 3 of his share for 39£. 5s. what was the vessel worth?

Ans. 448£. 11s. 103

11. If § yds. cost \$£. what will \$\frac{9}{15}\$ of an ell Eng. cost.

Ans. 17s. 1d. 2\$q.

12. A merchant bought a number of bales of cloth, each containing 129\frac{1}{4}\text{ yards, at the rate of }7\mathcal{L}\text{ for 5 yards, and sold them out at the rate of }11\mathcal{L}\text{ for 7 yards, and gained }200\mathcal{L}\text{ by the bargain; how many bales were there?}

First find for what he sold 5 yards; then what he gained on 5 yards—what he gained on 1 yard. Then, as many times as the sum gained on 1 yd. is contained in 200£, so many yards there must have been. Having found the number of yards reduce them to bales.

Ans. 9 bales.

13. If a staff, 5\(^2\) ft. in length, cast a shadow of 6 ft. how high is that steeple whose shadow measures 153 feet?

Ano. 1444 feet.

14. If 16 men finish a piece of work in 28\frac{1}{3} days, how long will it take 12 men to do the same work?

First find how long it would take 1 man to do it; then 12 men will do it in to of that time.

Ans. 377 days.

15. How many pieces of merchandise, at 201s. apiece, must be given for 240 pieces, at 121s. apiece? Ans. 14915.

16. How many yards of bocking that is 1-yd. wide will be sufficient to line 20 yds. of camlet that is 2 of a yard wide?

First find the contents of the camlet in square measure; then it will be easy to find how many yards in length of bocking that is 14 yd. wide it will take to make the same quantity.

Ans. 12 yards of camlet.

17. If 1\(\frac{1}{4}\) yd. in breadth require 20\(\frac{1}{2}\) yds. in length to make a clouk, what in length that is \(\frac{1}{4}\) yd. wide will be required to make the same !

\[\Lambda_{ns}\) 34\(\frac{1}{4}\) yds.

18. If 7 horses consume 2\(\frac{3}{4} \) tons of hay in 6 weeks, how

many tons will 12 horses consume in 8 weeks ?

If we knew how much 1 horse consumed in 1 week, it would be easy to find how much 12 horses would consume in 8 weeks.

 $2\frac{3}{4} = \frac{1}{4}$ tons. If 7 horses consume $\frac{1}{4}$ tons in 6 weeks, 1 horse will consume $\frac{1}{4}$ of $\frac{1}{4} = \frac{1}{2\frac{1}{8}}$ of a ton in 6 weeks; and if a horse consume $\frac{1}{2\frac{1}{8}}$ of a ton in 6 weeks, he will consume $\frac{1}{6}$ of $\frac{1}{2\frac{1}{8}} = \frac{1}{16\frac{1}{8}}$ of a ton in 1 week. 12 horses will consume 12 times $\frac{1}{16\frac{1}{8}} = \frac{1}{36\frac{1}{8}}$ in 1 week, and in 8 weeks they will consume 8 times $\frac{1}{16\frac{1}{8}} = \frac{1}{16\frac{1}{8}} = \frac{1}{16\frac{1}{8}} = 6\frac{1}{4}$ tons, answer.

19. A man with his family, which in all were 5 persons, did usually drink 74 gallons of cider in 1 week; how much will they drink in 221 weeks when 3 persons more are added to the family?

Ans. 2804 gallons.

20. If 9 students spend 107£ in 18 days, how much will 20 students spend in 30 days?

Ans. 39£ 18s. 424d.

DECUMAL FRACTIOFS.

163. We have seen, that an individual thing or number may be divided into any number of equal parts, and that these parts will be called halves, thirds, fourths, fifths, sixths, &c., according to the number of parts into which the thing or number may be divided; and that each of these parts may be again divided into any other number of equal parts, and so on. Such are called common or vulgar fractions. Their denominators are not uniform, but vary with every varying division of a unit. It is this circumstance which occasions the chief difficulty in the operations to be performed on them; for when numbers are divided into different kinds or parts, they cannot be so easily compared. This difficulty led to the invention of decimal fractions, in which an individual thing, or number, is supposed to be divided first into ten equal parts,

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ning or numarts, and that fifths, sixths, ich the thing se parts may parts, and so Their denomying division ons the chief n them; for r parts, they ed to the inual thing, or equal parts, which will be tenths; and each of these parts to be again divided into ten other equal parts, which will be hundredths; and each of these parts to be still further divided into ten other equal parts, which will be thousandths; and so on. Such are called decimal fractions, (from the Latin word decem, which signifies ten,) because they increase and decrease, in a tenfold proportion, in the same manner as whole numbers.

T64. In this way of dividing a unit, it is evident, that the denominator to a decimal fraction will always be 10, 100, 1000, or 1 with a number of ciphers annexed; consequently, the denominator to a decimal fraction need not be expressed, for the numerator only, written with a point before it (') called the separatrix, is sufficient of itself to express the true value. Thus,

† are written '6.

The denominator to a decimal fraction, although not expressed, is always understood, and is 1 with as many ciphers annexed as there are places in the numerator. Thus, 3765 is a decimal consisting of four places; consequently, I with four ciphers annexed (10000) is its proper denominator. Any decimal may be expressed in the form of a common fraction by writing under it its proper denominator. Thus, 3765 expressed in the form of a common fraction, is $\frac{3760}{10000}$.

When whole numbers and decimals are expressed together, in the same number, it is called a mixed number. Thus, 25'63 is a mixed number, 25', or all the figures on the left hand of the decimal point, being whole numbers, and '63, or all the figures on the right hand of the decimal point, being decimals.

The names of the places to ten-millionths, and, generally, how to read or write decimal fractions, may be seen from

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TABLE.

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Whole	3d place. 2d place, 1st place.	634	= 2 5	= 7	1 0		11		1	Hundreds. Tens. Units.	3.
	1st place. 2d place. 3d place. 4th place. 5th place.	•	•	•	•		*	•	•	Tenths.	
` \	1st place.	0	0	0	00	0	0	0	U	Mandandth a	j
2 1	2d place.	-	2	0	6	00	CR	O		Hundredths.	1
<u>∓</u> .	3d place.	-		-	-	Ch	-			Thousanths.	,
8	4th place	•		_	-	-	_			Ten-Thousant	hs.
= 4	4th place.)	0	0	40	1				
70	5th place.	0	,	0	20					Hundred-Thous	andths.
Parts.	6th place.	-		9						Millionths.	
Ş.	7th place.	0	,							Ten-Millionth	8.

5 Hundredths.
50 Thousandths.
6853 Ten-Thousandths.
68602 Hundred-Thousand
7 and 9 Millionths.
25 and 63 Hundredths.
634.

From the table it appears, that the first figure on the right hand of the decimal point signifies so many tenth parts of a unit; the second figure, so many hundredth parts of a unit; the third figure, so many thousandth parts of a unit, &c. It takes 10 thousandths to make 1 hundredth, 10 hundredths to make 1 tenth, and 10 tenths to make 1 unit, in the same manner as it takes 10 units to make 1 ten, 10 tens to make 1 hundred, &c. Consequently, we may regard unity as a starting point, from whence whole numbers proceed, continually increasing in a tenfold proportion towards the left

hand, and decimals continually decreasing, in the same proportion, towards the right hand. But as decimals decrease towards the right hand, it follows of course, that they increase towards the left hand, in the same manner as whole numbers.

¶ 65. The value of every figure is determined by its place from units. Consequently, eithers placed at the right hand of decimals do not alter their value, since every significant figure continues to possess the same place from unity. Thus, '5, '50, '500 are all of the same value, each being equal to $\frac{1}{2}$ a, or $\frac{1}{2}$.

But every cipher, placed at the left hand of decimal fractions, diminishes them tenfold, by removing the significant figures further from unity, and consequently making each part ten times as small. Thus, '5, '05, '005, are of different value, '5 being equal to \(\frac{1}{10}\), or \(\frac{1}{2}\); '05 being equal to \(\frac{1}{10}\).

or 20; and '005 being equal to Toon, or 200.

Decimal fractions, having different denominators, are readily reduced to a common denominator, by annexing ciphers until they are equal in number of places. Thus, '5, '06, '234 may be reduced to '500, '060, '234, each of which has 1000 for common denominator.

¶ 66. Decimals are read in the same manner as whole numbers, giving the name of the lowest denomination, or right hand figure, to the whole. Thus, '6853 (the lowest denomination, or right hand figure, being ten-thousandths) is read, 6853 ten-thousandths.

Any whole number may evidently be reduced to decimal parts, that is, to tenths, hundredths, thousandths, &c. by annexing ciphers. Thus, 25 is 250 tenths, 2500 hundredthe, 25000 thousandths, &c. Consequently, any mixed number may be read together giving it the name of the lowest denomination or right hand figure. Thus, 25'63 may be read 2563 hundredths, and the whole may be expressed in the form of a common fraction, thus, 25'53.

The denominations in FEDERAL MORRY are made to correspond to the decimal divisions of a unit now described, dollars being units, or whole numbers, dimes tenths, cents hundredths, and mills thousandths of a dollar; consequently, the

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ure on the right tenth parts of a parts of a unit; f a unit, &c. It

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expression of any sum in dollars, cents, and mills, is simply the expression of a mixed number in decimal fractions.

Forty-six and seven tenths 467-467.

Write the following numbers in the same manner:

Eighteen and thirty-four hundredths.

Fifty-two and six hundredths.

Nineteen and four hundred eighty-seven thousandths.

Twenty and forty-two thousandths.

One and five thousandths.

135 and 3784 ten-thousandths.

9000 and 342 ten-thousandths.

10000 and 15 ten-thousandths.

974 and 102 millionths.

320 and 3 tenths, 4 hundreths and 2 thousandths.

500 and 5 hundred-thousandths.

47 millionths.

Four hundred and twenty-three thousandths.

ADDITION AND SUBTRACTION OF DECIMAL FRACTIONS.

To. As the value of the parts in decimal fractions increases in the same proportion as units, tens, hundreds, &c. and may be read together, in the same manner as whole numbers, so, it is evident that all the operations on decimal fractions may be performed in the same manner as on whole numbers. The only difficulty, if any, that can arise, must be in finding where to place the decimal point in the result. This, in addition and subtraction, is determined by the same rule; consequently, they may be exhibited together.

1. A man bought a barrel of flour for \$9, a firkin of butter for \$3.50, 7 pounds of sugar for \$35 cents, an ounce of pepper for 6 cents; what did he give for the whole?

Fote. See the table of Federal Money, 7 27. Let the pupil go back now and read carefully all that is said respecting federal money, in Reduction. From what is there stated it is plain, that we may readily reduce any sums in federal money to the same denominations, as to cents or mills,

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DECIMAL

fractions innundreds, &c. er as whole ns on decimal r as on whole n arise, must in the result. d by the same gether.

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77. Let the said respectis there stated me in federal ats or mills, and add or subtract them as simple numbers. Or, what is the same thing, we may set down the sums, taking care to write dollars under dollars, cents under cents, and mills under mills, in such order, that the separating points of the several numbers shall fall directly under each other, and add them as simple numbers, placing the separatrix in the amount directly under the other points.

OPERATION.

 $$8^\circ$ = 8000 mills, or 1000ths of a dollar

06 = 60 mills, or 1000 ths.

Ans. \$12.395 = 12395 mills, or 1000ths.

As the denominations of federal money correspond with the parts of decimal fractions, so the rules for adding and subtracting decimals are exactly the same as for the same operations in federal money.

2. A man owing \$375, paid \$175'75; how much did

he then owe?

OPERATION.

\$375' = 37500 cents, or 100ths of a dollar. 175'75 = 17575 cents, or 100ths of a dollar.

8199.25 = 19925 cents, or 100ths.

Wherefore,—In the addition and subtraction of decimai fractions,—RULE: Write the numbers under each other, tenths under tenths, hundredths under hundredths, according to the value of their places, and point off in the results as many places for decimals as are equal to the greatest number of decimal places in any of the given numbers.

EXAMPLES FOR PRACTICE.

3. Bought 1 barrel of flour for 6 dollars 75 cents, 10 lb. of coffee for 2 dollars 30 cents, 7 lb, of sugar for 92 cents, 1 lb. of raisins for 12½ cents; and 2 oranges, for 6 cents; what was the whole amount?

Ans. \$10.155

4. A man is indebted to A, \$237'62; to B, \$350; to C, \$86'12\frac{1}{2} cents; to D, \$9'62\frac{1}{2}, and to E, \$0'834; what is the amount of his debts !

Ans. \$684'204.

5. A man has three notes specifying the following sums, viz. three hundred dollars, fifty dollars sixty cents, and

nine dollars eight cents; what is the amount of the three notes?

Ans. \$359.68.

6. A man gave 4 dollars 75 cents for a pair of boots, and 2 dollars 12½ cents for a pair of shoes; how much did the boots cost more than the shoes?

OPERATION. 4750 mills. or, \$4'75 arg 2125 mills. \$2'125

2625 mills = \$2.625 Ans. \$2.625 Ans.

7. A man bought a cow for eighteen dollars, and sold her again for twenty-one dollars thirty-seven and a half cents; how much did he gain?

Ans. \$3'375.

8. A man bought a horse for 82 dollars, and sold him again for seventy-nine dollars seventy-five cents; did he

gain or lose? and how much?

9. A man sold wheat at several times as follows, viz. 13°25 bushels: 8'4 bushels; 23,051 bushels; 6 bushels, and '75 of a bushel; how much did he sell in the whole?

Ans. 51'451 bushels.

10. What is the amount of 429, $21\frac{37}{100}$, 355, 100 and 170?

Ans. $808\frac{1}{1000}$, or $808^{\circ}143$.

11. What is the amount of 2 tenths, 80 hundredths, 89 thousandths, 6 thousandths, 9 tenths, and 5 thousandths?

12. What is the amount of three hundred twenty-nine, and seven tenths; thirty-seven and one hundred sixty-two thousandths, and sixteen hundreths?

13. A man, owing \$4316, paid \$376'865; how much did he then owe?

Ans. \$3939'135.

14. From thirty-five thousand take thirty-five thousandths.

Ans. \$34999.965.

15. From 5'83 take 4'2793. Ans. 1'5507.

16. From 480 take 245'0075.

Ans. 234'9925.

What is, the difference between 1702'12 and 217'

17. What is the difference between 1793'13 and 817' 05693!

Ans 976,07307.

18. From 418 take 210 - Remainder, 198, or 198.

19. What is the amount of 29_{10}^{3} , $374_{1000000}$, 97_{1000}^{263} , 315_{1000}^{4} , 27, and 100_{10}^{4} ?

Ans. $942^{\circ}957009$.

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5 Ans.

and sold her half cents : ns. 83'375. d sold him its; did he

ollows, viz. ; 6 bushels, the whole? 451 bushels. , 1000, 1700 or 808'143. ndredths, 89 ousandths ?

Ans. 2. twenty-nine, ed sixty-two

; how much \$3939 135. y-five thou-\$34999 965. Ans. 1'5507. s. 234 9925. 13 and 817 s 976.07307. 98, or 1.98. 942·957009.

MULTIPLICATION OF DECIMAL FRACTIONS

7 68. 1. How much hay in 7 loads, each containing 23:571 cwt 1.

OPERATION.

 $23^{\circ}571 \text{ cwt.} = 23571 1000 \text{ ths of a cwt.}$

Ans. 164,997 cwt. = 164997 1000ths of a cwt.

We may here (¶ 66) consider the multiplicand so many thousandths of a cwt., and then the product will evidently be thousandths, and will be reduced to a mixed or whole number by pointing off 3 figures, that is, the same number as are in the multiplicand; and as either factor may be made the multiplier, so, if the decimals had been in the multiplier, the same number of places must have been pointed off for decimais. Hence it follows, we must always point off in the product as many places for decimals as there are decimals places in both factors.

2. Multiply 75 by 25.

OPERATION.

475 25 375

150

In this example, we have 4 decimal places in both factors: we must therefore point off 4 places for decimals in the product. The reason of pointing off this number may appear still more plain, if we consider the two factors as

1875 Product. common or vulgar fractions. Thus, '75 is 70 and '25 is $\frac{25}{100}$: now, $\frac{75}{100} \times \frac{25}{100} = \frac{1875}{10000} = 1875$, Ans. same as be fore.

3. Multiply '125 by '03.

OPERATION.

125

Here, as the number of significant 403

figures in the product is not equal to the number of decimals in both fac-'00375 Product. tors, the deficiency must be supplied by prefixing ciphers, that is, placing them at the left hand.

The correctness of the rule may appear from the following process: 125 is 1000, and 03 is 100: now, 1000 × 100 1376 00375, the same as before.

These examples will be sufficient to establish the following

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RULE.

In the multiplication of decimal fractions, multiply as in whole numbers, and from the product point off so many figures for decimals as there are decimal places in the multiplicand and multiplier counted together, and, if there are not so many figures in the product, supply the deficiency by prefixing ciphers.

As the denominations of federal money correspond with the parts of decimal fractions; the rules for the multiplication and division of both are the same.

EXAMPLES FOR PRACTICE.

- 4. At \$5'47 per yard, what cost 8'3 yards of cloth?

 Ans. \$45'401.
- 5. At \$'07 per pound, what cost 26'5 pounds of rice?
- 6. If a barrel contain 1.75 cwt. of flour, what will be the weight of 63 of a barrel?

 Ans. 1.1025 cwt.
 - 7. If a melon be worth \$'00, what is '7 of a melon worth?

 Ans. 6-3 cents.
 - 8. Multiply five hundredths by seven thousandths.
 - Product, '00035.
 - 9. What is '3 of 116? Ans. 34'8.
 - 10. What is '85 of 3672?

 Ans. 3121'2.

 Ans. '020831.
 - 12. Multiply 572 by '58. Product, 331'76.
 - 13. Multiply eighty-six by four hundredths.
 - Product, 3'44.
 - 14. Multiply '2062 by '0008.
- 15. Multiply forty-seven tenths by one thousand eighty-six hundredths.
 - 16. Multiply two hundredths by eleven thousandths.
- 17. What will be the cost of thirteen hundredths of a ton of hay, at \$11 a ton?
- 18. What will be the cost of three hundred seventy-five thousandths of a cord of wood at \$2 a cord?
- 19. If a man's wages be seventy-five hundredths of a dollar a day, how much will he earn in 4 weeks, Sundays excepted?
- 20. What will 250 burnels of rye come to, at \$0.881 per bushel !

 Ans. \$221.25.
- 21. What is the value of 87 barrels of flour, at \$6'371 a

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22. What will be the cost of a hogshead of molasses, containing 63 gallons, at 28½ cents a gallon? Ans. 617 955.

23. If a man spend 12½ cents a day, what will that amount to in a year of 365 days? what will it amount to in 5 years?

Ans, \$228.12½ in 5 years.

DIVISION OF DECIMAL FRACTIONS.

¶ 69. Multiplication is proved by division. We have seen, in multiplication, that the decimal places in the product must always be equal to the number of decimal places in the multiplicand and multiplier counted together. The multiplicand and multiplier, in proving multiplication, become the divisor and quotient in division. It follows of course, in division, that the number of decimal places in the divisor and quotient, counted together, must always be equal to the number of decimal places in the dividend. This will still further appear from the examples and illustrations which follow:

1. If 6 barrels of flour cost \$44'718, what is that a bar rel?

By taking away the decimal point, \$44.718 = 44718 mills, or 1000ths, which, divided by 6, the quotient is 7453 mills, = \$7.453, the answer.

Or, retaining the decimal point, divide as in whole numbers?

OPERATION.
6)44'718

Ans. 7'453

As the decimal places in the dividend, counted together, must be equal to the number of decimal places in the dividend,

there being no decimals in the divisor,—therefore point off three figures for decimals in the quotient, equal to the number of decimals in the dividend, which brings us to the same result as before.

2. At \$4.75 a barrel for cider, how many barrels may be bought for \$31?

In this example, there are decimals in the divisor, and none in the dividend. \$4.75 = 475 cents, and \$31, by annexing two ciphers; = 3100 cents; that is, reduce the dividend to parts of the same denomination as the divisor.

T 00.

f cloth?

18. \$45'401.

19. \$1'855.

19. \$1'855.

19. \$1'1025 cwt.

uct, '00035.
Ans. 34'8.
Ans. 3121'2.
ns. '020831.
luct, 331'76.

roduct, 3'44.

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dredths of a ks, Sundays

\$0'881 per s. \$221'25. t \$6'371 a

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Then; it is plain, as many times as 475 cents are contained in 3100 cents, so many barrels may be bought.

475)3100(6244 barrels the answer; that is, 6 barrels and 2850 259 of another barrel.

But the remainder, 250, instead of being expressed in the form of a common fraction, may be reduced to 10ths by annexing a cipher, which, in effect, is multiplying it by 10, and the division continued, placing the decimal point after the 6, or whole ones already obtained, to distinguish it from the decimals which are to follow. The points may be withdrawn or not from the divisor and dividend.

OPERATION.

4'75)31'00(6'526+	barrels, the answer, that is, 6 barrels
2850	and 526 thousandths of another bar-
	rel.

	rel.
2500	By annexing a cipher to the first
2375	remainder, thereby reducing it to
*** (\$100.000.0000.000.000	10ths, and continuing the division,
1250	we obtain from it 6, and a still fur-
950	ther remainder of 125, which, by an-
3000	nexing another cipher, is reduced to
2850	100ths, and so on.
7000	The last remainder, 150, is 149 of
150	a thousandth part of a barrel, which

is of so trifling a value, as not to merit notice.

If now we count the decimals of the dividend, (for every cipher annexed to the remainder is evidently to be counted a decimal of the dividend,) we shall find them to be five, which corresponds with the number of decimal places in the divisor and quotient counted together.

3. Under ¶68, ex. 3, it was required to multiply 125 by 03; the product was 00375. Taking this product for a dividend, let it be required to divide 00375 by 125. One operation will prove the other. Knowing that the number of decimal places in the quotient and divisor, counted together, will be equal to the decimal places in the dividend, we may divide as in whole numbers, being careful to retain the decimal points in their proper places. Thus,

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6 barrels and

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er to the first educing it to the division, and a still furwhich, by an-, is reduced to

150, is 150 of barrel, which

nd, (for every to be counted in to be five, imal places in

product for a by '125. One at the number or, counted ton the dividend, areful to retain Thus,

OPERATION. '125)'00375('03 375

375 000 The divisor, 125, in 375 goes 3 times and no remainder. We have only to place the decimal point in the quotient, and the work is done.

There are five decimal places in the dividend; consequently there must be five in the divisor and quotient counted together; and, as there are three in the divisor, there must be two in the quotient; and since we have but one figure in the quotient, the deficiency must be supplied by prefixing a cypher.

The operation by vulgar fractions will bring us to the same result. Thus, '125 is $\frac{125}{1000}$, and '00375 is $\frac{375}{1000000}$: now, $\frac{375}{1000000} \div \frac{125}{1000} = \frac{3750000}{125000000} = \frac{3}{100000} = \frac{3}{1000000}$ the same as

before.

¶ 70. The foregoing examples and remarks are sufficient to establish the following

RULE.

In the division of decimal fractions, divide as in whole numbers, and from the right hand of the quotient point off as many figures for decimals, as the decimal figures in the dividend exceed those in the divisor, and if there are not so many figures in the quotient, supply the deficiency by prefixing ciphers.

If at any time there is a remainder, or if the decimal figures in the divisor exceed those in the dividend, ciphers may be annexed to the dividend or the remainder, and the quotient carried to any necessary degree of exactness; but the ciphers annexed must be counted so many decimals of

the dividend.

EXAMPLES FOR PRACTICE.

4. If \$472.875 be divided equally between 13 men, how much will each one receive?

Ans. \$36.375.

5. At \$'75 per bushel, how many bushels of rye can be bought for \$141?

Ans. 188 bushels.

6. At 61 cents apiece, how many oranges may be bought for \$8?

Ans. 128 oranges.

7. If '6 of a harrel of flour cost \$5, what is that per barrel 1 Ans. 8'333+

8. Divide 2 by 53'1.

Quot. '037+

9. Divide '012 by '005. Quot. 2'4.

11. Divide three thousandths by four hundredths.

11. How many times is '17 contained in 8?

12. If I pay \$468.75 for 750 pounds of wool, what is the value of 1 pound?

Ans. \$0.625; or thus \$0.621.

13. If a piece of cloth, measuring 125 yards, cost \$181.25 what is that a yard?

Ans. \$1.45.

14. If 536 quintals of fish cost \$1913.52, how much is that a quintal?

Ans. \$3.57.

15. Bought a farm, containing 84 acres, for \$3213; what did it cost me per acre?

Ans. \$38'25.

16. At \$954 for 3816 yards of flannel, what is that per yard?

Ans. 80°25.

REDUCTION OF COMMON OR VULGAR FRAC-TIONS TO DECIMALS.

¶ 71. 1. A man has \$ of a barrel of flour; what is that

expressed in decimal parts ?

As many times as the denominator of a fraction is contained in the numerator, so many whole ones are contained in the fraction. We can obtain no whole ones in \$\frac{1}{2}\$, because the denominator is not contained in the numerator. We may, however, reduce the numerator to tenths, (¶69, ex. 2.) by annexing a cipher to it, (which, in effect, is multiplying it by 10,) making 40 tenths, or 4°0. Then, as many times as the denominator, 5, is contained in 40, so many tenths are contained in the fraction. 5 into 40 goes 8 times, and no remainder.

Ans. '8 of a bushel.

2. Express 4 of a dollar in decimal parts.

The numerator, 3, reduced to tenths, is $\frac{10}{10}$, 3°0, which, divided by the denominator, 4, the quotient is 7 tenths, and a remainder of 2. This remainder must now be reduced to hundredths by annexing another cipher, making 20 hundredths. Then, as many times as the denominator 4, is contained in 20, so many hundredths also may be obtained. 4 into 20 goes 5 times, and no remainder. $\frac{3}{4}$ of a dollar, therefore, reduced to decimals, is 7 tenths and 5 hundredths, that is, °75 of a dollar.

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Quot. 4075.

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Quot. 24.

Quot. '075.

col, what is thus \$0.62\frac{1}{25}. cost \$181.25
Ans. \$1.45. ow much is Ans. \$3.57. column \$38.25. at is that per Ans. \$0.25.

R FRAC-

what is that

n is containcontained in n ½, because erator. We \$69, ex. 2.) multiplying many times many tenths times, and of a bushel.

3'0, which, tenths, and e reduced to ing 20 hunor 4, is conbtained. 4 of a dollar, hundredths,

The operation may be presented in form as follows:--

Num.

Denom. 4)3'0('75 of a dollar, the answer.

28

 $\frac{20}{20}$

3. Reduce $\frac{4}{6.6}$ to a decimal fraction.

The numerator must be reduced to hundredths by annexing two ciphers, before the division can begin.

66) 4'00('0606+, the answer.

396

400 396

As there can be no tenths, a cipher must be placed in the quotient, in tenth's place.

Note. $\frac{4}{66}$ cannot be reduced exactly; for, however long the division be continued, there will still be a remainder.* It is sufficiently exact for most purposes, if the decimal be extended to three or four places.

"Decimal figures which continually repeat, like '06, in this example, are called Repetends or Circulating Decimals. If only one figure repeats, as '3333 or '7777, &c. it is called a single repetend. If two or more figures circulate alternately, as '060606, '234234234, &c. it is called a compound repetend. If other figures arise before those which circulate, as '743333, '143010101. &c. the decimal is called a mixed repetend.

A single repetend is denoted by writing only the circulating figure with a point over it: thus, '3, signifies that the 3 is to be continually repeated, forming an infinite or never ending series of 3's.

A compound repetend is denoted by a point over the first and last repeating figure: thus, 234 signifies that 234 is to be continually repeated

It may not be amiss, here to show how the value of any repetend may be found, or in other words, how it may be reduced to its equivalent vulgar fraction.

If we attempt to reduce $\frac{1}{2}$ to a decimal, we obtain a continual repetition of the figure 1: thus, '11111, that is, the repetend'1. The value of the repetend 1, then is $\frac{1}{2}$; the value of '222, &c. the repetend 2 will be twice as much; that is,

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From the foregoing examples we may deduce the following general Rule :- To reduce a common to a decimal fraction :- Annex one or more ciphers, as may be necessary, to the numerator, and divide it by the denominator. If then there" be a remainder, annex another cipher, and divide as before, and so continue to do so long as there shall continue

In the same manner, '3=3, and '4=4, and '5=4, and so on to 9, which=1:

1. What is the value of '8?

Ans. #.

2. What is the value of '61 Ans. \== 2. What is the value of '3? — of '7? — '41 — '51—'91 — '1?

If $\frac{1}{88}$ be reduced to a decimal, it produces 010101, or the The repetend '02, being 2 times as much, must be 2 and 03-3, and 48, being 48 times as much, must be 48. and '74-74, &c.

If glg be reduced to a decimal, it produces '001; consequently, $002 = \frac{2}{990}$, and $037 = \frac{37}{990}$, and $425 = \frac{125}{990}$, &c. As this principle will apply to any number of places, we have this general RULE for reducing a circulating decimal to a vulgar fraction .- Make the given repetend the numerator, and the denominator will be as many 9s as there are repeating figures.

3. What is the vulgar fraction equivalent to '704?

Ans. 704.

4. What is the value of '003? --- '0141 --- '324? --(01021 1 (24631 --- '002103 1 Ans. to the last, 333333.

5. What is the value of '43?

In this fraction, the repetend begins in the second place, or place of hundredths. The first figure, 4, is 40, and the repetend, 3, is 3 of 10, that is, 30; these two parts must be added together. 4 + 3 - 39 - 13, ans. Hence, to find the value of a mixed repetend,—Find the value of the two parts separately, and add them together.

6. What is the value of '153? $\frac{15}{100} + \frac{3}{900} - \frac{138}{900} - \frac{23}{150}$, ans.

7. What is the value of '138 ! — '16! — '4123! It is plain, that circulates may be added, subtracted, multiplied, and divided, by first reducing them to their equivalent vulgar fractions.

duce the followa decimal fracbe necessary, to inator. If then

r, and divide as

18, &c.

¶ 71.

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What is the '91 — '11's '010101, or the ing 2 times as eing 48 times as

ces (001); conse- $425 = \frac{425}{59}$, &c. or of places, we culating decimal etend the numer-795 as there are

t to '704?

Ans. 794.

the last, 333333

the second place, is $\frac{4}{10}$, and the wo parts must be Hence, to find value of the two

-138 -- 23, ans. 6 1 -- 4123 1 subtracted, multo their equivato be a remainder, or until the fraction shall be reduced to any necessary degree of exactness. The quotient will be the decimal required, which must consist of as many decimal places as there are ciphers annexed to the numerator; and if there are not so many figures in the quotient, the deficiency must be supplied by prefixing ciphers.

EXAMPLES FOR PRACTICE.

4. Reduce $\frac{1}{2}$, $\frac{1}{4}$, $\frac{12}{480}$, and $\frac{1129}{1128}$ to decimals.

Ans. '5; '25; '025; '00797+

5. Reduce $\frac{27}{38}$, $\frac{3}{1000}$, $\frac{5}{1785}$, and $\frac{1}{60006}$ to decimals.

Ans. 692+; 903; 9028+; 900183+.

6. Reduce $\frac{478}{952}$, $\frac{10}{387}$, $\frac{16}{8600}$ to decimals.

7. Reduce $\frac{4}{9}$, $\frac{5}{99}$, $\frac{8}{999}$, $\frac{3}{3}$, $\frac{2}{11}$, $\frac{1}{11}$, $\frac{1}{939}$ to decimals.

8. Reduce $\frac{1}{8}$, $\frac{3}{8}$, $\frac{5}{8}$, $\frac{1}{5}$, $\frac{2}{5}$, $\frac{3}{5}$, $\frac{4}{5}$, $\frac{1}{20}$, $\frac{1}{25}$, $\frac{3}{75}$ to decimals.

REDUCTION OF DECIMAL FRACTIONS.

¶ 72. Fractions, we have seen (¶ 60,) like integers, are reduced from low to higher denominations by division, and from high to lower denominations by multiplication.

To reduce a compound number to reduce the decimal of a ber to a decimal of the highest higher denomination to integers denomination.

Of lower denominations.

1. Reduce 7s. 6d. to the 2. Reduce 375£ to intedecimal of a pound.

6d. reduced to the decimal '375£ reduced to shillings, of a shilling, that is, divided that is, multiplied by 20, is by 12, is '5s., which annexed 7'50s.; then the fractional to the 7s. making 7'5s., and part, '50s., reduced to pence, divided by 20, is '375£ the that is, multiplied by 12, is answer.

6d.

Ans. 7s. 6d.

The process may be presented in form of a rule, thus:—decimal by that number which Divide the lowest denomination to make one of this or more ciphers, as may be higher, and from the right necessary, by that number hand of the product point off which it takes of the same to as many figures for decimals make one of the next higher as there are figures in the denomination, and annex the given decimal, and so contin-

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value of the fraction in the proper denominations.

EXAMPLES FOR PRACTICE EXAMPLES FOR PRACTICE.

3. Reduce 1 oz. 10pwt. to 4. Reduce 125lbs, Troy to the fraction of a pound.

OPERATION. 20)100 pwt. 12)15 oz.

125 lb. Ans.

5. Reduce 4cwt. 23 grs to the decimal of a ton.

23 = 2.6.Note.

7. Reduce 38gals, 3'52qts. of beer, to the decimal of a hogshead of beer? hhd.

9. Reduce 1gr. 2n. to the decimal of a yard.

11. Reduce 17h. 6m. 43s. to the decimal of a day.

13. Reduce 21s. 101d. to the decimal of a guinea.

8oz. to the decimal of a ton. 15334821 of a ton?

integers of lower denominations.

OPERATION. lb. 1125 12 oz. 14500 20

pwt 10'000. Ans. 10z.10pwt 6. What is the value of 2325 of ton !

8. What is the value of '72

10. What is the value of '375 of a yard ?

12. What is the value of '713 of a day ?

14. What is the value of '78125 of a guinea?

15. Reduce 3cwt. 0gr. 7lbs. 16. What is the value of

Let the pupil be required to reverse and prove the following examples:

17. Reduce 4 rods to the decimal of an acre.

18. What is the value of '7 of a lb. of silver?

19. Reduce 18 hours, 15m. 50.4 sec. to the decimal of a day.

20. What is the value of '67 of a league !

21. Reduce 10s. 91d. to the fraction of a pound.

7 78. There is a method of reducing shillings, pence,

h all the de several numhand of the will be the action in the actions.

R PRACTICE. 25lbs. Troy to er denomina-

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prove the fol-

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i pound.

illings, pence,

and farthings to the decimal of a pound, by inspection, more simple and concise than the foregoing. The reasoning in relation to it is as follows:

In of 20s is 2s. ; therefore exery 2s. is 10, or 12. Every shilling is $\frac{1}{20} = \frac{1}{100}$, or '05£. Pence are readily reduced to farthings. Every farthing is what. Had it so happened, that 1000 farthings, instead of 960, had made a pound, then every farthing would have been roun, or '0012. 960 + 40 = 1000; that is, $\frac{1}{\sqrt{3}}$ of 960 added to 960 is 1000. Taking & of a number, and adding to that number, is the same as multiplying the number by unity and the fraction 11. Suppose you have the fraction 14. If you multiply both the numerator, and denominator by 1,2, you do not change the value of the fraction. Do this, and you obtain $\frac{25}{100}$. $\frac{24}{100}$ then is equal to $\frac{25}{100}$. 24 £ is 24 farthings; of course it follows that 24 farthings is equal to Wherefore, if the number of farthings, in the Theat. given pence and farthings, be more than 12, 24 part will be more than 1; therefore add 1 to them: if they be more than 36, 1/2 part will be more than 11; therefore add 2 to them: then call them so many thousandths, and the result will be correct within less than 1 of 1000 of a pound. Thus, 17s. 54d. is reduced to the decimal of a pound as forlows: 16s. = '8£ and 1s. = '05£. Then, 54d = 23 farthings, which, increased by 1, (the number being more than 12, but not exceeding 36,) is '024£, and the whole is '874£ the answer.

Wherefore, to reduce shillings, pence and farthings to the decimal of a pound by inspection,—Call every two shillings one tenth of a pound; every odd shilling, five hundredths; and the number of farthings, in the given pence and farthings, so many thousandths, adding one, if the number be more than twelve and not exceeding thirty-six, and two, if the number be more than thirty-six.

I 74. Reasoning as above, the result, or the three first figures in any decimal of a pound, may readily be reduced back to shillings, pence and farthings, by inspection. Double the first figure, or tenths, for shillings, and, if the second figure, or hundredths, be five or more than five, reckon enother shilling; then, after the five is deducted, call the figures

in the second and third place so many farthings, abating one when they are above twelve, and two when above thirty-six, and the result will be the answer, sufficiently exact for all practical purposes. Thus, to find the value of '876 £ by inspection :-

18	tenths of a pound -	-		=	16 shi	llings.
'05	hundredths of a pound	-	-	=	1 shi	lling.
'026	thousandths, abating 1, =	=25 fa	rthings	=	0 s.	61 d.

'876 of a pound

EXAMPLES FOR PRACTICE.

1. Find, by inspection, the decimal expressions of 9s. 7d. and 12s. 04d. Ans. '479 £, and '603 £.

2. Find, by inspection, the value of '523 £, and '694 £. Ans. 10s. 51d., and 13s. 101d.

3. Reduce to decimals, by inspection, the following sums, and find their amount, viz: 15s. 3d.; 8s. 111d.; 10s. 61d.; Amount, £1'833. Is. 81d.; 1d. and 21d. 4. Find the value of 47.8.

Note. When the decimal has but two figures, after taking out the shillings, the remainder, to be reduced to thousandths will require a cipher to be annexed to the right hand, or supposed to be so. Ans. 9s. 43d.

5. Value the following decimals, by inspection, and find their amount, viz. '785£.; '357£.; '916£.; '74£.; '5£.;

'25£.; '09£.; and '008£. Ans. 3£. 12s. 11d.

SUPPLEMENT TO DECIMAL FRACTIONS.

QUESTIONS.

1. What are decimal fractions? 2. Whence is the term derived? 3. How do decimals differ from common fractions? 4. How are decimal fractions written? 5. How can the proper denominator to a decimal fraction be known, if it be not expressed? 6. How is the value of every figure determined? 7. What does the first figure on the right hand of the decimal point signify? - the second figure? third figure? — fourth figure? S. How do ciphers, placed at the right hand of decimals affect their value? 9. Placed at the left hand how do they affect their value? 10. How are decimals read? 11. How are decimal fractions, having different denominators, reduced to nings, abating en above thiriciently exact value of '876 £

ONS.

= 16 shillings. = 1 shilling. = 0 s. 6½ d. = 17 s. 6½ d.

sions of 9s. 7d. £, and '603 £. £, and '694 £. and 13s. 10½d. following sums, ½d.; 10s. 6¼d.; mount, £1'833.

es, after taking d to thousandths right hand, or Ans. 9s. 43d. ection, and find ; '74£.; '5£.;

RACTIONS.

common denominator? 12. What is a mixed number? 13. How may any whole number be reduced to decimal parts? 14. How can any mixed number be read together, and the whole expressed in the form of a common fraction? 15. What is observed respecting the denominations in federal money? 16. What is the rule for addition and subtraction of decimals, particularly as respects placing the decimal point in the results?—multiplication? — division? 17. How is a common or vulgar fraction reduced to a decimal? 18. What is the rule for reducing a compound number to a decimal of the highest denomination contained in it? 19. What is the rule for finding the value of any given decimal of a higher denomination in terms of a lower? 20. What is the rule for reducing shillings, pence and farthings to the decimal of a pound, by inspection? 21. What is the reasoning in relation to this rule? 22. How may the three first figures of any decimal of a pound be reduced to shillings, pence and farthings, by inspection?

EXERCISES.

1. A merchant had several remnants of cloth, measuring as follows:

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2. From a piece of cloth, containing 36 gyds. a merchant sold, at one time, 7 gyds. and, at another time, 12 gyds.; how much of the cloth had he left?

Ans. 16 7 yds.

3. A farmer bought 7 yards of broadcloth for $8_{13}^{6}\mathcal{L}$, a barrel of flour for $2_{15}^{4}\mathcal{L}$, a cask of lime for $1_{3}^{8}\mathcal{L}$, and 7lbs. of rice for $\frac{5}{24}\mathcal{L}$; he paid 1 ton of hay at $3_{18}^{7}\mathcal{L}$., 1 cow at $6_{3}^{2}\mathcal{L}$ and the balance in pork at $\frac{1}{40}\mathcal{L}$. per lb.; how many were the pounds of pork?

Note. In reducing the common fractions in this example, it will be sufficiently exact if the decimal be extended to three places.

Ans. 1084 lb.

4. At 121 cents per lb. what will 374 bs. of butter cost?

Ana. \$4'7184.

5. At \$17'37 per ton for hay, what will 11\$ tons cost !

Ans. \$201'924.

6. The above example reversed. At \$201'925 for 115 tons of hay, what is that per ton ! Ans. \$17'37.

7. If '45 of a ton of hay cost \$9, what is that per ton 'Consult I 62.

- 8. At 4 of a dollar a gallon, what will '25 of a gallon of molesses cost?
- 9. At \$9 per cwtī, what will 7 cwt. 3 qrs. 16 lbs. of sugar cost?

Note. Reduce the 3 qrs. 16 lbs. to the decimal of a cwt. extending the decimal in this, and the examples which follow to four places.

Ans. 71'935-1.

10. At \$69.875 for 5 cwt. 1qr. 14lbs. of raisins, what is that per cwt.

Ans. \$13.

11. What will 2300lbs of hay come to at 7 mills per lb.

12. What will 7654lbs. of coffee come to at 18 cents per lb.

Ans. \$137.79.

13. What will 12 gallons, 3 qts. 1 pt. of gin cost, at 28 conts a quart?

Note. Reduce the whole quantity to quarts and the decimal of a quart.

Ans. \$14.42.

14. Bought 16 yds. 2qrs. 3na. of broadcloth for \$100 125; what was that per yard?

Ans. \$6.

15. At \$1'92 per bushel, how much wheat may be purchased for \$'72 1 Ans. 1 peck 4 qts.

16. At \$92'72 per ton, how much iron may be purchasd for \$60'268 !
Ans. 13cwt.

17. Bought a load of hay for \$9'17, paying at the rate of \$16 per ton; what was the weight of the hay?

Ans. 11cwt. 1qr. 23lbs.

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18. At \$302'4 per tun, what will 1 hhd. 15 gals. 3 qts. of wine cost ! Ans. \$94'50.

19. The above reversed. At \$94.50 for 1 hhd. 15 gals. 3qts. of wine, what is that per tun?

Ans. \$302.4.

Note. The following examples reciprocally prove each other, excepting when there are some fractional losses, as explained above, and even then the results will be sufficiently exact for all practical purposes. If, hower greater exactness be required, the decimals must be extended to a greater number of places.

90. At \$1'80 for 3½ qts. of 21. At \$2'215 per gallon, wine, what is that per gal. 1 what cost 3½ qts.1

22. If \$ of a ton of potash—23. At \$96.72 per ton for es coet \$60.45, what is that pot-ashes, what will \$ of a ton per ton 1

of a gallon Ans. 8:1. 3 lbs. of su-

al of a cwt.
which fol71'935-ins, what is
Ans. \$13.
mills per lb.
Ans. \$16'10
18 cents per
ns. \$137'79.
n cost, at 28

nd the decins. \$14.42. or \$100.125; Ans. \$6.

may be purl peck 4 qts.
he purchasAns. 13cwt.
g at the rate
hay ?

. 1qr. 23lbs. gals. 3 qts. ns. \$94'50. hd. 15 gals. ns. \$302'4.

prove each
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per gallon,

per ton for Il 4 of a ton

REDUCTION OF CURRENCIES.

In the United States, since the act of Congress in 1786, establishing Federal Money, calculations in money, have generally been made in dollars, cents and mills. In England the denominations, though the same in name as the currency of this Province, are different in value. In the United States, previously to the act of Congress, it was the custom to reckon in pounds, shillings, acc. and now, though all accounts are kept in federal money; small sums are mentioned frequently in these denominations. There are different currencies of the same name in different parts of the United States. It may be necessary often in commercial dealings, and in the course of ordinary business, to change values in foreign currencies into the currency of the Provinces.

Supposing there is a sum in federal money—\$24'604. We find by the table of coins, ¶ 27, that 1 dollar is equal to 5 shillings, and of course 4 dollars equal 1 pound, there being 4 times 5 shillings in 20 shillings. The value of pounds, then it is clear, is 4 times that of dollars, and of course dollars are reduced to pounds by dividing the given sum by 4.

4) .! d. llars.

o pounds.

There remain, however, 604, 60 cents and 4 mills, to be changed to Halifax currency. By referring to Decimal Fractions, ¶ 66, we see that dollars are the units in federal money, and cents and mills decimal parts; cents hundredths, and mills thousandths We have then simply to divide these decimals of a dollar by 4, and the quotient will be an decimal parts of a pound, thus—

4) '604 of a dollar.

'151 of a pound.

This can be reduced to shillings, pence and farthings by inspection, (See ¶ 73,) as follows: '151£ equal 3s. 0d. 1qr. We find that \$24.604 is equal to 6£ 3s. 0d. 1qr. Ans.

The following then, is the general rule, to reduce federal money to Halifax currency,—Divide the given sum by 4, and the quotient will be in pounds and decimal parts of a pound, which can be reduced to shillings, pence and farthings by inspection.

EXAMPLES FOR PRACTICE.

 Reduce \$500 to Halifax currency,
 Ans. 125£.

 " \$27'304
 6£ 11s. 6d. 1qr.

 " \$118'25
 29£ 11s. 3d.

 " \$236'50
 59£ 2s 6d.

Reduce \$490 to Halifax currency. \$56.03, \$93.814, \$85.63, \$1977.642 respectively to Halifax currency.

To reduce Halifax currency to federal money, we must reverse the process in the above examples. The rule is as follows: Reduce the shillings, pence, &c. if any, to the decimal of a pound, by inspection,

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and multiply the given sum by 4, the product will be in the denominations of federal money.

EXAMPLES FOR PRACTICE.

Red to 125£ Halifax currency to federal money.

4na. \$500.

236.50.

In order to change English sterling money, and the currencies in some degree in use in the different parts of the United States, into Halifax currency; since the denominations are the same in name, it will be necessary to take some other currency, the denominations of which are different, as a common object of comparison for these currencies, and for Halifax currency. By this means we shall be able to ascertain the values of the former relatively to those of the latter. We will take federal money as this common object of comparison; and will compare with a unit of one of its denominations, the dollar, one or more cuits of a denomination of Halifax currency, and the before mentioned currencies, the shilling.

In Halifax currency, -- - - 5s. = \$1.

In English, or sterling money, (4s. 6d.)41s.=\$1.

In New-England currency, - - 6s. = \$1.

In New-York currency.

The Pennsylvania currency (7s. 6d.) 74s.=\$1.

In Halifax currency 5s. are equal to \$1, and in English sterling money, 4 shillings and a half are equal to \$1. Sterling money, then, is to Halifax currency as 5 to 4½, or to avoid the fraction, as 10 to 9, since 2×5=10, and 2×4½=9. Therefore, to change sterling money into Halifax currency,—Multiply by ½0, or take once the given sum, and ½, thus,—

9)48.2 12s. 9d. Sterling money.

54 0 19 Halifax currency.
Reduce 56£ 17s. 6d. sterling to Halifax currency. Ans. 63£ 3s. 10d.
Reduce 92 4 6 " " " "

In New-England currency 6s. are reckoned to the dollar. New England currency, then, is to Halifax currency as 5 to 6. Therefore, to reduce New-England currency to Halifax currency,—

Take # of the given sum, thus,—

6) 14£ 5s. 4d. New-England currency.

2 7 5

11 17 4 Halifax currency.

Reduce 60£ 4s. 10d. N. E. currency to Halifax currency Ans. 50£ 4s. 04d

n the denomin-

Ana. \$500. \$236.50.

a currencies in States, into Halia fiame, it will ations of which ese currencies, a able to ascerator. We will a dollar, one or the before men-

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s = \$1.

. =81.

s. = \$1.

inglish sterling g money, then, the fraction, Therefore, to y,—Multiply s,—

s. 63£ 3s. 10d.

dollar. News

ax currency 50£ 4s. 04d To reduce Halifax currency to sterling money, or to reduce Halifax to New-England, it is only necessary to reverse the process in the foregoing operations.

To aduce sterling to Halifax we multiply by 10, therefore, to reduce Halifax currency to sterling money,—Divide the given sum by 10, or, what is the same, multiply by 11, that is, take 10 of the given sum; e.g.

10) 54£ Os. 10d. Halifax currency.

5, 8 1

48 12 9 sterling money.

In the same manner, to reduce Halifax currency to New-England,—Take 6 of the given sum, or, add 5 to the given sum.

From the foregoing rules and illustrations, the pupil himself will be able, by pursuing a similar course, to reduce, with facility, any currency, the denominations of which are pounds, shillings, &c. to any other, in which the denominations are the same.

The following is the general rule for finding a multiplier to reduce any currency to the par of another: Make the number of shillings that are equal to a dollar in the currency to be reduced, the denominator of a fraction; and over this, for a numerator, write the number of shillings that are equal to a dollar in the currency to which the given sum is to be reduced.

Let the pupit find multipliers to reduce New-York and Pennsylvania, currencies to Halifax, and then Halifax currency to those.

ISPTDRDST.

T75. Interest is an allowance made by a debter to a creditor for the use of money. It is computed at a certain number of pounds for the use of each hundred pounds, or so many dollars for each hundred dollars, &c. one year, and in the same proportion for a greater or less sum, or for a longer or shorter time.

The number of pounds so paid for the use of a hundred

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pounds, one year, is called the rate per cent or per centum; the words per cent, or per centum, sygnifying by the hundred.

The highest rate allowed by law in the Canadas is 6 per cent* that is, 6 pounds for 100 pounds, 6 shillings for 100 shillings; in other words $\frac{6}{160}$ of the sum lent or due is paid for the set of it one year. This is called legal interest, and will have understood when no other rate is mentioned.

Let us suppose the sum lent, or due, to be 1£. The 100th part of 1£ or $\frac{1}{100}$ of a pound is, decimally expressed, thus, '01, and $\frac{1}{100}$ of a pound, the legal interest, written as a decimal fraction, is

So of any rate per cent.

Note. The rate per cent is a decimal carried to two places, that is, to hundredths; all decimal expressions lower than hundredths are parts of 1 per cent. § per cent for instance, is '625 of 1 per cent that is, '90625.

Write 21 per cent as a decimal fraction.

2 per cent is '02, and $\frac{1}{2}$ per cent is '005. Ans. '025. Write 4 per cent as a decimal fraction. $\frac{4\frac{1}{2}}{2}$ per cent. $\frac{4\frac{3}{2}}{2}$ per cent. $\frac{3\frac{3}{4}}{2}$ per cent. $\frac{-7\frac{1}{4}}{2}$ per cent. $\frac{-9\frac{1}{2}}{2}$ per cent. 10 per cent. $\frac{-10\frac{1}{2}}{2}$ per cent.

1. If the interest on 1£ for 1 year, be '06 of a pound, what will be the interest on 25£ for the same time?

It will be 25 times 6, or 6 times 25, which is the same thing:

25£.

496

1'50 answer; that is, 1£ and 5 tenths. The 5 tenths must be reduced to shillings, pence and farthings by the rule

^{*}In the New-England States the legal rate is the same as in the Canadas. In England it is 5 per cent.

or per centum; by the hundred. madas is 6 per millings for 100 tor due to paid al interest, and is mentioned.

be 1£. The sally expressed, rest, written as

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arried to two plaexpressions lower per cent for \$25.

Ans. '025.

4½ per cent.

per cent.

1, 9½ per

decimally, '10,)

2½ per cent

'06 of a pound, ame time 1 which is the same

s. The 5 tenths things by the rule

the same as in the

for the reduction of decimals; or with sufficient exactness by inspection. See 7 73. '50, or '5 of a pound equal 10 shillings. The interest of 25£. for a year is then 1£. 10s.

To find the interest on any sum for I year, it is evident we need only multiply it by the rate per cent written as a decimal fraction. The product, observing to place the point as directed in multiplication of decimal fractions, will be the interest required.

Note. PRINCIPAL is the money due, for which interest is paid. AMOUNT is the principal and interest added together.

2. What will be the interest of 32£. 3s. 1 year, at 4½

per cent?

We are to multiply the principal by the rate per cent, 4½, expressed in the form of a decimal, '045; we must therefore reduce the 3s. in the principal, to decimals by inspection. We find 3s. equal to '15. There being five decimal places

32'15£. principal.
'045 rate per cent.

16075 12860

1 44675£.

in the multiplicand and multipla 5 figures must be pointed at for decimals from the product, which gives the answer 1 pound and 44675 hundred thousandths. Any thing less than thousandths need not

be regarded, hence, 1'446£ is sufficiently exact for the answer. The '446 must be reduced to shillings, pence and farthings by inspection. Double the '4 for shillings, equals 8s.; call the '046 so many farthings, deducting two because one 36 equals 44 farthings. In 44 qrs. there are 11 d. '446£—8s. 11d. The interest, then, of 32£. 3s. for 1 year, at 4½ per cent, is 1£. 8s. 11d. answer.

Always, then, if there are shillings, pence and farthings, or either denomination, in the given principal, reduce them to the decimal of a pound by inspection, before multiplying by the rule. After obtaining the answer in decimals, reduce the tenths, hundredths and thousandths, to shillings, pence and farthings, by inspection. The method of effecting each reduction, is exhibited in ¶ 73, and 74, and must be made perfectly familiar to the pupil's mind.

3. What will be the interest of 11£. 3s. 4d. for 1 year, at 3 per cent 1—at 5½ per cent 7—at 6 per cent ?—at 7½ per cent ?—at 8½ per cent ?—at 10 per cent ?—at 10 per cent ?—at 11 per

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cent 1 — at 112 per cent ? — at 12 per cent ! — at 123 per cent ? — at

4. A tax on a certain town is 406£. 15s. 104d., on which the collector is to receive 2½ per cent for collecting; what will be receive for collecting the whole tax at that rate 3

In this example, the shillings, &c. reduced to the decimal of a pound equal '795. Multiply therefore, 406'795£. by the rate 2½, that is, '025. The answer, in decimals, is 10'169£.; the tenths, &c. reduced to shillings, &c. equal 3s. 44d. The answer, then, is, 10£. 3s. 4d.

Note. In the same way are calculated commission, insurance, buying and selling stocks, loss and gain, or any thing else rated at so much per cent without respect to time.

5. What must a man, paying $37\frac{1}{2}$ per cent on his debts, pay on a debt of $132\pounds$. 5s. ?

Ans. $49\pounds$. 11s. 104d.

6. A merchant, having purchased goods to the amount of 580£. sold them so as to gain 12½ per cent, and in the same proportion for a greater or less sum; what was his whole gain, and what was the whole amount for which he sold the goods?

Ans. His whole gain was 72£. 10s. whole amount, 652£.

10s.

7. A merchant bought a quantity of goods for 173£. 15s. how much must be sell them for to gain 15 per cent?

Ans, 199£. 16s. 3d.

176. Commission is an allowance of so much percent to a person called a correspondent, factor, or broker, for assisting merchants and others in purchasing and selling goods.

8. My correspondent sends me word that he has purchased goods to the amount of 1286£, on my account; what will his commission come to at 2½ per cent? Ans. 32£. 3s.

9. What must I allow my correspondent for selling goods to the amount of 2317£9s. 23d. at a commission of 31 per cent 4.

INSURANCE is an exemption from hazard, stated by the payment of a certain sum, which is generally a much per cent. on the estimated value of the property transcript.

Pararom is the sum paid by the insured for the insured

ent ! --- at

Ad., on which ecting; what that rate to the decimal 406.795£. by decimals, is ags, &c. equal

minission, ingain, or any respect to time. on his debts, of. 11s. 104d. to the amount of, and in the what was his for which he

amount, 652£.

for 173£. 15s. per cent 1

199£. 16s. 3d.

of so much per , or broker, for ng and selling

at he has puraccount; what Ans. 32£. 3a for selling good ission of 3‡ per hs. 75£ 6s. 4d.

rd, chained by nerally to much arty interedit or the insurance Policy is the name given to the instrument or writing, by which the contract of indemnity is effected between the insurer and insured.

INTEREST.

10. What will be the premium for insuring a ship from Montreal to Liverpool, valued at 9450.£, at 4½ per cent?

Ans. 425£ 5s.

11. What will be the annual premium for insurance on a house against loss by fire, valued at 875£ at \$\frac{3}{4}\$ per cent?

By removing the separatrix 2 figures towards the left, it is evident, the sum itself may be made to express the premium at 1 per cent, of which the given rate parts may be taken; thus, 1 per cent on 875£ is 8'75£, and 3 of 875£ is 6'562£.

Ans. 6£ 11s. 3d.

12. What will be the premium for insurance on a ship and cargo valued at 6310£, at \(\frac{1}{2}\) per cent? — at \(\frac{2}{2}\) per cent? — at \(\frac{1}{2}\) per cent? — at \(\frac{1}{2}\) per cent? Ans. At \(\frac{1}{2}\) per cent the premium is 39£7s. 8\(\frac{1}{2}\)d.

STOCK is a general name for the capital of any trading company or corporation, or of a fund established by government.

The value of stock is variable. When 100 pounds of tock sells for 100 pounds in money, the stock is said to be it par, which is a Latin word signifying equal; when for tore, it is said to be above par; when for less, it is said to be below par.

13. What is the value of 756£ of stock, at 112½ per ent? that is, when 1 pound of stock sells for 1 pound 12½ undredths in money, which is 12½ per cent above par, or

21 per cent advance, as it is sometimes called.

Ans. 850£ 11s.

14. What is the value of 3700£ of bank stock, at 95½ or cent, that is, 4½ per cent below par? Ans. 3533£ 10s.

15. What is the value of 120£ of stock, at 92½ per cent?—at 86½ per cent?—at 104½ or cent?—at 108½ per cent?—at 115 per cent?—at 37½ per cent advance?

Loss and Gain. 16. Bought a hogshead of molasses 15£; for how much must I sell to gain 20 per cent?

Ans. 18£.

17. Bought broadcloth at 12s. 6d. per yard; but, it be-

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ing damaged, I am willing to sell it so as to lose 12 per cent.; how much will it be per yard?

Ans. 11s.

18. Bought calico at 1s. per yard; how must I sell it to gain 5 per cent.? —— 10 per cent.? —— 15 per cent.? —— to lose 20 per cent.? —— to to lose 20 per cent.? —— to the last, 92d. per yard.

177. We have seen how interest is cast on any sum of money when the time is one year; but it is frequently necessary to cast interest for months and days.

Now, the interest on 1£ for 1 year, at 6 per cent, being

'06, is

'01, one hundredth for 2 months,

'005 five thousandths (or \(\frac{1}{2} \) a hundredth) for 1 month of 30 days, (for so we reckon a month in casting interest,) and

'001 one thousandth for every 6 days; 6 being contained 5 times in 30.

Hence, it is very easy to cast in the mind, the interest on 1£, at 6 per cent for any given time. The hundredths, it is evident, will be equal to half the greatest even number of months; the thousandths will be 5 for the odd month, if there he one, and 1 for every time 6 is contained in the given number of the days.

Suppose the interest of 1£, at 6 per cent, be required for 9 months, and 18 days. The greatest even number of the months is 8, half of which will be the hundredths, '04; the thousandths, reckoning 5 for the odd month, and 3 for the 18 (3 times 6 = 18) days, will be '008, which, united with the hundredths ('048) give 4 hundredths and 8 thousandths, 4 hundredths, and 8 thousandths, or, '048£ reduced=11d.

1. What will be the interest on 1£ for 5 months 6 days

— 6 months 12 days? — 7 months? — 8 months

24 days? — 9 months 12 days? — 10 months?

11 months 6 days? — 12 months 18 days? — 15

months 6 days? — 16 months?

ODD DAYS. 2. What is the interest of $1\mathcal{L}$ for 13 month 16 days?

The hundredths will be 6, and the thousandths 5, for the odd month, and 2 for 2 times 6 = 12 days, and there is remainder of 4 days, the interest for which will be sud

° 1 76, 77.

o lose 12 per

Ans. 11s.

11s per cent. 1

12d, per yard.

11s on any sum

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nd, the interest The hundredths, atest even numthe odd month, contained in the

t, be required for number of the redths, '04; the h, and 3 for the ich, united with d 8 thousandths, greduced=11d.

1£ for 13 month

sandths 5, for the side of the

part of 1 thousandth as 4 days is part of 6 days, that is, \$

= \frac{2}{3}\$ of a thousandth.

Ans. '067\frac{2}{3}.

3. What will be the interest of 1£ for 1 month 8 days 1 — 2 months 7 days 1 — 3 months 15 days 1 — 4 months 22 days 1 — 5 months 11 days 7 — 6 months 17 days 1 — 7 months 3 days 1 — 8 months 11 days 1 — 9 months 2 days 1 — 10 months 15 days 1 — 11 months 4 days 1 — 12 months 3 days 1

Note. If there is no odd month, and the number of days be less than 6, so that there are no thousandths, it is evident, a cipher must be put in the place of thousandths; thus, in the last example,—12 months 3 days,—the hundredths will be '06, the thousandths 0, the 3 days 4 a thousandth.

Ans. 1s.23d.

4. What will be the interest of 1£ for 2 months 1 day?

— 4 months 2 days? — 6 months 3 days? — 8 months
4 days? — 10 months 5 days? — for 3 days? —

for 1 day? — for 2 days? — for 4 days? — for 5 days?

5. What is the interest of 56£ 2s. $7\frac{2}{4}$ d. for 8 months 5 days? The interest of 1£, for the given time, is '040\frac{1}{4};

therefore,

4) and 4)56'13£. principal.

'040g interest of 1£ for the given time.

224520 interest for 8 months.

2806 interest for 3 days.

1871 interest for 2 days.

2'29197£ = 2£ 5s. 94d.

5 days = 3 days + 2 days. As the multiplicand is taken once for every 6 days, for 3 days take $\frac{1}{2}$, for 2 days take $\frac{1}{3}$, of the multiplicand. $\frac{1}{2} + \frac{1}{3} = \frac{1}{6}$. So also, if the odd days be 4 = 2 days + 2 days, take $\frac{1}{3}$ of the multiplicand twice; for 1 day, take $\frac{1}{6}$.

From the illustrations now given, it is evident,—To find the interest of any sum in Halifax currency, or any other currency of which the denominations are pounds, shillings, &c. at 6 per cent, it is only necessary to multiply the given principal, after having reduced the shillings and pence in it to the decimal of a pound by inspection, by the interest of 1£ for the given time, found as above directed and written as a deci-

mal fraction; after pointing off as many places for decimals in the product as there are decimal places in both the factors counted together, these can be reduced back again to shillings and pence by inspection.

EXAMPLES FOR PRACTICE.

6. What	is the	interest of	87£ 3s.	97d. f	or 1 year 3
months ?		9 4	. , .	Ans.	6£ 10s. 94d.

7. Interest of 116£ 1s. 74d. for 11 mo. 19 days?

Ans. 6£ 15s. 04d.

8. Interest of 200£ for 8 mo. 4 days ? 8£ 2s. 7‡d. 9. " of 17s. for 19 mo. ? 1s. 7‡d.

10 " of 8£ 10s. for 1 year 9 mo. 12 days?

18s. 27d.

11. " of 675£ for 1 mo. 21 days 1 5£ 14s. 84d. 12. " of 8673£ for 10 days 1 14£ 9s. 14d.

13. " of 14s. 7\flat for 10 mo. 1 8\frac{7}{2}d.

14. " of 96£ for 3 days ? Note. The

15. " of 73.£ 10s. for 2 days? | interest of 1.£

16. " of 180£ 15s. for 5 days ? ∫ for 6 days be-17. " of 15000£ for 1 day? ∫ ing 1 thou-

sandth, the pounds themselves express the interest in thousandths for six days, of which we may take parts.

Thus, 6)15000 thousandths,

2'500, that is, 2£ 10s Ans. to the last.

When the interest is required for a large number of years, it will be more convenient to find the interest for one year, and multiply it by the number of years; after which find the interest for the months and days, if any, as usual.

18. What is the interest of 10002 for 120 years ?

Ans. 7200£.

19. What is the interest of 520£ 0s. 92d. for 30 years and 6 months?

Ans. 951£ 13s. 52d.

20. What is the interest on 4002 for 10 years 3 months and 6 days 1

21. What is the interest of 220£ for 5 years? — for 12 years? — 50 years? Ans. to the last 660£.

22. What is the amount of 86£, at interest 7 years ?

Ans. 122£ 2s. 44d.

23. What is the interest of \$48'30 for 1 year?
It must be clear to the pupil's mind, that to obtain the

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ays ! 18s, 27d. 5£ 14s, 87d. 14£ 9s, 11d.

Note. The nterest of 1£ or 6 days being 1 thouserest in thousers.

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the interest upon any sum in federal money, for any time, we proceed just as we do in Halifax currency; only we are not compelled to reduce any part of the given sum to decimals, since all the denominations of federal money are in a decimal ratio. The answer to the last example is \$2.890.

What is the interest of \$64 for 2 years ? Ans. \$7'68. What is the interest of \$98'50 for 7 years, 6 months and 10 days? Ans. \$44'489.

178. 1. What is the interest of 36 pounds for 8

months, at 41 per cent?

Note. When the rate is any other than six per cent, first find the interest at 6 per cent, then divide the interest rational by such part as the interest, at the rate required, exceeds or falls short of the interest, at 6 per cent, and the quotient added to or subtracted from the interest at 6 per cent, as the case may be, will give the interest required.

36£

'04

4½ per cent is ¼ of 6 per cent; therefore, from the interest at 6 per cent subtract ¼; the remainder will be the interest at 4½ per cent.

1.08£. 1£ 1s. 74d. answer.

2. Interest of 54£ 16s. 22d, for 18 months, at 5 per cent !

Ano. 4£ 2s. 22d.

3. Interest of 500£ for 9 months 9 days, at 8 per cent?

Ans. 31£.

4. Interest of 62£ 2s. 43d. for 1 mo. 20 days, at 4 per cent?

Ans. 6s. 103d.

5. Interest of 85£ for 10 months 15 days, at 12½ per cent?

Ans. 9£ 5s. 102d.

6. What is the amount of 53£ at 10 per cent for 7 mo.?

Ans. 56£ 1s. 94d.

The time, rate per cent. and amount given, to find the principal.

7 79. 1. What sum of money, put at interest at 6 per cent, will amount to 61£ 43d. in 1 year 4 months?

The amount of $1\pounds$ at the given rate and time, is $1^{\circ}08\pounds$; hence, $61^{\circ}02\pounds\div1^{\circ}08\pounds=56^{\circ}50$, the principal required; that is,—Find the amount of $1\pounds$ at the given rate and time, by which divide the given amount; the quotient will be the principal required.

Ans. $56\pounds$ 10s.

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2. What principal, at 8 per cent, in 1 year 6 months, will amount to 85£ 2s. 42d. 1

3. What principal, at 6 per cent, in 11 months 9 days, will amount to 992 6s. 23d.1

4. A factor receives 985£ to lay out after deducting his commission of 4 per cent; how much will remain to be laid out?

It is evident, he ought not to receive commission on his own money. This question, therefore, in principle, does not differ from the preceding.

Note. In questions like this, where no respect is had to time, add the rate to 1£.

Ans. 950£.

5. A factor receives 1008£ to lay out after deducting his commission of 5 per cent, what does his commission amount to?

Ans. 48£

DISCOUNT. 6. Suppose I owe a man 397£ 10s. to be paid in I year, without interest, and I wish to pay him now; how much ought I to pay him when the usual rate is 6 per ct.?

l ought to pay him such a sum, as put at interest, would, in 1 year, amount to 397£. 10s. The question, therefore, does not differ from the preceding.

Ans. 375£.

Note. An allowance made for the payment of any sum of money before it becomes due, as in the last example, is called Discount.

The sum which, put at interest, would, in the time and at the rate per cent, for which discount is to be made, amount to the given sum, or debt, is called the present worth.

What is the present worth of S34£, payable in 1 year
 months and 6 days, discounting at the rate of 7 per cent !
 Ans. 750£.

8. What is the discount on 3212 12s. 74d. due 4 years hence, discounting at the rate of 6 per cent?

9. How much ready money must be paid for a note of 18£, due 15 months hence, discounting at the rate of 6 per cent?

Ans. 16£ 14s. 104d.

10. Sold goods for 650£; payable one half in 4 months, and the other half in 8 months; what must be discounted for present payment?

Art. 18£.

¶ 79.

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7 per cent ! Ans. 750£. due 4 years

to 50. 24d. or a note of ate of 6 per 14s. 104d. a 4 months, discounted Ann. 18£.

11. What is the present worth of 56£ 4s. payable in 1 year 8 months, discounting at 6 per cent 1 — at 4½ per cent 1 — at 5 per cent 1 — at 7½ per cent 1 — at 9 per cent 1

Ans. to the last 48£ 17s. 47d.

The time, rate per cent., and interest being given, to find the principal.

¶ 80. 1. What sum of money, put at interest 16 months,

will gain 10£ 10s. at 6 per cent !

1£ at the given rate and time, will gain '08; hence, $10^{\circ}50\pounds \div '08\pounds = 131^{\circ}25$,£ the principal required; that is,—Find the interest of 1£, at the given rate and time, by which divide the given gain, or interest; the quotient will be the principal required.

Ans. 131£ 5s.

2. A man paid 4.£ 10s. 42d. interest at the rate of 6 per cent at the end of 1 year 4 months; what was the principal?

Ans. 56.2 10a.

3. A man received, for interest on a certain note, at the end of 1 year, 20£; what was the principal, allowing the rate to have been 6 per cent?

Ans. 333£ 6s. 8d.

The principal, interest and time being given, to find the rate per cent.

T 81. 1. If I pay 32 15s. 74d. interest, for the use of 302 for 1 year and 6 months, what is that per cent?

The interest on 36£ at 1 per cent, the given time, is '54£; hence, 3'78£: '54£='07, the rate required; that is, Find the interest on the given sum, at 1 per cent, for the given time, by which divide the given interest; the quotient will be the rate at which interest was paid.

Ans. 7 per cent.

2. At 2£ 6s. 9\(\frac{2}{4}\)d. for the use of 468£ 1 month, what is the rate per cent?

Ans. 0 per cent.

3. At 46£ 16s. for the use of 520£, 2 years, what is that per cent?

Ans. 4½ per cent.

The prices at which goods are bought and sold, being given, to find the rate per cent. of GAIN or LOSS.

¶ 82. 1. If I purchase cloth at 12 2s. a yard, and sell it at 12 7s. 6d. per yard; what do I gain per cent?

This question does not differ essentially from those in the foregoing paragraph. Subtracting the cost from the price

at sale, it is evident I gain 275.20 on a yard, that is, 778 of the first cost. 278-25 per cent the answer. That is, —Make a common fraction, writing the gain or loss for the numerator, and the price at which the article was bought for the denominator; then reduce it to a decimal.

2. A merchant purchases goods to the amount of 550£;

what per cent profit must be make to gain 66£?

Ans. 12 per cent.

3. — What per cent profit must be make on the same purchase to gain 38£ 10s.? — to gain 24£ 15s.? —

to gain 2£ 15s. ?

Note. The last gain gives for a quotient '005, which is per cent. The rate per cent, it will be recollected, (¶ 75, note,) is a decimal carried to two places, or hundredths; all decimal expressions lower than hundredths are parts of 1 per cent.

4. Bought a hogshead of liquor, containing 114 gallons, at '96£ per gallon, and sold it at 1£ 0s. 0d. 3½qrs. per gallon; what was the whole gain, and what was the gain per cent 1 Ans. 4£ 18s. 5½d. whole gain. 4½ gain per cent.

5. A merchant bought a quantity of tea for 365£, which, proving to have been damaged, he sold for 332£ 3s. what did he lose per cent?

Ans. 9 per cent.

6. If I buy cloth at 2£ per yard, and sell it for 2£ 10s.

per yard, what should I gain in laying out 100£.

Ans. 25£

7. Bought indigo at 6s: per lb. and sold the same at 4s. 6d. per lb.; what was the loss per cent? Ans. 25 per cent.

8. Bought 30 hogsheads of liquous at $600\pounds$; paid in duties $20\pounds$ 13s. $2\frac{1}{2}$ d.; for freight, $40\pounds$ 15s. $7\frac{1}{2}$ d.; for porterage, $6\pounds$. 1s.; and for insurance, $30\pounds$ 16s. $9\frac{1}{2}$ d.; if I sell them at $26\pounds$ per hogshead, how much shall 1260 per cent.

Ans. 11'695 per cent.

The principal, rate per cent, and interest being given, to find the time.

¶ 83. 1. The interest on a note of 36£, at 7 per cent, was 3£ 15s. 7½d., what was the time ?

The interest on 36£ 1 year, at 7 per cent, is 2£ 10s. 42d. 3'78£-2'52£=1'5 years, the time required; that is,—Find the interest for 1 year on the principal given, at the given

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10s. 42d. is,—Find the given rate, by which divide the given interest; the quotient will be the time required, in years and decimal parts of a year; the latter may then be reduced to months and days.

Ans. I year 6 months.

2. If 31£ 14s. 2½d. interest be paid on a note of 226£ 10s. what was the time, the rate being 6 per cent 1

Ans. 2'331=2 years 4 months.

3. A note of 600£, paid interest 20£, at 8 per cent; what was the time 1

Ans. '416+=5 months so nearly as to be called 5, and would be exactly 5 but for the fraction lost.

4. The interest on a note of 217£ 5s. at 4 per cent, was 28£ 4s. 10d.; what was the time? Ans. 3 y. 3 mo.

Note. When the rate is 6 per cent, we may divide the interest by ½ the principal, removing the separatrix two places to the left, and the quotient will be the answer in months.

The method given above, of finding the interest upon any sum in Halifax currency, for any time, and at any rate, will be found sufficiently exact in practice, and as simple and concise, perhaps, as any that could be proposed.

The teacher will do well to see that the scholar understands perfectly, the process by which the reciprocal reductions are effected by inspection, and the reason of this process.

If greater exactness be required, the reductions can be effected by the ordinary rules for the reduction of decimal fractions.

The following is a method of casting interest by vulgar fractions.

To obtain the interest upon any sum, for any time, at any rate:—Multiply the lowest terms of a fraction, the numerator of which is the given rate, and the denominator 100. by the given number of years; multiply the lowest terms of a fraction, the numerator of which is the given rate and the denominator 1200, by the given number of months, multiply the lowest terms of a fraction the numerator of which is the given rate, and the denominator 3600, by the given number of days; then reduce these several fractions to one common denominator; add them together, and by the resulting fraction multiply the given principal.

Find the interest of 100£ for 2 years, 6 months and 10 days, at 6 per sent.

> $\frac{3}{50}$ (or, $\frac{3}{100}$) × 2 years = $\frac{6}{50}$ $\frac{1}{260}$ (or, $\frac{1}{1200}$) \times 6 months = $\frac{1}{260}$. ϵ_{000} (or, ϵ_{000}) ≈ 10 days = ϵ_{00} = ϵ_{00} .

50, x60, and are to be reduced to one common denominator. Neglect the ciphers in the denominators-

 $5 \times 2 \times 6 = 60$; 1+2+2=5, the number of ciphers. The common denominator is then 60, and 5 ciphers.

 $6 \times 2 \times 6 = 72$; this with 4 ciphers is 1st numerator.

 $5 \times 6 \times 6 = 180$; this with 3 ciphers is 2d numerator.

 $5 \times 2 \times 1 = 10$; this with 3 ciphers is 3d numerator.

Each numerator has as many as 3 ciphers; cut off 3 from each and 3 from the common denominator; $\frac{720}{6000} + \frac{180}{600}$ $+\frac{10}{900} = \frac{910}{6000} = \frac{91}{6000}$. Then 100£, the given principal,

multiplied by $\frac{9}{600} = \frac{9}{6} \pounds = 15 \pounds 3s. 4d.$

The reasons of the different steps in the foregoing process will appear—When the rate, as in the above example, is 6 per cent it is obvious, that the interest of any given principal for one year is $\frac{6}{100}$, or $\frac{3}{50}$ of that principal. For any number of years, the interest must be as many times 30 of the principal, as there are units in the given number of years. In the example 2 is the given number of years; multiply then 3 by 2; or multiply the lowest terms of a fraction the numerator of which is the given rate, and the denominator 100, by the given number of years. 6 of the given principal then is the interest for 2 years. 1200 of the given principal is the interest for 1 month; for there are 12 months in a year, and $\frac{1}{100} \times \frac{1}{12} = \frac{6}{1200}$, or $\frac{1}{200}$. $\frac{6}{3600}$ of the given principal is the interest for I day; for there are 30 days in 1 month, and $\frac{6}{1200} \times \frac{1}{20} = \frac{6}{3600} = \frac{1}{6000}$. We have then 30 of given principal, as the interest for 1 year; $\frac{1}{2}$ of same, for 1 month, and $\frac{1}{6000}$ for 1 day. For 2 years, we have $\frac{6}{50} \times 2 = \frac{6}{50}$; for 6 months $\frac{1}{200} \times 6 = \frac{6}{200}$; for 10 day, $6000 \times 10 = 6000 = 600$. $\frac{6}{50}$, $\frac{6}{200}$ and $\frac{1}{600}$ then of the given principal are the interest of 100£ for 2 years, 6 months and 10 days. It is clear now, why we reduce these several fractions to one common denominator, add them together, and by the resulting fraction multiply the given principal.

Find the interest upon 78£ 4s. for 3 years, 9 months and 6 days, by this method, at 6 per cent, and also at 5 pr cent.

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To find the interest due on notes, &c. when partial payments have been incide.

T 84. There is no statute in this Province, prescribing any particular form or method of casting interest upon notes or other obligations. It is believed the following method is generally allowed before the courts of the country, and also is that which has obtained to the greatest extent in mercantile transactions.

RULE.—Compute the interest upon the value for which the note, or other instrument was given, to the time of payment, which add to the principal; find the amount also of each endorsement to the time of payment, which several amounts add together, and the sum subtract from the amount of the value upon the face of the note, or other instrument.

1. For value received, I promise to pay Louis Rousseau, or order, one hundred pounds fifteen shillings, with interest.

100£ 15s.

JOHN BURTON.

May 1, 1822.

On this note, were the following endorsements:

Dec. 25, 1822, received 102.

July 10, 1823, " 1£ 4s.

Sept. 1, 1824, " 3£6s.

June 14, 1825, " 21£ 150.

April 15, 1826, " 54£ 9s.

What was due Aug. 3, 1827 ! Ans. 31£ 3s. 1d.

The whole time is, from May 1st, 1822, to Aug. 3, 1827, which is 5 years, 3 months, 2 days. The interest of 100£ 15s. for this time is 31£. 15s. 42d. This added to the value for which the note was given is, 100£ 15s.+31£ 15s. 42= 132£ 10s. 42d. which is equal to the amount of the value for which the note was given. The first endorsement is 10£; the date of this endorsement is Dec. 25, 1822; the time of payment is Aug. 3, 1827. The time, therefore, for which interest is to be cast upon this endorsement, is 4 yrs. 7 mo. 8 days. The interest for this time is 2£ 15s. 3d. which added to the endorsement makes its amount 12£ 15s. 3d. In the same way find the amount of each other endorsement, by casting the interest upon it from the day of its date to the day of the payment of the note, and add this interest to the principal, that is, the endorsement.

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terest annually; but at the end of I year, not finding it convenient to pay the interest, he consents to pay interest on the interest from that time, the same as on the principal.

Note. Simple interest is that which is allowed for the principal only; compound interest is that which is allowed for both principal and interest, when the latter is not paid at the time it becomes due.

Compound interest is calculated by adding the interest to the principal at the end of each year, and making the amount the principal for the next succeeding year.

1. What is the compound interest of 256£ for 3 years,

at 6 per cent?

256£ given sum or first principal. '06

15'36 interest, 256'00 principal, } to be added together.

271'36 amount, or principal for 2d year.

16'2816 compound interest 2d year, addded to-271'36 principal, do. gether.

287'6416 amount, or principal for 3d year.

17.258496 compo interest 3d year, 2 added to 287.641 principal, do 304.899 amount.

256 first principal subtracted.

48,899£ compound interest for 3 years.

Ams. 48£ 17s. 114d.

2. At 6 per cent, what will be the compound interest, and what the amount, of 1£ for 2 years? — what the amount for 3 years? — for 4 years? — for 5 years! — for 6 years! — for 7 years! — for 8 years!

Ans. to the last, 13 11s. 101d.

It is plain that the amount of &£, for any given time, will be 2 times as much as the amount of &£; the amount of &£ will be 3 times as much, &c.

Hence, we may form the amounts of L£, for several years,

into a table of multipliers for finding the amount of any sum for the same time.

TABLE,

Showing the amount of 1£, or 1\$, &c. for any number of years; not exceeding 24, at the rates of 5 and 6 per cent compound interest.

Years.	5 per cent.	6 per cent.	Yrs.	5 per cent.	6 per cent.
1	1.05	1.08	18	1.88564+	2 13292+
2	1.1025	1.1236	14	1 97993-	2.26090-
13	1.15762+	1419101+	15	2.07892-	2.39655+
4	1.21550-	1.20247-	10	2418287+	2.54035+
5	1.27628+	1.33822-	17	2 29201+	2.69277
6	1.34009	1.41951+	18	2:40661+	2'85483+
7	1.40710+	1.50363+	19	2.52695	3 02559-
8	1.47745+	1.59384+	20	2.65329+	3-20713+
9	1.55132+	1.68947+	21	2.78596+	3.39956+
10	1.62889-	1'79084+	22	2.92526+	3.60353+
- 11	1.71033+	1.89829+	23	3.07152+	3'81974+
12	1.79585+	2.01219+	24	3-22509+	4.04893+

Note 1. Four decimals in the above numbers will be suf

ciently accurate for most operations.

Note 2. When there are months and days, you may first find the amount for the years, and on that amount cast the interest for the months and days; this, added to the amount, will give the answer.

8. What is the amount of 600£ 10s. for 20 years, at 5 per cent, compound interest? — at 6 per cent?

1£ at 5 per cent, by the table is 9.65329£; therefore, $2.65329 \times 600.50 = 1593.30£ + is <math>1593£$ 6s. Ans. at 5 per cent; and $3.20713 \times 600.50 = 1925.881£ + is <math>1925£$ 17s $7\frac{3}{2}4$. Ans. at 6 per cent.

4. What is the amount of 40.6 4s. at 6 per cent, compound interest, for 4 years? — for 10 years? — for 1 years? — for 12 years? — for 3 years and 4 months

--- for 24 years 6 months and 18 days !

Ans. to the last 168£ 2s. 834

Note. Any sum at compound interest will double itse require, Note.

From what has now been advanced we deduce the following general

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you may first nount cast the to the amount,

20 years, at 5 cent?

9£: therefore, Ans. at 5 per in Halifax currency. is 1925£ 17s

RULE.

1. To find the interest when the time is I year, or, to find the rate per cent on any sum of money, without respect to time, as the premium for insurance, commission, &c ..-Multiply the principal, or given sum, after having reduced the shillings, and pence in it to the decimal of a pound, by the rate per cent, written as a decimal fraction; after pointing off as many places for decimals in the product as there are decimals in both the factors, and reducing these decimals back to shillings and pence, we shall obtain the interest required.

II. When there are months and days in the given time. to find the interest on any sum of money at 6 per cent .-Multiply the principal, reducing the shillings and pence by inspection, by the interest on 12 for the given time, found by inspection, and the product, as before, will be the interest required, taking care to reduce the decimal parts to shillings

and pence by inspection.

To find the interest on 1£, at 6 per cent, for any given time by inspection, -It is only to consider, that half the greatest even number of months will denote hundredths of a pound, and that there will be five thousandths of a pound for the odd month, (if there be one,) and one thousandth for every 6 days.

IV. If the sum given be in federal money,-The denominations being in a decimal ratio, we are saved from the neconsity of effecting the reciprocal reductions, at the beginning and end of the process, otherwise proceed precisely as

V. If the interest required be at any other rate than 6 per cent, (if there be months, or months and days, in the per cent, com given time,)—First find the interest at 6 per cent; then direct a for livide the interest so found by such part or parts, as the inand 4 months terest, at the rate required, exceeds, or falls short of the interest at 6 per cent, and the quotient, or quotients, added to at 168£ 2s. 84 or subtracted from the interest at 6 per cent, as the case may vill double itse require, will give the interest at the rate required.

Note. The interest on thy number of pounds, for 6 days. at 6 per cent, is readily found by cutting off the unit or deduce the for right hand figure; those at the left hand will show the in-

erest in hundredths for 6 days.

EXAMPLES FOR PRACTICE.

- 1. What is the interest of 1600.2 for I year and 3 months?
- 2. What is the interest of 5£ 16s. for 1 year 11 months?

 Ans. 13s. 4d.
- 3. What is the interest of 2£ 5s. 94d? for 1 month 19 days, at 3 per cent?

 Ans. 24d.
- 4. What is the interest of 18£ for 2 years 14 days, at 7 per cent?

 Ans. 2£ 11s. 42d.
- 5. What is the interest of 17£ 13s, 7\frac{1}{4}d, for 11 months 28 days?

 Ans. 1£ 1s. 1d.
- 6. What is the interest of 200£ for 1 day! —— 2 days! —— 3 days! —— 5 days!
 - Ans. for 5 days, 3s. 34d.
 - 7. What is the interest of half '001£ for 567 years 1 Ans. 4d.
- 8. What is the interest of 81£, for 2 years 14 days, at ½ per cent? ¾ per cent? 2 per cent? 3 per cent? 4½ per cent? 5 per cent? 6 per cent? 7 per cent? 7½ per cent? 8 per cent? 9 per cent? 10 per cent? 12 per cent? 12½ per cent?
 - Ans. to last, 20£ 12s. 101d.

 9. What is the interest of '09£ for 45 years, 7 months.
- 11 days ! Ans. 4s. 101d.

 10. A's note of 175£ was given Dec. 6, 1798, on which
- 10. A's note of 175£ was given Dec. 6, 1798, on which was endorsed one year's interest; what was there due Jan. 1, 1803?
- Note. Consult ex. 16, Supplement to Subtraction of Compound Numbers.

 Ans. 207£ 4s. 4‡d.
- 11. B's note of 56£ 15s. was given June 6, 1801, on interest after 90 days; what was there due Feb. 9, 1802 !

 Ans. 58£ 3s. 94d.
- 12. C's note of 365£ was given Dec. 3, 1797; June 7, 1800, he paid 97£ 3s. 24d.; what was there due Sept. 11.

 1800 1

 Ans. 327£ 0s. 74d.
- 13. Supposing a note of 422£, dated July 5, 1797, on which were endorsed the following payments, viz. Sept. 13. 1799, 208£ 4s.; March 10, 1800, 96£; what was there due Jan. 1, 1801.

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s. 13s. 4d. month 19 Ans. 24d. days, at 7 £ 11s. 44d. 11 months

— 2 days ! ys, 3s. 3åd. 7 years !

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ubtraction of 207£ 4s. 4¾d. 1801, on inb. 9, 1802 ? 58£ 3s. 9¾d. 797; June 7, due Sept. 11. 327£ 0s. 7¼d. 75, 1797, on viz. Sept. 13, hat was there

SUPPLEMENT TO INTEREST.

QUESTIONS.

1. What is interest? 2. How is it computed? 3. What is understood by rate per cent?? 4. — by principal? 5. — by amount? 6. — by legal interest? 7. — by commission? 8. — insurnnco? 9. — premium? 10. — policy? 11. — stock? 12. What is understood by stock being at par? 13. - above par? 14. — below par? 15. The rate per cent. is a decimal carried to how many places? 16. What are decimal expressions lower than hundredths: 17. How is interest, (when the time is I year,) commission, insurance, or any thing else rated at so much per cent. without respect to time, found? 18. When the rate is one per cent., or less, how may the operation be contracted? 19. How is the interest on 1£, at 6 per cent. for any given time, found by inspection? 20. How is interest cast, at 6 per cent., when there are mouths and days in the given time? 21 When the given time is less than 6 days, how is the interest most readily found? 22. If the sum given be in federal money, how is interest cast? 23. When the rate is any other than 6 per cent., if there be months and days in the given time, how is the interest found? 24. What is the rule for casting interest on notes, &c. when partial payments have been made? 25. How may the principal be found, the time, rate per cent. and amount being given? 26. What is understood by discount? 27. - by present worth? 28. How is the principal found, the time, rate per cent, and interest being given? 29. How is the rate per cent of gain or loss found, the prices at which goods are bought and sold being given? 30. How is the rate per cent found, the principal, interest, and time being given? 31. How is the time found, the principal, rate per cent and interest being given? 32 How may interest be east by vulgar fractions? 33. What is the reasoning in regard to this rule? 34. What is simple interest? 35. compound interest? 36. How is compound interest computed?

EXERCISES

1/ What is the interest of $273\pounds$ 10s. $2\frac{3}{4}$ d. for 1 year 10 days, at 7 per cent?

Ans. $19\pounds$ 13s. $6\frac{3}{4}$ d

2. What is the interest of 486£ for 1 year, 3 months, 19 days, at 8 per cent?

Ans. 50£ 13s. 4\frac{3}{4}d.

3. D's note of 203£ was given Oct. 5, 1808, on interest, after 3 months; January 5, 1809, he paid 50£; what was there due May 2, 1811?

Ans. 175£ 7s. 2d.

4. E's note of 870£, was given Nov. 17, 1800, on interest after 90 days; Feb. 11, 1805, he paid 186£; what was there due Dec. 23, 1807? Ans. 1009£ 11s. 634.

5. What will be the annual insurance, at \S per cent, on a house valued at $1600\pounds$?

6. What will be the insurance of a ship and cargo, valued

at 5643£ at 1½ per cent ? — at ½ per cent ?

Note. Consult T 76, ex. 11.

Ana. at # per cent. 42£ 6s. 54d.

7. A man having compromised with his creditors at 624 per cent, what must be pay on a debt of 137£ 9s. 24d.

Ans. 85£ 18a. 3d.

8. What is the value of 800£ Montreal Bank stock, at 1121 per cent ?

Ans. 900£.

9. What is the value of 560£ 15s. of stock, at 93 per cent?

Ans. 521£ 9s. 114d.

10 What principal at 7 per cent, will, in 9 months 18 days amount to 422£ 8s.

Ans. 400£.

11. What is the present worth of 426£, payable in 4 years and 12 days, discounting at the rate of 5 per cent 1

In large sums, to bring out the hundredths and thousandths correctly, it will sometimes be necessary to extend the decimal in the divisor to five places.

Ans. 354£ 10s. 12d.

12. A merchant purchased goods for 250£, ready money, and sold them again for 300£, payable in 9 months; what did he gain, discounting at 6 per cent 1 *Ans. 37£ 1s. 72d.

14. The interest on a certain note, for 1 year 9 months, was 49£ 17s. 6d., what was the principal?

Ans. 475£.

15. What principal, at 5 per cent., in 16 months 24 days, will gain 35£?

Ans. 500£.

16. If I pay 15£ 10s. interest for the use of 500£, 9 months and 9 days, what is the rate per cent?

17. If I buy candles at \$ '167 per lb., and sell them at 20 cents, what shall I gain in laying out \$100 ?

Ans. \$19'76.

18. Bought hats at 4s, apiece, and sold them again at 4s. 9d.; what is the profit in laying out 100£?

Ans. 18£ 15s.

19. Bought 37 gallons of brandy, at \$1'10 per gatton and sold it for \$40; what was gained or lost per cent?

20. At 4s. 6d. profit on 1£, how much is gained in laying out 100£, that is, how much per cent? Ans. 22£ 10s.

21. Bought cloth at \$4'48 per yard; how must I sell it to gain 124 per cent?

Ans. \$5'04.

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k. at 93 per £ 9n. 111d. months 18 Ans. 400£. payable in 4 per cent ?

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e half in 3 must be dis-8£ 9s. 10d. r 9 months.

Ans. 475£. the 24 days. Ans. 500£. of 500£, 9

sell them at ns. \$19'76.

again at 4s. a. 18£ 15s. per gallon er cent !

ned in lays. 22£ 10s. nust I sell it Ans. \$5.04.

22. Bought a barrel of powder for 42; for how much must it be sold to lose 10 per cent? . Ans. 3£ 12a.

23. Bought cloth at 15s. per yard, which not proving so good as I expected, I am content to lose '17; per cent; how must I sell it per yard?

24. Bought 50 gallons of brandy, at 92 cents per gallon, but by accident 10 gallons leaked out; at what rate must I sell the remainder per gallon, to gain upon the whole cost at the rate of 10 per cent? Ans. \$1'265 per gal.

25. A merchant bought 10 tons of iron for \$950; the freight and duties came to \$145, and his own charges to \$25; how must be sell it per lb. to gain 20 per cent by it ! Ans. 6 cents per lb.

EQUATION OF PAYMENTS.

V. 86. Equation of payments is the method of finding the mean time for the payment of several debts due at different times.

1. In how many months will 12 gain as much as 5 pounds will gain in 6 months !

2. In how many months will 1£ gain as much as 40£ will gain in 15 months? L. K. 1.1.

3. In how many months will the use of 5£ be worth as much as the use of 1£ for 40 months?

4. Berrowed of a friend 1£ for 20 months; afterwards lent my friend 4£; how long ought he to keep it to become indemnified for the use of the 1£!

5. I have three notes against a man; one of 12£, due in 3 months; one of 9£, due in 5 months; and the other of 6£, due in 10 months; the man wishes to pay the whole at once; in what time ought he to pay it?

122 for 3 months is the same as 12 for 36 months, and 9£ for 5 months is the same as 1£ for 45 months, and 6£ for 10 months is the same as 1£ for 60 months.

27

He might; therefore, have 1.2 141 months, and he may

keep 27 pounds by part as long; that is, 14 = 5 months

ti- days, Answer:

Hence,—To find the mean time for several payments,—Rule: Multiply each sum by its time of payment, and divide the sum of the products by the sum of the payments,

and the quotient will be the answer.

Note. This rule is founded on the supposition, that what is gained by keeping a debt a certain time after it is due, is the same as what is lost by paying it an equal time before it is due; but, in the first case, the gain is evidently equal to the interest on the debt for the given time, while, in the second case, the loss is only equal to the discount of the debt for that time, which is always less than the interest; therefore, the rule is not exactly true. The error, however, is so trifling, in most questions that occur in business, as scarce to merit notice.

6. A merchant has owing to him $300\pounds$, to be paid as follows: $50\pounds$ in 2 months, $100\pounds$ in 5 months, and the rest in 8 months; and it is agreed to make one payment of the

whole: in what time ought that payment to be?

Ans. 6 months.

7. A owes B 136£, to be paid in 10 months; 96£ to be paid in 7 months; and 260£ to be paid in 4 months; what is the equated time for the payment of the whole?

Ans. 6 months, 7 days+.

1,482 July 150 150 1 15 15

8. A owes B 600£, of which 200£ is to be paid at the present time, 200 in 4 months, and 200 in 8 months; what is the equated time for the payment of the whole?

Ans: 4 months.

9: A owes B 200£, to be paid as follows: \(\frac{1}{3} \) in 3 months, \(\frac{1}{3} \) in 4 months, and the rest in 6 months: what is the equated time?

Ans. 4\(\frac{1}{3} \) months,

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THE RELATION OF NUMBERS.

187. 1. What part of 1 gallon is 3 quarts 1 1 gallon is 4 quarts, and 3 quarts is 3 of 4 quarts. Ans 3 of a gal.

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2. What part of 3 quarts is 1 gallon? 1 gallon, being 4 quarts, is 4 of 3 quarts; that is, 4 quarts is 1 time 3 quarts and 4 of another time.

Ans. 4=14.

3. What part of 5 bushels is 12 bushels !

Finding what part one number is of another is the same as finding what is called the ratio, or relation of one number to another; thus, the question, What part of 5 bushels is 12 bushels? is the same as What is the ratio of 5 bushels to 12 bushels? The answer is \$2-22.

Ratio, therefore, may be defined, the number of times one number is contained in another; or, the number of times one quantity is contained in another quantity of the same

kind.

4. What part of 8 yards is 13 yards? or, What is the ra-

tio of 8 yards to 13 yards !

13 yards is $\frac{1}{8}$ of 8 yards, expressing the division fractionally. If now we perform the division, we have for the ratio $1\frac{5}{8}$; that is, 13 yards is 1 time 8 yards, and $\frac{3}{8}$ of another time.

We have seen, (¶ 15, sign,) that division may be expressed fractionally. So also the ratio of one number to another, or the part one number is of another, may be expressed fractionally, to do which, make the number which is called the part, whether it be the larger or the smaller number, the numerator of a fraction, under which write the other number for a denominator. When the question is, What is the ratio, &c.? the number last named is the part; consequently it must be made the numerator of the fraction, and the number first named the denominator.

5. What part of 12 pounds is 11 pounds 1 or, 11 pounds is what part of 12 pounds? 11 is the number which expresses the part. To put this question in the other form, viz. What is the ratio, &c. let that number, which expresses the part, be the number last named; thus, What is the ratio of 12 pounds to 11 pounds?

Ans. 44

6. What part of 1£ is 2s. 6d. ? or, What is the ratio of

1£ to 2s. 6d.?

1£=240 pence, and 2s. 6d=30 pence; hence, $\frac{30}{240} = \frac{1}{6}$ is the Answer.

7. What part of 13s. 6d. is 1£ 10s. or, What is the ratio of 13s. 6d. to 1£ 10s. 1 Ans. $\frac{20}{9}$.

8. What is the ratio of 3 to 51 -- of 5 to 31 -- of 7

to 19! — of 19 to 7? — of 15 to 90? — of 90 to 15!
— of 84 to 160; — of 160 to 84! — of 615 to 1107?
— of 1107 to 615!

Ans. to the last §.

PROPORTION :

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THE RULE OF THREE

88. 1. If a piece of cloth, 4 yards long, cost 12£, what will be the cost of a piece of the same cloth 7 yards long?

2. If a horse travel 30 miles in 6 hours, how many miles

will he travel in 11 hours at that rate ?

1 10, 11,11,11

11 hours is 3 of 6 hours, that is, 11 hours is 1 time 6 hours, and 3 of another time; consequently, he will travel, in 11 hours, 1 time 30 miles, and 3 of another time, that is, the ratio between the distances will be equal to the ratio between the times.

of 30 miles; that is, 30 × 1 = 3 = 55 miles. If, then, no error has been committed, 55 miles must be 4 of 30 miles. This is actually the case; for 48 = 4.

Ans. 55 miles

Quantities which have the same ratio between them are said to be proportional. Thus, these four quantities,

hours, hours, miles, miles,

written in this order, being such, that the second contains the first as many times as the fourth contains the third, that

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contains ird, that is, the ratio between the third and fourth being equal to the ratio between the first and second, form what is called a proportion,

It follows, therefore, that proportion is a combination of two equal ratios. Ratio exists between two numbers; but pro-

portion requires at least three.

To denote that there is a proportion between the numbers 6, 11, 30, and 55, they are written thus :--

6:11::30:55

which is read, 6 is to 11 as 30 is to 55; that is, 6 is the same part of 11 that 30 is of 55; or, 6 is contained in 11 as many times as 30 is contained in 55; or, lastly, the ratio or relation of 11 to 6 is the same as that of 55 to 30.

The first term of a ratio, or relation, is called the antecedent, and the second the consequent. In a proportion there are two antecedents, and two consequents, viz. the antegedent of the first ratio, and that of the second; the consequent of the first ratio, and that of the second. In the preportion 6:11::30:55, the antecedents are 6, 30: the consequents, 11, 55.

The consequent, as we have already seen, is taken for the numerator, and the antecedent for the denominator of the fraction, which expresses the ratio or relation. first ratio is $\frac{1}{6}$, the second $\frac{5}{3} = \frac{1}{6}$; and that these two ratios are equal, we know, because the fractions are equal.

The two fractions 11 and 35 being equal, it follows that. by reducing them to a common denominator, the numerator of the one will become equal to the numerator of the other. and, consequently, that 11 multiplied by 30 will give the same product as 55 multiplied by 6. This is actual. the case; for 11×30=330, and 55×6=330. Hence it follows. -If four numbers be in proportion, the product of the first and last, or of the two extremes, is equal to the product of the second and third, or of the two means.

Hence it will be easy, having three terms in a proportion given, to find the fourth. Take the last example. Knowing that the distances travelled are in proportion to the times or hours occupied in travelling, we write the proportion thus : .. or vilesed at dolor

hours, hours, miles, miles, 6:11 :: 30,:

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Now, since the product of the extremes is equal to the product of the means, we multiply together the two means, 11, and 30, which makes 330, and, dividing this product by the known extreme, 6, we obtain for the result 55, that is 55 miles, which is the other extreme, or term, sought.

3. At 54£ for 36 barrels of flour, how many barrels may be purchased for 186£?

In this question, the unknown quantity is the number of barrels bought for 186£, which ought to contain the 36 barrels as many times as 186£contains 54£; we thus get the following proportion:

54 : 186 : 36	barrels. berrel	
1116 558		
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The product 6696, of the two means, divided by 54, the known extreme, gives 124 barrels for the other extreme, which is the term sought, or Answer.

Any three terms of a proportion being given, the operation by which we find the fourth is called the *Rule of Three*. A just solution of the question will sometimes require, that the order of the terms of proportion be changed. This may be done, provided the terms be so placed, that the product of the extremes shall be equal to that of the means.

4. If 3 men perform a certain piece of work in 10 days, how long will it take 6 men to do the same !

The number of days in which 6 men will do the work, being the term sought, the known term of the same kind, viz. 10 days, is made the third term. The two remaining terms are 3 men and 6 men, the ratio of which is §. But the more* men there are employed in the work, the less time will

The rule of three has sometimes been divided into direct and inverse, a distinction which is totally useless. It may not however be amiss to explain, in this place, in what this distinction consists.

The Rule of Three Direct is when more requires more, or less ro

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ect and inowever be inta. or less re be required to do it; consequently, the days will be less in proportion as the number of men is greater. There is still a proportion in this case, but the order of the terms is inverted; for the number of men in the second set, being two times that in the first, will require only one half the time. The first number of days, therefore, ought to contain the second as many times as the second number of men contains the first. This order of the terms, being the reverse of that assigned to them in announcing the question, we say, that the number of men is in the inverse ratio of the number of days. With a view, therefore, to a just solution of the question, we reverse the order of the two first terms, (in doing which we invert the ratio,) and, instead of writing the proportion, 3 men: 6 men, $(\frac{6}{3})$ we write it, 6 men: 3 men, $(\frac{2}{3})$ that is,

men. men. days. days. 6 : 3 :: 10 : ...

Note. We invert the ratio when we reverse the order of the terms in the proportion, because then the antecedent takes the place of the consequent, and the consequent that of the antecedent; consequently, the terms of the fraction which express the ratio are inverted; hence the ratio is inverted. Thus, the ratio expressed by \$\frac{3}{3}=2\$, being inverted, is \$\frac{3}{2}=1\$.

Having stated the proportion as above, we divide the product of the means, (10×3=30,by) the known extreme, 6, which gives 5, that is, 5 days, for the other extreme, or term sought.

Ans. 5 days.

From the examples and illustrations now given, we deduce the following general

quires less, as in this example:—If 3'men dig a trench 48 feet long in a certain time, how many feet will 12 men dig in the same time? Here it is obvious, that the more men there are employed, the more work will be done; and therefore, in this instance, more requires more. Again:—If 6 men dig 48 feet in a given time, how much will 3 men dig in the same time? Here less requires less, for the less men there are employed, the less work will be done.

The Rule of Three Inverse is when more requires less, or less requires more, as in this example:—If 6 men dig a certain quantity of trench in 14 hours, how many hours will it require 12 men to dig the same quantity? Here more requires less; that is, 12 men being more than 6, will require less time. Again:—If 6 men perform a piace of work in 7 days, how long will 3 men be in performing the same work? Here less requires more; for the number of men, being less will require more time.

RULE.

Of the three given numbers, make that the third term which is of the same kind with the answer sought. Then consider, from the nature of the question, whether the answer will be greater or less than this term. If the answer is to be greater, place the greater of the two remaining numbers for the second term, and the less number for the first term; but if it is to be less, place the less of the two remaining numbers for the second term, and the greater for the first; and, in either case, multiply the second and third terms together, and divide the product by the first for the answer, which will always be of the same denomination as the third term.

Note 1. If the first and second terms contain different denominations, they must both be reduced to the same denomination.

If 8 yards of cloth cost 12 4s, what will 364 qrs. cost?

yds. | qrs. | attractor | water to east

Reduce 8 yards and 364 quarters to the same denomination, by dividing the 364 quarters by 4, which will bring it into yards. 364 = 91.

yds. yds. 8 : 91 :: 1£4s.

Note 2. If the third term be a compound number, it must either be reduced to integers of the lowest denomination, or the low denominations must be reduced to a fraction of the highest denomination contained in it.

yards. yards. 8: 91 :: 1£ 4s.

24 4

Now multiply the 24s. by 91, and divide the product by 8; the answer will be shillings, which can be reduced to pounds.

Or, the 4s. can be reduced to the fraction of a pound; 4s.

Or, we can reduce the 4s. to the decimal of a pound;

20)40 which, annexed to the 1£, is equal to 12£.

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The first method is most usually practised.

Note 3. The same rule is applicable, whether the given quantities be integral, fractional, or decimal.

EXAMPLES FOR PRACTICE.

5. If 6 horses consume 21 bushels of oats in 3 weeks, how many bushels will serve 20 horses the same time ? Ans. 70 bushels.

6. The above question reversed. If 20 horses consume 70 bushels of oats in 3 weeks, how many bushels will serve 6 horses the same time ? Ans. 21 bushels.

7. If 365 men consume 75 barrels of provisions in 9 months, how much will 500 men consume in the same time !

Ans. 10244 barrels.

8. If 500 men consume 10244 barrels of provisions in 9 months, how much will 365 men consume in the same time? Ans. 75 barrels.

9. A goldsmith sold a tankard for 10£ 12s. at the rate of 5s. 4d. per ounce; I demand the weight of it.

Anv. 39 oz. 15 pwt.

10. If the moon move 13° 10' 35" in 1 day, in what time does it perform one revolution? Ans. 27 days, 7 h. 43 m.

11. If a person, whose rent is 33£, pay 3£ 2s. parish taxes, how much should a person pay whose rent is 97£?

Ans. 9£ 2s. 249d.

12. If I buy 7lbs. of sugar for 3s. 9d., how many pounds can I buy for 1£ 10s.

13. If 2 lbs. of sugar cost 1s. 3d., what will 100 lbs. of coffee cost, if 8 lbs. of sugar are worth 5 lbs. of coffee !

14. If I give 6£ for the use of 100£ for 12 months, what must I give for the use of 983£ the same time?

Ans. 58 28 £.

15. There is a cistern which has 4 pipes; the first will fill it in 10 minutes, the second in 20 minutes, the third in 40 minutes, the fourth in 80 minutes; in what time will all four, running together, fill it ?

 $\frac{1}{10} \pm \frac{1}{20} + \frac{1}{40} + \frac{1}{10} = \frac{1}{10}$ cistern in 1 minute.

Ans. 51 minutes.

16. If a family of 10 persons spend 3 bushels of mait in a month, how many bushels will serve them when there are 30 in the family 1 Ans. 9 bushels.

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Note. The rule of proportion, although of frequent use, is not of indispensable necessity; for all questions under it may be solved on general principles, without the formality of a proportion; that is, by analysis, as already shown, ¶ 62, ex. 1. Thus, in the above example,—If 10 persons spend 3 bushels, 1 person, in the same time, would spend $\frac{1}{10}$ of 3 bushels, that is, $\frac{1}{10}$ of a bushel; and 30 persons would spend 30 times as much, that is, $\frac{2}{10} = 9$ bushels, as before.

17. If a staff, 5 ft. 8 in. in length, cast a shadow of 6 feet, how high is that steeple whose shadow measures 153 feet?

Ans. 1444 feet.

18. The same by analysis. If 6 ft. shadow require a staff of 5 ft. 8 in. = 68 in., 1 ft. shadow will require a staff of $\frac{1}{6}$ of 68 in. or $\frac{6}{6}$ in.; then 153 ft. shadow will require 153 times as much; that is, $\frac{6}{6}$ × 153 = $\frac{104}{6}$ 04 = 1734 in. = 144 $\frac{1}{2}$ ft., as before.

19. If 3£ sterling be equal to 34£ Halifax, how much

Halifax is equal to 1000£ sterling?

Ans. 1111£ 2s. 23d.

20. If 1111£ 2s. $2\frac{3}{2}d$. Halifax, be equal to 1000£ sterling, how much sterling is equal to $3\frac{1}{2}£$ Halifax? Ans. 3£.

21. If 1000£ sterling be equal to 1111£ 2s. 23d Halifax, how much Halifax is equal to 3£ sterling? Ans. 34£.

22. If 3£ sterling be equal to 3½ Halifax, how much sterling is equal to 1111£ 2s, 24d. Halifax.

Aus. 1000£.

23. Suppose 2000 soldiers had been supplied with bread sufficient to last them 12 weeks, allowing each man 14 ounces a day; but, on examination, they find 105 barrels, containing 200 lbs. each, wholly spoiled; what must the allowance be to each man, that the remainder may last them the same time?

Ans. 12 cz. a day.

24. Suppose 2000 soldiers were put to an allowance of 12 oz. of bread per day for 12 weeks, having a seventh part of their bread spoiled; what was the whole weight of their

bread, good and bad, and how much was spoiled !

Ina. Spoiled, - - 21000 lbs.

25. — 2000 soldiers, having lost 105 barrels of bread, weighing 200 lbs. each, were obliged to subsist on 12 oz. a day for 12 weeks; had none been lost, they might have

quent use, as under it formality own, ¶ 62, sons spend pend To of sons would, as before.

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147000 lbs. 21000 lbs. els of bread, on 12 oz. a might have had 14 oz. a day; what was the whole weight, including what was lost, and how much had they to subsist on ?

Ans. Whole weight, 147000 lbs. Left, to subsist on, 126000 lbs.

26. — 2000 soldiers, after losing one seventh part of their bread, had each 12 oz. a day for 12 weeks; what was the whole weight of their bread, including that lost, and how much might they have had per day, each man, if none had been lost?

(Whole weight, 147000 lbs.

Ans. Loss, ... 21000 lbs.

27. There was a certain building raised in 8 months by 120 workmen; but, the same being demolished, it is required to be built in 2 months; I demand how many men must be employed about it.

Ans. 480 men.

28. There is a cistern having a pipe which will empty it in 10 hours, how many pipes of the same capacity will empty it in 24 minutes?

Ans. 25 pipes.

29. A garrison of 1200 men has provisions for 9 months, at the rate of 14 oz. per day; how long will the provisions last, at the same allowance, if the garrison be reinforced by 400 men?

Ans. 63 months.

30. If a piece of land, 40 rods in length and 4 in breadth, make an acre, how wide must it be when it is but 25 rods long?

Ans. 62 rods.

31. If a man perform a journey in 15 days when the days are 12 hours long, in how many will he do it when the days are but 10 hours long?

Ans. 18 days.

32. If a field will feed 6 cows 91 days, how long will it feed 21 cows?

33. Lent a friend 292£ for 6 months; some time after, he lent me 806£; how long may I keep it to balance the favor?

Ans. 2 months 5 + days.

34. If 30 men can perform a piece of work in 11 days, how many men will accomplish another piece of work, 4 times as big, in a fifth part of the time?

Ans. 600 men.

35. If 11 lb. of sugar cost 75 of a shilling, what will 13 of a lb. cost 1 Ans. 4d. 34814q.

Note. See ¶ 62, ex. 1, where the above question is solved by analysis. The eleven following are the next succeeding examples in the same ¶.

- 36. If 7 lbs. of sugar cost 2 of 5s., what cost 19 lbs.
- 37. If 61 yds. of cloth cost 3£, what cost 91 yds 1

 Ans. 4£ 5s. 44d.
- 38. If 2 oz. of silver cost 11s. 25d. what costs 4 oz. 1
- Ans. 4s. 2\$\frac{2}{3}\text{d}. If \$\frac{4}{2}\text{ oz. cost \$4\frac{7}{12}\text{s}\$, what costs \$1\text{ oz. ?}\$ Ans. 6s. 5d.
- 40. If \(\frac{1}{3} \) lb. less by \(\frac{1}{6} \) lb. cost 13\(\frac{1}{6} \), what cost 14 lbs, less by \(\frac{1}{6} \) of 2 lbs, ?

 Ans. 4\(\mathcal{L} \) 9s. 9\(\frac{1}{2} \) d.
 - 41. If 3 yd. cost 7£, what will 401 yds. cost?
 - Ans. 59£ 1s. $2\frac{1}{4}$ d, 42. If $\frac{7}{16}$ of a ship cost 251£, what is $\frac{3}{3}$ 2 of her worth?

 Ans. 53£ 15s. 84d.
 - 43. At 34£ per cwt, what will 94 lbs, cost ?
 - Ans. 6s. 355d.
- 44. A merchant, owning $\frac{1}{2}$ of a vessel, sold $\frac{3}{2}$ of his share for $957\pounds$; what was the vessel worth? Ans. $1794\pounds$ 7s. 6d.
- 45. If § yd. cost \$£, what will 15 of an ell English cost?

 Ans. 17s. 1d. 25q.
- 46. A merchant bought a number of bales of velvet, each containing \$2914 yds., at the rate of 7£ for 5 yds., and sold them cut at the rate of 11£ for 7 yds., and gained 200£ by the pargain; how many bales were there? Ans. 9 bales.
- 47. At 9£ for 6 barrels of flour, what must be paid for 178 barrels?

 Ans. 267£.
- 48. At 9s. 6d. for 3 cwt. of hay, how much is that per ton?

 Ans. 3£ 3s. 4d.
- 49. If 2.5 lbs. of tobacco cost 75 cents, how much will 185 lbs. cost? Ans. \$5.55
- 50. What is the value of '15 of a hogshead of lime, at 11s. 114d per hhd. ?

 Ans. 1s. 94d.
- 51. If '15 of a hhd. of lime cost 1s. 92d., what is it per hhd. ? Ans. 11s. 112d.

COMPOUND PROPORTION.

- T 90. It frequently happens, that the relation of the quantity required, to the given quantity of the same kind, depends upon several circumstances combined together; it is then called Compound Proportion or Double Rule of Three.
 - 1. If a man travel 273 miles in 13 days, travelling only

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5s. 81d.

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bs. 7 hours in a day, how many miles will he travel in 12 days, if he travel 10 hours in a day?

Thus question may be solved several ways. First by

This question may be solved several ways. First by analysis:—

If we knew how many miles the man travelled in 1 hour it is plain, we might take this number 10 times, which would be the number of miles he would travel in 10 hours, or in L of these long days, and this again, taken times, would be the number of miles he would travel in 10 hours each day.

If he travel 273 miles in 13 days, he miles; that is $^{2}1_{3}^{3}$ miles, in 1 day of 7 hours, and $\frac{1}{2}$ of $^{2}1_{3}^{3}$ miles is $^{2}1_{3}^{3}$ miles, the distance he travels in 1 hour: then, 10 times $^{2}1_{3}^{3} = ^{2}1_{3}^{3}$ miles, the distance he travels in 10 hours; and 12 times $^{2}1_{3}^{3} = ^{3}1_{3}^{3} =$

But the object is to show how the question may be solved by proportion:

First; it is to be regarded, that the number of miles travelled over depends upon two circumstances, viz. the number of days the man travels, and the number of hours he travels each day.

We will not at first consider this latter cirsumstance, but suppose the number of hours to be the same in each case: the question then will be,—If a man travel 273 miles in 13 days, how many miles will be travel in 12 days? This will furnish the following proportion:—

13 days : 12 days : : 273 miles : miles

which gives for the fourth term, or answer, 252 miles.

Now, taking into consideration the other circumstance, or that of the hours, we must say,—If a man, travelling 7 hours a day for a certain number of days, travels 252 miles, hoto far will he travel in the same time, if he travel 10 hours in a day?

This will lead to the following proportion :-

7 hours : 10 hours : : 252 miles : miles.

This gives for the fourth term, or answer, 360 miles.

We see, then, that 273 miles has to the fourth term, or answer, the same proportion that 13 days has to 12 days,

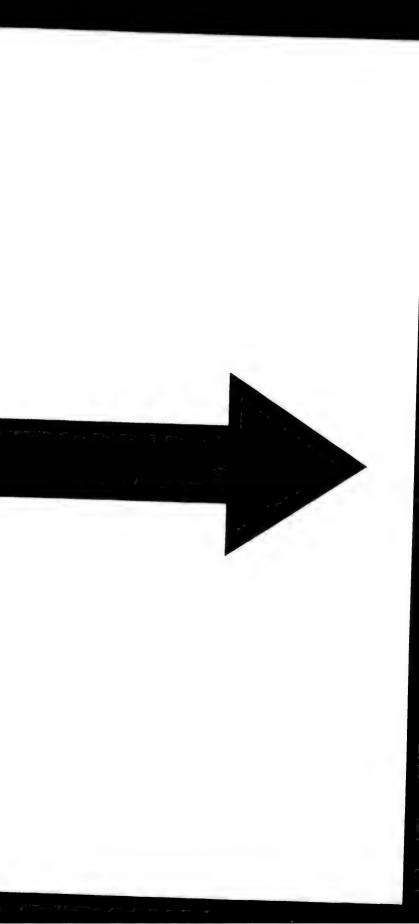
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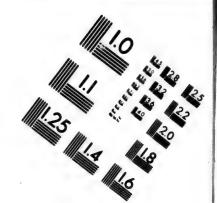
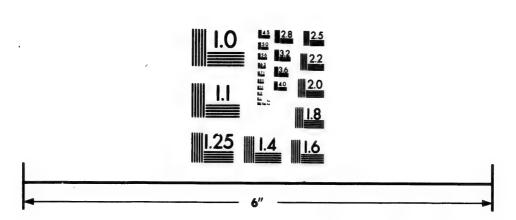


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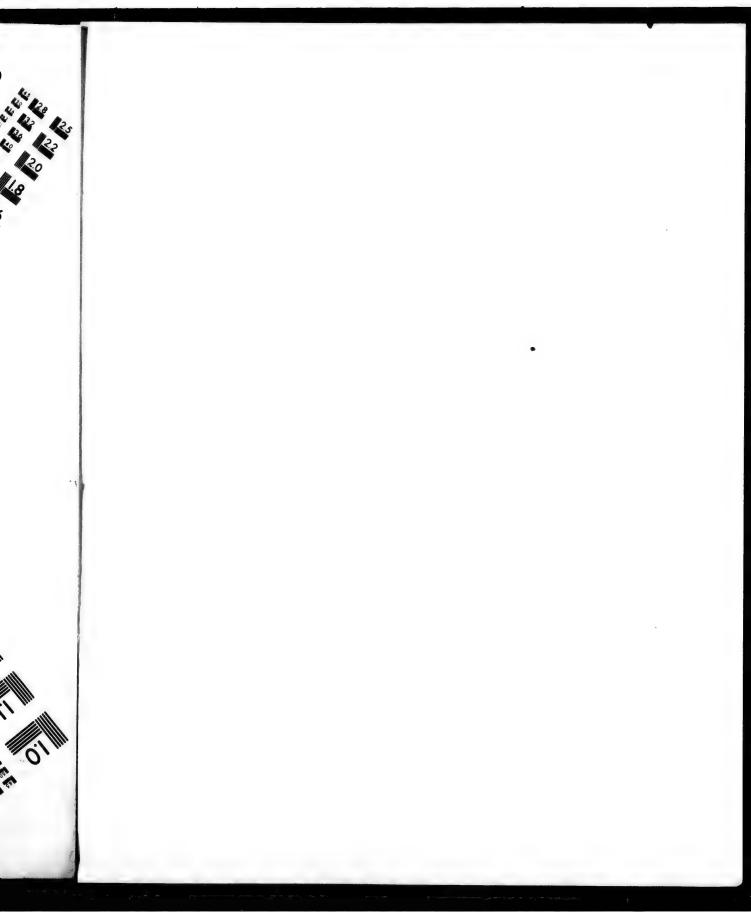


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and that 7 hours has to 10 hours. Stating this in the form of a proportion, we have.

13 days : 12 days 7 hours : 10 hours 2 :: 273 miles : miles

by which it appears, that 273 is to be multiplied by both 12 and 10; that is, 273 is to be multiplied by the product of 12×10, and divided by the product of 13×7, which, being done, gives 360 miles for the fourth term, or answer, as before.

In the same manner, any question relating to compound proportion, however complicated, may be stated and solved.

2. If 248 men, in 5 days, of 11 hours each, can dig a trench 230 yards long, 3 wide, and 2 deep, in how many days, of 9 hours each, will 24 men dig a trench 420 yards

long, 5 wide and 3 deep ?

Here the number of days, in which the proposed work can be done, depends on five circumstances, viz. the number of men employed, the number of hours they work each day, the length, breadth, and depth of the trench. We will consider the question in relation to each of these circumstances, in the order in which they have been named:—

1st. The number of men employed. Were all the circumstances in the two cases alike, except the number of men and the number of days, the question would consist only in finding in how many days 24 men would perform the work which

248 men had done in 5 days; we should then have

24 men : 248 men : : 5 days : days.

2d. Hours in a day. But the first laborers worked 11 hours in a day, whereas the others worked only 9; less hours will require more days, which will give

9 hours : 11 hours : : 5 days : days.

3d. Length of the ditches. The ditches being of unequal length, as many more days will be necessary as the second is longer than the first; hence we shall have

230 length: 420 length: 5 days: days.
th. Widths. Taking into consideration the widths,

which are different, we have

3 wide : 5 wide : : 5 days : days.

5th. Depthe. Lastly, the depths being different, we have 2 deep : 3 deep : 5 days : days.

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It would seem, therefore, that 5 days has to the fourth term, or answer, the same proportion

Men, 24: 248
Hours, 9: 11
Length, 230: 420
Width, 3: 5
Depth, 2: 3

¶ 91. The continued product of all the second terms $248 \times 11 \times 420 \times 5 \times 3$, multiplied by the third term, 5 days, and this product divided by the continued product of the first terms, $24 \times 9 \times 230 \times 3 \times 2$, gives 288.84860 days for the fourth term, or answer. 288.529.

But the first and second terms are the fractions 245, 1, 1, 220, 3 and 2, which express the ratios of the men, and of the hours, of the lengths, widths and depths of the two ditches. Hence it follows, that the ratio of the number of days given to the number of days sought, is equal to the product of all the ratios, which result from a comparison of the terms relating to each circumstance of the question.

The product of all the ratios is found by multiplying together the fractions which express them, thus,

 $248 \times 11 \times 420 \times 5 \times 3$ 17186400, and this fraction, 298080 represents the ratio of the quantity required to the given quantity of the same kind. A ratio resulting in this manner, from the multiplication of several ratios, is called a compound ratio.

From the examples and illustrations now given we deduce the following general

RULE

for solving questions in compound proportion, or double rule of three, viz.—Make that number which is of the same kind with the required answer, the third term; and, of the remaining numbers, take away two that are of the same

kind, and arrange them according to the directions given in simple proportion; then, any other two of the same kind, and so on till all are used.

Lastly, multiply the third term by the continued product of the second terms, and divide the result by the continued product of the first terms, and the quotient will be the fourth term, or answer required.

EXAMPLES FOR PRACTICE.

1. If 6 men build a wall 20 feet long, 6 ft. high, and 4 ft. thick in 16 days, in what time will 24 men build one 200 ft. long, 8 ft. high, and 6 ft thick?

Ans. 80 days.

2. If the freight of 9 hlds. of sugar, each weighing 12 cwt. 20 leagues, cost 16£, what must be paid for the freight of 50 tierces, each weighing 2½ cwt. 100 leagues?

Ans. 92£ 11s. 10gd.

3. If 56 lb. of bread be sufficient for 7 men 14 days, how much bread will serve 21 men 3 days?

Ans. 36 lbs.

The same by analysis. If 7 men consume 56 lbs. of bread, 1 man, in the same time, would consume \$\frac{1}{2}\$ of 56 lbs. = \$\frac{1}{2}\$ lbs.; and if he consume \$\frac{1}{2}\$ lbs. in 14 days, he would consume \$\frac{1}{4}\$ of \$\frac{1}{2}\$ = \$\frac{1}{2}\$ lb. in 1 day. 21 men would consume 21 times so much as 1 man; that is, 21 times \$\frac{1}{2}\$ = \$\frac{1}{2}\$ lbs. in 1 day, and in 3 days the ould consume 3 times as much; that is, \$\frac{1}{2}\$ = equal lbs. as before.

Ans. 36 lbs.

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Note. Having wrought the following examples by the rule of proportion, let the pupil be required to do the same by analysis.

4. If 4 reapers receive 2£ 15s. 2½d. for 3 days' work, how many men may be hired 16 days for 25£ 15s. 2½d.?

Ans. 7 men.

5. If 7 oz. 5 pwt. of bread be bought for 43d, when corn is 4s. 2d. per bushel, what weight of it may be bought for 1s. 2d. when the price per bushel is 5s. 6d. 2.

Ans. 1 lb. 4 oz. 3478pwts.

6. If 100£ gain 6£ in 1 year, what will 400£ gain in 9 months?

Note. This and the three following examples reciprocally prove each other.

7. If 100£ gain 6£ in 1 year, in what time will 400£ gain 18£!

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8. If 400£ gain 18£ in 9 months, what is the rate per cent per annum 1

9. What principal, at 6 per cent per annum, will gain

18£ in 9 months ?

10. A usurer put out \$75 at interest, and at the end of 8 months, received, for principal and interest, \$79; I demand at what rate per cent, he received interest.

Ans. 8 per cent.

11. If 3 men receive $8_{10}^{9}\mathcal{L}$ for 19½ days' work, how much must 20 men receive for 100½ days?

Ans. 305£ 0s. 8d.

SUPPLEMENT TO THE SINGLE RULE OF THREE.

QUESTIONS.

1. What is proportion? 2. How many numbers are required to form a ratio? 3. How many to form a proportion? 4. What is the first term of a ratio called? 5— the second term? 6. Which is taken for the numerator, and which for the denominator of the fraction expressing the ratio? 7. How may it be known when 4 numbers are in proportion? 8. Having three terms in a proportion given, how may the fourth term be found? 9. What is the operation, by which the fourth term is found, called? 10. How does a ratio become inverted? 11. What is the rule in proportion? 12. In what denomination will the 4th term or answer, be found? 13. If the first and second terms contain different denominations, what is to be done? 14. What is compound proportion, or double rule of three? 15. Rule?

EXERCISES.

1. If I buy 76 yards of cloth for 28£ 5s. 10d. for 28£ has. 9s. 34d.

2. Bought 4 pieces of Holland, each containing 24 ells English for 24£; how much was that per yard?

Ans. 49.

3. A garrison had provision for 8 months, at the rate of 15 ounces to each person per day; how much must be allowed per day, in order that the provision may last 94 months?

Ans. 1212 oz.

4. How much land at 12s. 6d. per acre, must be given

in exchange for 360 acres, at 18s. 9d. per acre !

Ans. 540 acres.

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5. Borrowed 185 quarters of corn when the price was 19s.; how much must I pay when the price is 17s. 4d. ?

6. A person owning $\frac{3}{4}$ of a coal mine, sells $\frac{3}{4}$ of his share for $171\pounds$; what is the whole mine worth $\frac{3}{4}$. $\frac{380£}{4}$.

7. If \$\frac{1}{2}\$ of a gallon cost \$\frac{1}{2}\$ of a pound, what costs \$\frac{1}{2}\$ of a tun?

Ans. 140£.

8. At 1½£ per cwt. what cost 3½ lbs. ? Ans. 104d.

9. If 4½ cwt. can be carried 36 miles for 35 shillings, how many pounds can be carried 20 miles for the same money?

Ans. 9074 lbs.

10. If the sun appears to move from east to west 360 degrees in 24 hours, how much is that in each hour?—— in each minute?—— in each second?

Ans. to the last, 15" of a deg.

11. If a family of 9 persons spend 112£ 10s. in 5 months, how much would be sufficient to maintain them 8 months if 5 persons more were added to the family 4. Ans. 280£.

Note. Exercises 14th, 15th, 16th, 17th, 18th, 19th and 20th, "Supplement to Fractions," afford additional examples in single and double proportion, should more examples be thought necessary.

PULLOWSHIP.

¶ 92. 1. Two men own a farm; the first owns $\frac{1}{4}$, and the second owns $\frac{3}{4}$ of it; the farm is sold for 40£; what is each man's share of the money?

2. Two men purchase a horse for 20 pounds, of which one pays 5 pounds, and the other 15 pounds; the horse is sold for 40 pounds; what is each man's share of the money?

3. A and B bought a quantity of cotton; A paid 100 pounds, and B 200 pounds; they sold it so as to gain 30 pounds; what were their respective shares of the gain?

The process of ascertaining the respective gains or losses of individuals, engaged in joint trade, is called the Rule of Fellowship.

The money, or value of the articles employed in trade, is called the Capital, or Stock; the gain or loss to be shared is called the Dividend.

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It is plain, that each man's gain or loss ought to have the same relation to the whole gain or loss, as his share of the stock does to the whole stock.

Hence we have this Rule:—As the whole stock: to each man's share of the stock: the whole gain or loss: his share of the gain or loss.

4. Two persons have a joint stock in trade; A put in 250£, and B 350£; they gain 400₺; what is each man's share of the profit?

OPERATION.

A's stock, 250£ } Then,

B's stock, 350 | 600 : 250 :: 400 : 166£ 13s. 4d. A's g. Whole stock, 600£ | 600 : 350 :: 400 : 233£ 6s. 7d. B's g.

The pupil will perceive, that the process may be contracted by cutting off an equal number of ciphers from the first and second, or first and third terms; thus, 6:250::4:166£ 13s. 4d. &c.

It is obvious, the correctness of the work may be ascertained by finding whether the sums of the shares of the gains are equal to the whole gain; thus, 166£ 13s. 4d.+233£ 6s. 7d.—400£, the whole gain.

5. A, B and C trade in company; A's cipital was 175£, B's 200£, and C's 500£; by misfortune they lose 250£; what loss must each sustain? 50£, A's loss.

Ans. 57£ 2s. 101d. B's loss.

142£ 17s. 14d. C's loss.

6. Divide \$600 among 3 men so that their shares may be to each other as 1, 2, 3, respectively.

Ans. \$100, \$200, and \$300.

7. Two merchants, A and B, loaded a ship with 500 hhds. of rum; A loaded 350 hhds. and B the rest; in a storm the seamen were obliged to throw overboard 100 hhds.; how much must each sustain of the loss?

Ans. A 70, and B 30 hhds.

8. A and B companied; A put in 45£, and took out \$\frac{3}{2}\$ of the gain; how much did B put in?

Ans. 30£.

Note. They took out in the same proportion as they put in; if 3 fifths of the stock is 45.5 how much is 2 fifths of it?

9. A and B companied, and trade with a joint capital of

wns $\frac{1}{4}$, and ϵ ; what is

of which the horse is he money? A paid 100 to gain 30 he gain?

ins or losses he Rule of

in trade, is be shared 400£; A receives, for his share of the gain, $\frac{1}{2}$ as much as B; what was the stock of each?

Ans. { 133£ 6s. 7d. A's stock. 266£ 13s. 4d. B's stock.

10. A bankrupt is indebted to B \$780, to C \$460, and to D \$760; his estate is worth only \$600; how must it be divided?

Note. The question evidently involves the principles of fellowship, and may be wrought by it

Ans. B \$234, C 138, and D \$228.

11. B and C venture equal stocks in trade, and clear 164£; by agreement, B was to have 5 per cent of the profits, because he managed the concerns; C was to have but 2 per cent; what was each one's gain? and how much did B receive for his trouble?

Ans. B's gain was 117£ 2s. 104d. and C's 46£ 17s. 14d.

and B received 70.5 5s. 83d. for his trouble.

12. A cotton factory, valued at 12000£, is divided into 100 shares; if the profits amount to 15 per cent. yearly, what will be the profit accruing to 1 share? — to 2 shares? — to 25 shares? — Ans. to the last 450£.

13. In the above-mentioned factory, repairs are to be made which will cost 340£; what will be the tax, on each share, necessary to raise the sum? — on 2 shares? — on 3 shares? — Ans. to the last 34£.

14. If a town raise a tax of $1850\pounds$, and the whole town be valued at $37000\pounds$, what will that be on 1£? What will be the tax of a man whose property is valued at 1780£?

Ans. 1s. on a pound, and 89£ on 1780£.

ventory of the property, both real and personal, of the whole town, and also of the whole number of the polls 1 and, as the polls are rated at so much each, we must first take out from the whole tax what the polls amount to, and the remainder is to be assessed on the property. We may then find the tax upon 1£ and make a table containing the tixes on 1, 2, 3, &c. to 10£; then on 20, 30, &c. to 100£; and then on 100, 200, &c. to 1000£. Then knowing the inventory of any individual, it is easy to find the tax upon his property.

15. A certain town, valued at 64530£, raises a tax of

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2259£ 18s.; there are 540 polls, which are taxed 3s. each; what is the tax on a pound, and what will be B's tax, whose real totale is valued at 1340£, his personal property at 874£, and who pays for 2 polls.

It will be better in questions relating to the assessment of taxes to use decimals, as we have done in interest. The process will be shorter, and the result will be obtained with exactness. The shillings, therefore, in the given values, will be reduced to the decimal of a pound, and the table will be male out decimally, and the decimal parts in the final

answer can be reduced to shillings and pence. 540 \times '60 (3s.) = 324£, amount of the poll taxes, and 2259'90 (2259£ 18s.) -324£=1935'90, to be assessed on property 64530£: 1935'90 :: 1£'03; or, $\frac{19.3 \, 5.90}{64530}$ = '03, tax in 1£.

TABLE.

7	E	rt	£	* *	£	£	1,14 1	£	£
Tax	on I	is	'03	Tax on	10 is	'30	Tax on	100 is	36
	5	is	'06	66	20 is	'60	**	200 is	6
£€	1	is	'09	66	30 is	190	16.6	300 is	9.
66	- 4	is	12	et .	40 is	1'20	66	400 is	
46	4	is	15	**	50 is	1.50	**	500 is	
46	6	is	18	66	60 is	1'80	**	600 is	184
4.6	7	is	'21	**	70 is	2.10	"	700 is	214
48	8	is	24		80 is	2'40	* * **	800 is	
46	9	is	27	**	90 is	2.70	* **	900 is	
		1	10 .		4 >< p2	17984	* *4"	1000 is	

Now, to find B's tax, his real estate being 1340£, I find, by the table, that

The tax on - 1000£ The tax on - 300 The tax on - 40	 is	•,	
Tax on his real estate In like manner I find the tax on		-	
property to be	 -	•	- 26/22
2 polls at '60 each, are	 •	,•	- 1'20

Amount, 67:62 67:62£=67£ 12s. 43d. Ans.

16. What will C's tax amount to, whose inventory is 874 dollars real, and 210 dollars personal property, and who pays for 3 polls?

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17. What will be the tax of a man, paying for 1 poll, whose property is valued at \$34'82? — at \$768? — at \$940? — at \$4657?

18. Two men paid 22 10s. for the use of a pasture 1 month; A kept in 24 cows, and B 16 cows; how much

should each pay 1

19. Two men hired a pasture for 2£ 10s.; A pet in 8 cows 3 months, and B put in 4 cows 4 months; how much should each pay?

T 94. The pasturage of 8 cows for 3 month, is the same as 24 cows for 1 month, and the pasturage of 4 cows for 4 months is the same as of 16 cows for 1 month. The shares of A and B, therefore, are 24 to 16, as in the former question. Hence, when time is regarded in fellowship,—Multiply each one's stock by the time he continues it in trade, and use the product for his share. This is called Double Fellowship.

Ans. A 1£ 10, and B 1£.

20. A and B enter into partnership; A pus in 100£6 months, and then puts in 50£ more; B pus in 200£4 months, and then takes out 80£; at the close of the year, they find that they have gained 95£; what is the profit of each?

Ans. \ 51£ 5s. 2d. B's share.

21. A. with a capital of $500\pounds$, began trad Jan. 1, 1826, and meeting with success, took in B as a partner, with a capital of $600\pounds$, on the first of March following; 4 months after, they admit C as a partner, who brought $800\pounds$ stock; at the close of the year, they find the gain to be $700\pounds$; how must it be divided among the partners?

Ans. \ 250£, A's share, \ 250£, B's share. \ 200£, C's share.

QUESTIONS.

1. What is fellowship? 2. What is the rule for operaing? 3. When time is regarded in fellowship, what is it called? 4. What is the method of operating in double fellowship? 5. How are taxes assessed? 6. How is fellowship proved?

abbigation.

T 95. Alligation is the method of mixing two or more simples, of different qualities, so that the composition may be of a mean, or middle quality.

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months is the rage of 4 cows 1 month. The as in the former llowslip,-Mulnuesit in trade, is cilled Double 10s. and B 1£. pum in 100£ 6 pus in 200£ 4 loss of the year, t i the profit of 2d. A's share. . 21. B's share. de Jan. 1, 1826, partner, with a wing; 4 months glt 800£ stock ; in to be $700\pounds$; 50.6, A's share,

for operating? 3. alled? 4. What is How are taxes as-

50£, B' share.

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o ing two or more nposition may be When the quantities and prices of the simples are given, to find the mean price of the mixture, compounded of them, the process is called Alligation Medial.

1. A farmer mixed together 4 bushels of wheat, worth 66 pence per bushel, 3 bushels of rye, worth 32 pence per bushel, and 2 bushels of corn, worth 28 pence per bushel; what is a bushel of the mixture worth?

It is plain, that the cost of the whole, divided by the number

of bushels, will give the price of one bushel.

4 bushels, at 66 pence, cost 264 pence.

3 " at 32 " 96

2 " at 28 " 56

9 bushels cost 416 pence.

 $^{4}1^{6} = 468$ pence, Ans.

2. A grocer mixed 5lbs. of sugar, worth 10 pence per lb. 8 lbs. worth 12 pence, 20 lbs. worth 14 pence; what is a pound of the mixture worth?

Ans. 124?d.

3. A goldsmith melted together 3 ounces of gold 20 carats fine, and 5 ounces 22 carats fine; what is the fineness of the mixture?

Ans. 214.

4. A grocer puts 6 gallons of water into a cask containing 40 gallons of rum, worth 2s. 7d. per gallon; what is a gallon of the mixture worth?

Ans. 2s. 244d.

5. On a certain day the mercury was observed to stand in the thermometer as follows; 5 hours of the day, it stood at 64 degrees; 4 hours, at 70 degrees; 2 hours, at 75 degrees, and 3 hours, at 73 degrees; what was the mean temperature for that day?

It is plain this question does not differ, in the mode of its operation, from the former.

Ans. 697 degrees.

- T 96. When the mean price or rate, and the prices or rates of the several simples are given, to find the proportions or quantities of each simple, the process is called Alligation Alternate; alligation alternate is, therefore, the reverse of alligation medial, and may be proved by it.
- 1. A man has corn worth 40 pence per bushel, which he wishes to mix with rye worth 50 pence per bushel, so that the mixture may be worth 42 pence per bushel; what proportions, or quantities of each, must be take?

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Had the price of the mixture required exceeded the price of the corn, by just as much as it fell short of the price of the rye, it is plain, he must have taken equal quantities of corn and rye; had the price of the mixture exceeded the price of the corn, by only & as much as it fell short of the price of the rye, the compound would have required 2 times as much corn as rye; and in all cases, the less the difference between the price of the mixture and that of one of the simples, the greater must be the quantity of that simple, in proportion to the other; that is, the quantities of the simples must be inversely as the differences of their prices from the price of the mixture; therefore, if these differences be mutually exchanged, they will, directly, express the relative quantities of each simple necessary to form the compound required. In the above example, the price of the mixture is 42 pence, and the price of the corn is 40 pence; consequently, the difference of their prices is 2 pence; the price of the rye is 50 pence, which differs from the price of the mixture by 8 pence. Therefore, by exchanging these differences, we have 8 bushels of corn to 2 bushels of rye, for the proportion required.

Ans. 8 bushels of corn to 2 bushels of rye, or in that

proportion.

The correctness of this result may now be ascertained by the last rule; thus, the cost of 8 bushels of corn, at 40 pence is 320 pence; and 2 bushels of rye, at 50 pence, is 100 pence; then, 320+100=420, and 420, divided by the number of bushels, (8+2,) = 10, gives 42 pence for the price of the mixture.

2. A merchant has several kinds of tea; some at 8 shillings, some at 9 shillings, some at 11 shillings, and some at 12 shillings per pound; what proportions of each must he mix, that he may sell the compound at 10 shillings per

pound?

Here we have 4 simples; but it is plain, that what has just been proved of two will apply to any number of pairs, if in each pair the price of one simple is greater, and that of the other less, than the price of the mixture required. Hence we have this

RULE.

The mean rate and the several prices being reduced to the same denomination,—connect with a continued line each ed the price

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price that is LEss than the mean rate with one or more that is GREATER, and each price GREATER than the mean rate with one or more that is LESS.

Write the difference between the MBAN rate, or price, and the price of EACH SIMPLE opposite the price with which it is connected; (thus the difference of the two prices in each pair will be mutually exchanged;) then the sum of the differences, standing against any price, will express the RELATIVE QUANTITY to be taken of that price.

By attentively considering the rule, the pupil will perceive, that there may be as many different ways of mixing the simples, and consequently as many different answers, as there are different ways of linking the several prices.

We will now apply the rule to solve the last question:-OPERATIONS.

$$10s \begin{cases} 8s. - \begin{vmatrix} 1 & 0 \\ 0 & -1 \\ -1 \\ 11s. - \begin{vmatrix} -1 \\ -1 \\ 12s. - \begin{vmatrix} -2 \\ -1 \\ -1 \\ 2s. - \end{vmatrix} \end{cases} Ans. 10s. \begin{cases} 8 - -2 + 1 = 3 \\ 9 - \begin{vmatrix} 1 & -1 \\ -1 + 2 = 3 \\ 12 - -2 & = 2 \end{cases} \end{cases}$$

Here we set down the prices of the simples, one directly under another, in order, from least to greatest, as this is most convenient, and write the mean rate, (10s.) at the left hand. In the first way of linking, we find, that we may take in the proportion of 2 pounds of the teas at 8 and 12s. to 1 pound at 9 and 11s. In the second way, we find for the answer, 3 pounds at 8 and 11s. to 1 pound at 9 and 12s.

3. What proportions of sugar, at 8 pence, 10 pence, and 14 pence per pound, will compose a mixture worth 12 pence per pound ?

Ans. In the proportion of 2lbs. at 8 and 10 pence to 6lbs. at 14 pence.

Note. As these quantities only express the proportions of each kind, it is plain, that a compound of the same mean price will be formed by taking 3 times, 4 times, one half, or any proportion, of each quantity. Hence,

When the quantity of one simple is given, after finding the proportional quantities, by the above rule, we may say, As the PROPORTIONAL quantity: is to the GIVER quantity 1: so is each of the other PROPORTIONAL quantities : to the RM-QUIRED quantities of each.

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4. If a man wishes to mix 1 gallon of brandy worth 16s. with rum at 9s. per gallon, so that the mixture may be worth 11s. per gallon, how much rum must he use ?

Taking the differences as above, we find the proportions to be 2 of brandy to 5 of rum; consequently, 1 gallon of brandy will require 24 gallons of rum?

Ans. 24 gallons.

5. A grocer has sugars worth 7 pence, 9 pence, and 12 pence per pound, which he would mix so as to form a compound worth 10 pence per pound; what must be the proportions of each kind?

Ans. 2lbs. of the first and second to 4lbs. of the third kind.

6. If he use 1lb. of the first kind, how much must be take of the others? —— if 4lbs. what? —— if 6lbs. what? —— if 20lbs. what?

Ans. to the last, 20lbs. of the second, and 40 of third.

7. A merchant has spices at 16d. 20d. and 32d. per pound; he would mix 5 pounds of the first sort with the others, so as to form a compound worth 24d. per pound; how much of each sort must be use?

Ans. 5lbs. of the second, and 75lbs. of the third.

8. How many gallons of water, of no value, must be mixed with 60 gallons of rum, worth 48 pence per gallon, to reduce its value to 42 pence per gallon? Ans. 8\$ gallons.

9. A man would mix 4 bushels of wheat, at 90 pence per bushel, rye at 70 pence, corn at 70 pence, and barley at 30 pence, so as to sell the mixture at 48 pence per bushel; how much of each may he use?

10. A goldsmith would mix gold 17 carats fine with some 19, 21, and 24 carats fine, so that the compound may be 22 carats fine; what proportions of each must be use?

Ans. 2 of the 3 first sorts to 9 of the last.

11. If he use loz. of the first kind, how much must he use of the others? What would be the quantity of the compound?

Ans. to last, 7½ ounces.

12. If he would have the whole compound consist of 15 oz., how much must he use of each kind? —— if of 30oz., how much of each kind? —— if of 37-joz., how much?

Ans. to last, 50z. of the 3 first, and 2210z. of the last. Hence, when the quantity of the compound is given, we may say, As the sum of the PROPORTIONAL quantities found by the ABOVE RULE, is to the quantity REQUIRED, so is each PROPORTIONAL quantity, found by the rule, to the REQUIRED quantity of EACH.

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13. A man would mix 100 pounds of sugar, some at 8 pence, some at 10 pence, and some at 14 pence per pound, so that the compound may be worth 12 pence per pound; how much of each kind must be use?

We find the proportions to be, 2, 2, and 6. Then, 2+2 +6=10, and (2:20lbs. at 8d.)

10 : 100 :: {2 : 20lbs. at 8d. } Ans. 6 : 60lbs. at 14d. }

14. How many gallons of water, of no value, must be mixed with brandy at 120 pence per gallon, so as to fill a vessel of 75 gallons, which may be worth 92 pence per gallon?

Ans. 17½ gallons of water to 57½ gallons of brandy.

15. A grocer has currents at 4d., 6d., 9d. and 11d per lb.; and he would make a mixture of 240lbs., so that the mixture may be sold at 8d. per lb.; how many pounds of each sort may he take !

Ans. 72, 24, 48, and 96lbs., or 48, 48, 72, 72, &c.

Note. This question may have five different answers.

QUESTIONS.

1. What is alligation? 2. — medial? 3. — the rule for operating? 4. What is alligation alternate? 5. When the price of the mixture, and the price of the several simples, are given, how do you find the proportional quantities of each simple? 6. When the quantity of one simple is given, how do you find the others? 7. When the quantity of the whole compound is given, how do you find the quantity of each simple?

DWODECLMALS.

1 97. Duodecimals are fractions of a foot. The word is derived from the Latin word duodecim, which signifies twelve. A foot, instead of being divided decimally into ten equal parts, is divided duodecimally into twelve equal parts, called inches, or primes, marked thus, ('). Again, each of these parts is conceived to be divided into twelve other equal parts, called seconds, ("). In like manner, each second is conceived to be divided into twelve equal parts, called thirds, (""); each third into twelve equal parts, called fourths, (""); and so on to any extent.

In this way of dividing a foot, it is obvious, that

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1' inch or prime is - - - - $\frac{1}{12}$ of a foot. 1" second is $\frac{1}{12}$ of $\frac{1}{12}$ - - = $\frac{1}{144}$ of a foot. 1" third is $\frac{1}{12}$ of $\frac{1}{12}$ of $\frac{1}{12}$ of $\frac{1}{12}$ of $\frac{1}{12}$ of a foot. 1"" fourth is $\frac{1}{12}$ of $\frac{1}{12}$ of

Duodecimals are added and subtracted in the same manner as compound numbers, 12 of a less denomination making 1 of a greater, as in the following

TABLE.

12"" fourths make 1"" third,
12" thirds - - 1" second,
12" seconds - - 1' inch or prime,
12' inches, or primes, 1 foot.

Note. The marks, ', ", ", ", &c. which distinguish the different parts, are called the indices of the parts or denominations.

MULTIPLICATION OF DUODECIMALS.

Duodecimals are chiefly used in measuring surfaces and solids.

1. How many square feet in a board 16 feet 7 inches long, and 1 foot 3 inches wide?

Note. Length × breadth—superficial contents, (¶ 25.) OPERATION.

7 inches, or primes $=\frac{7}{12}$ of a ft. Length, 16 7' foot, and 3 inches 3 of a foot; Breadth, 1 consequently, the product of 7' $\times 3' = \frac{21}{14}$ of a foot, that is, 21''1' $9^{\prime\prime}$ 4 =1' and 9"; wherefore, we set 7' 16 down the 9", and reserve the Ans. 20 8' 1' to be carried forward to its

proper place. To multiply 16 feet by 3' is to take $\frac{3}{12}$ of $\frac{1}{16}$ = $\frac{48}{12}$, that is, 48'; and the 1' which we reserved makes 49', =4 feet 1'; we therefore set down the 1', and carry forward the 4 feet to its proper place. Then, multiplying the multiplicand by the 1 foot in the multiplier, and adding the two products together, we obtain the answer, 20ft, 8'9'.

The only difficulty that can arise in the multiplication of duodecimals is, in finding of what denomination is the pro1 97

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= 72 of a 32 of a foot; oduct of 7' that is, 21" lore, we set eserve the ward to its ke 72 of 46 red makes and carry nultiplying and adding 20ft, 8'9". plication of is the pro-

duct of any two denominations. This may be ascertained as above, and in all cases it will be found to hold true, that the product of any two denominations will always be of the denomination denoted by the sum of their INDICES. Thus, in the above example, the sum of the indices of 7'×3' is"; consequently, the product is 21"; and thus primes multiplied by primes will produce seconds; primes multiplied by seconds produce thirds; fourths multiplied by fifths produce ninths,&c.

It is generally most convenient, in practice, to multiply the multiplicand first by the feet of the multiplier, then by the inches, &c. thus:—

ft.
16 7'
1 3'
16 7'
4 1' 9"

20

¶ 97.

16 ft.×1 ft.=16 ft., and $7'\times1$ ft. =7'. Then, 16 ft.×3'=48'=4 ft., and $7'\times3'=21''=1'$ 9''. The two products added together, give for the answer. 20 ft. 8' 9'', as before.

2. How many solid feet in a block 15 ft. 8' long, 1 ft. 5' wide, and 1ft. 4' thick?

OPERATION.

9"

ft.
Length, 15 8'
Breadth, 1 5'

The length multiplied by the breadth, and that product by the thickness, givs the solid contents, (¶ 33.)

6 6' 4"

22 2' 4"

Thickness 1 4'

22 2' 4" 7 4' 9" 4"' Ans. 29 7' 1" 4"'

From these examples we derive the following RULE:—Write down the denominations as compound numbers, and in multiplying remember, that the product of any two denominations will always be of that denomination denoted by the sum-of their indices.

EXAMPLES FOR PRACTICE.

3. How many square feet in a stock of 15 boards, 12 ft. 8' in length, and 13' wide?

Ans. 205 ft. 10'.

4. What is the product of 371ft 2' 6" multiplied by 181 ft. 1' 9" ?

Ans. 67242 ft. 10' 1" 4" 6"".

Note. Painting, plastering, paving, and some other kinds of work, are done by the square yard. If the contents in square feet be divided by 9, the quotient, it is evident, will be square yards.

5. A man painted the walls of a room 8 ft. 2' in height, and 72 ft. 4' in compass; (that is, the measure of all its

sides;) how many square yards did he paint?

Ans. 65 yds. 5 ft. 8' 8"

6. How many cord feet of wood in a load 8 feet long, 4 feet wide, and 3 feet 6 inches high?

Note. It will be recollected, that 16 solid feet make a cord foot.

Ans. 7 cord feet.

7. In a pile of wood 176 ft. in length, 3 ft. 9' wide, and 4 ft. 3' high, how many cords?

Ans. 21 cords, and 776 cord feet.

8. How many cord feet of wood in a load 7 feet long, 3 feet wide, and 3 feet 4 inches high? and what will it come to at 2s. per cord foot?

Ans. 43 cord feet, and will come to 8s. 9d.

9. How much wood in a load 10 ft. in length, 3 ft. 9' in width, and 4 ft. 8' in height? and what will it cost at \$1'92 per cord?

Ans. 1 cord and 215 cord feet, and it will come to \$2.621.

T 98. Remark. By some surveyors of wood, dimensions are taken in feet and decimals of a foot. For this purpose, make a rule or scale 4 feet long, and divide it into feet and each foot into 10 equal parts. On one end of the rule for 1 foot, let each of these parts be divided into 10 other equal parts. The former division will be 10ths, and the latter 100ths of a foot. Such a rule will be found very convenient for surveyors of wood and of lumber, for painters, joiners, &c.; for the dimensions taken by it being in feet and decimal parts of a foot, the casts will be no other than so many operations in decimal fractions.

10. How many square feet in a hearth stone, which, by a rule, as above described, measures 4.5 feet in length, and 2,6 feet in width? and what will be its cost, at 75 cents per

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, which, by a length, and t 75 cents per square foot ? Ans. 11'7 feet; and it will cost \$8'775.

11. How many cords in a load of wood 7'5 feet in length, 3'6 feet in width, and 4'8 feet in height 1 Ans. 1 cord 1,5 ft.

12. How many cord feet in a load of wood 10 feet long, 3'4 feet wide, and 3'5 feet high?

Ans. 776.

QUESTIONS.

1. What are duodecimals? 2. From what is the word derived?
3. Into how many parts is a foot usually divided, and what are the parts called? 4. What are the other denominations? 5. What is understood by the indices of the denominations? 6. In what are duodecimals chiefly used? 7. How are the contents of a surface bounded by straight lines found? 8. How are the contents of a solid found? 9. How is it known of what denomination is the product of any two denominations? 10. How may a scale or rule be formed for taking dimensions in feet and decimal parts of a foot?

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¶ 99. Involution, or the raising of powers, is the multiplying any given number into itself continually a certain number of times. The products thus produced are called the powers of the given number. The number itself is called the first power or root. If the first power be multiplied by itself, the product is called the second power or square: if the square be multiplied by the first power, the product is called the third power, or cube, &c. thus,

5 is the root, or 1st power of 5.

 $5\times 5=25$ is the 2d power, or square, of 5, $=5^2$ $5\times 5\times 5=125$ is the 3d power, or cube, of 5, $=5^3$ $5\times 5\times 5\times 5=625$ is the 4th power, or biquadrate, of $=5^4$

The number denoting the power is called the *index*, or exponent; thus, 5⁴ denotes that 5 is raised or involved to the 4th power.

1. What is the square, or 2d power of 7? Ans. 49.

2. What is the square of 30 ?

3. What is the square of 4000 ?

Ans. 16000000.

4. What is the cube, or 3d power, of 41 Ans. 64.

5. What is the cube of 800?

Ans. 5120000000.

6. What is the 4th power of 60? Ans. 12960000.

7. What is the square of 1? — of 2? — of 3? — of 4? Ans. 1, 4, 9, and 16.

8. What	t is the	cube of	11	-	of 21	of	31-
of 47							

9. What is the square of \(\frac{2}{3} \) --- of \(\frac{4}{5} \)? --- of \(\frac{4}{5} \)?

10. What is the cube of $\frac{2}{4}$? — of $\frac{1}{4}$? — of $\frac{1}{4}$?

Ans. $\frac{a}{27}$, $\frac{64}{125}$, and $\frac{343}{512}$.

11. What is the square of $\frac{1}{2}$? —— the 5th power of $\frac{1}{2}$?

Ans. $\frac{1}{4}$, and $\frac{1}{32}$.

12. What is the square of 1.5 ! — the cube !

Ans. 2.25, and 3.375.
What is the 6th power of 1.2?

Ans. 2.985984.

13. What is the 6th power of 1'2?
14. Involve 24 to the 4th power.

Note. A mixed number, like the above, may be reduced to an improper fraction before involving: thus, $21-\frac{9}{4}$; or it may be reduced to a decimal; thus, $21-\frac{9}{4}$:

Ans. $\frac{6161}{256} = 25\frac{1}{26}$.

15. What is the value of 74, that is, the 4th power of 7?

Ans. 2401.

16. How much is 93? — 65? — 104?

Ans. 729, 7776, 10000.

17. How much is 27! — 36! — 45! — 53! — 65! — 103! Ans. to the last, 100000000.

The powers of the nine digits, from the first power to the fifth, may be seen in the following

TABLE.

Roots	or	1st	Powers1	2	3	1	41	5	61	7	81	9
Squares	lor	21	Powers	4	9	T	16	251	361	491	64	81
Cubes	or	3 d	Powers 1	81	27	T	641	125	216	3431	5121	129
Biquadrates	or	4th	Powers!	16	81	T	256	625	1296	2401	40961	6561
Sursolida	or	51h	Powers	32	243	Ť	10241	3125	7776	16807	327681	59049

EVOLUTION.

1 100. Evolution, or the extracting of roots, is the method of finding the root of any power or number.

The root, as we have seen, is that number, which, by a continual multiplication into itself, produces the given power. The square root is a number which, being squared, will produce the given number; and the cube, or third root, is a number, which being cubed or involved to the 3d power will produce the given number: thus, the square root of 14

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31 and 64.

99, 100.

, 18, 11. 3? and 243. ver of 1?

, and 32. and 3'375. 2'985984.

be reduced 21-2; or

 $=25\frac{1}{2}\frac{1}{6}\frac{1}{6}$. power of 7 1 Ans. 2401.

776, 10000. — 5³ ? 100000000. power to the

7| 8| 9 19| 64| 81 13| 512| 129 01| 4096| 656| 07|32768| 59049

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third root, is a
the 3d power.
are root of 14

is 12, because $12^2=144$; and the cube root of 343 is 7, because 7^3 , that is, $7\times7\times7=343$; and so of other numbers.

Although there is no number which will not produce a perfect power by involution, yet there are many numbers of which precise roots can never be obtained. But by the help of decimals, we can approximate, or approach, towards the root to any assigned degree of exactness. Numbers, whose precise roots cannot be obtained, are called surd numbers, and those whose roots can be exactly obtained, are called rational numbers.

The square root is indicated by this character \checkmark placed before the number; the other roots by the same character with the index of the root placed over it. Thus, the square root of 16 is expressed \checkmark 16; and the cube root of 27 is

expressed $\sqrt{27}$? and the 5th root of 7776, $\sqrt{7776}$.

When the power is expressed by several numbers, with the sign + or — between them, a line, or vinculum, is drawn from the top of the sign over all the parts of it; thus, the square root of 21—5 is 121—5. &c.

EXTRACTION OF THE SQUARE ROOT.

¶ 101. To extract the square root of any number is to find a number, which, being multiplied into itself, shall produce the given number.

1. Supposing a man has 625 yards of carpeting, a yard wide, what is the length of one side of a square room, the floor of which the carpeting will cover? that is, what is one side of a square, which contains 625 square yards?

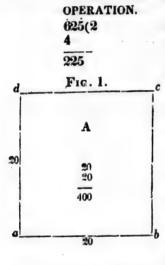
We have seen, (132,) that the contents of a square surface is found by multiplying the length of one side into itself, that is, by raising it to the second power; and hence, having the contents, (625) given, we must extract its square root to find one side of the room.

This we must do by a sort of trial: and,

1st. We will endeavor to ascertain how many figures there will be in the root. This we can easily do, by pointing off the number, from units, into periods of two figures each; for the square of any root always contains just twice

as many, or one figure less than twice as many figures, as are in the root; of which truth the pupil may easily satisfy himself by trial. Pointing off the number, we find, that

the root will consist of two figures, a ten and a unit.



2d. We will now seek for the first figure, that is, for the tens of the root, and it is plain that we must extract it from the left hand period 6, (hundreds.) The greatest square in 6 (hundreds) we find, by trial, to be 4, (hundreds,) the root of which is 2, (tens, = 20;) therefore, we set 2 (tens) in the root. root, it will be recollected, is one side of a square. Let us, then, form a square, (A. Fig. 1.) each side of which shall be supposed 2 tens, = 20 yards, expressed by the root now obtained.

The contents of this square are $20 \times 20 = 400$ yards, now disposed of, and which, consequently, are to be deducted from the whole number of yards, (625,) leaving 225 yards. This deduction is most readily performed by subtracting the square number 4, (hundreds,) or the square of 2, (the figure in the root already found,) from the period 6, (hundreds,) and bringing down the next period by the side of the remainder making 225, as before.

3d. The square A is now to be enlarged by the addition of the 225 remaining yards; and, in order that the figure may retain its square form, it is evident, the addition must be made on two sides. Now, if the 225 yards be divided by the length of the two sides, (20 + 20 = 40), the quotient will be the breadth of this new addition of 225 yards to the sides c d and b c of the square A.

But our root already found, = 2 tens, is the length of one side of the figure A; we therefore take double this root, = 4 tens, for a divisor.

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OPERATION—CONTINUED.
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45)225 225 Frg. II. 20 yds.

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	20 yds.	Profession (Miles	5 yds.	- 1			

The divisor, 4, (tens) is in reality 40, and we are to seek how many times 40 is contained in 225, or, which is the same thing, we may seek how many times 4 (tens) is contained in 22, (tens,) rejecting the right hand figure of the dividend, because wo have rejected the cipher in the divisor. We find our quotient, that is, the breadth of the addition. to be 5 yards; but, if we look at Fig. II., we shall perceive that this addition of 5yds. to the two sides does not complete the square; for there is still wanting, in the corner D, a small square, each side of

which is equal to this last quotient, 5; we must, therefore, add this quotient, 5, to the divisor, 40, that is, place it as the right hand of the 4 (tens,) making it 45; and then the whole divisor, 45, multiplied by the quotient, 5, will give the contents of the whole addition around the sides of the figure A, which, in this case, being 225 yards, the same as our dividend, we have no remainder, and the work is done. Consequently, Fig. II. represents the floor of a square room, 25 yards on a side, which 625 square yards of carpeting will exactly cover.

The proof may be seen by adding together the several parts of the figure, thus:-

The square A contains 400 yards.
The figure B " 100 "

Or we may prove it by involution, thus:—
25 × 25 = 625, as before.

S

From this example and illustration we derive the following general

RULE

For the extraction of the Square Root.

1. Point off the given number into periods of two figures each, by putting a dot over the units, another over the hundreds, and so on. These dots show the number of figures of which the root will consist.

II. Find the greatest square number in the left hand period, and write its root as a quotient in division. Subtract the square number from the left hand period, and to the remainder bring down the next period for a dividend.

III. Double the root already found for a divisor; seek how many times the divisor is contained in the dividend, excepting the right hand figure, and place the result in the root, and also at the right hand of the divisor; multiply the divisor, thus augmented, by the last figure of the root, and subtract the product from the dividend; to the remainder bring down the next period for a new dividend.

IV. Double the root already found for a new divisor, and continue the operation as before, until all the periods are brought down.

Note 1. If we double the right hand figure of the last divisor, we shall have the double of the root.

Note 2. As the value of figures, whether integers or decimals, is determined by their distance from the place of units, so we must always begin at unit's place to point off the given number, and, if it be a mixed number, we must point it off both ways from units, and if there be a deficiency in any period of decimals, it may be supplied by a cipher. It is plain, the root must always consist of so many integers and decimals as there are periods belonging to each in the given number.

EXAMPLES FOR PRACTICE.

9: What is the square root of 10342656 ?

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or; seek dividend, alt in the tiply the root, and remainder

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10342656 (3216, Ans.

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62) 134 124

641) 1026

641

6426) 38556 38556

3. What is the square root of 43264 !

OPERATION.

43264 (208, Ans.

7. 000

408) 3264 3264

4. What is the square root of 998001? Ans. 999.

5. What is the square root of 234'09 ? Ans. 15'3.

6. What is the square root of 964'5192360241!

Ans. 31'05671.

7. What is the square root of '001296?

Ans. '036.

8. What is the square root of '2916?

Ans. '54.

9. What is the square root of 36372961 1 Ans. 6031.

10. What is the square root of 164! Ans. 12'8+.

I 102. In this last example, as there was a remainder, after bringing down all the figures, we continued the operation to decimals, by annexing two ciphers for a new period, and thus we may continue the operation to any assigned degree of exactness; but the pupil will readily perceive, that he can never in this manner, obtain the precise root; for the last figure in each dividend will always be a cipher, and the last figure in each divisor is the same as the last quotient figure; but no one of the nine digits, multiplied into itself,

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produces a number ending with a cipher; therefore, whatever be the quotient figure, there, will still be a remainder.

11. What is the square root of 3? Ans. 1	73-	۴.
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Note. We have seen, (¶ 99, ex. 9.) that fractions are squared by squaring both the numerator and the denominator. Hence it follows, that the square root of a fraction is found by extracting the root of the numerator and of the denominator. The root of 4 is 2, and the root of 9 is 3.

					Ans.	7.	
15	What	in the	 most of	4 1	Ann	2	

16.	What is	the square	root of 18	Ans. 10.

17. What is the square root of
$$\frac{1}{144}$$
?

18. What is the square root of 201 ?

Ans. $\frac{1}{12} = \frac{2}{4}$.

When the numerator and denominator are not exact squares, the fraction may be reduced to a decimal, and the approximate root found, as directed above.

19.	What	is	the	square	root	of	2= '75 1	Ans. 1866+.
				square				Ans. '912+,

SUPPLEMENT TO THE SQUARE ROOT.

QUESTIONS.

EXERCISES.

1. A general has 4006 men; how many must be place

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Ans. 3.

Ans. 5.

Ins. 10.

12 = 1.

Ans. 41.

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in rank and file to form them into a square 1

2 If a square field contains 2025 square rods, how many rods does it measure on each side?

Ans. 45.

3. How many trees in each row of a square orchard con taining 5025 trees?

Ans. 75.

4. There is a circle whose area, or superficial contents, is 5184 feet; what will be the length of the side of a square a equal area?

\$\sqrt{5184}\$=72 feet, Ans.

5. A has two fields, one containing 40 acres, and the other containing 50 acres, for which B offers him a square field containing the same number of acres as both of these; how many rods must each side of this field measure?

Ans. 120 rods.

6. If a certain square field measure, 20 rods on each side, how much will the side of a square field measure, containing 4 times as much?

\$\sqrt{20\times 20\times 40 \text{ rods}^4 \text{ Ass.}}\$

8. It is required to lay out 288 rods of land in the form of a parallelogram, which shall be twice as many rods in length as it is in width.

Note. If the field be divided in the middle, it will form two equal squares. Ans. 24 rods long, and 12 rods wide.

9. I would set out, at equal distances, 784 apple trees, so that my orehard may be 4 times as long as it is broad; how many rows of trees must I have, and how many trees in each row?

Ans, 14 rows, and 56 in each row.

10. There is an oblong piece of land, containing 192 square rods, of which the width is \(^3\) as much as the length; required its dimensions.

Ans. 16 by 12.

11. There is a circle, whose diameter is 4 inches; what

is the diameter of a circle, 9 times as large ?

Note. The areas or contents of circles are in proportion to the squares of their diameters, or of their circumferences. Therefore, to find the diameter required, square the given diameter, multiply the square by the given ratio, and the square root of the product will be the diameter required.

 $\sqrt{4\times4\times9}$ =12 inches, Ans.

12. There are two circular ponds in a gentleman's pleas-

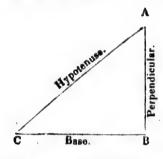
wrs ground; the diameter of the less is 100 feet, and the greater is 3 times as large; what is its diameter?

Ans. 173'2+ ft.

13. If the diameter of a circle be 12 inches, what is the diameter of one 1 as large?

Ans. 6 inches.

values 14. A carpenter has a large wooden square; one part of it is 4 feet long, and the other part 3 feet long; what is the length of a pole that will just reach from one and to the other?



Note. A figure of 3 sides is called a triangle, and if one of the corners be a square corner, or right angle, like the angle at B in the annexed figure, it is called a right-angled triangle, of which the square of the longest side A C, (called the hypotenuse, is equal to the sum

of the squares of the other two sides, A B and B C.

 $4^2=16$, and $3^2=9$; then, $\sqrt{9+16}=5$ feet, Ans.

15. If, from the corner of a square room, 6 feet be measured off one way, and 8 feet the other way, along the sides of the room, what will be the length of a pole reaching from point to point?

Ans. 10 feet.

16. A wall is 32 feet high, and a ditch before it is 24 feet wide; what is the length of a ladder that will reach from the top of the wall to the opposite side of the ditch?

Ans. 40 feet.

17. If the ladder be 40 feet, and the wall 32 feet, what is the width of the ditch?

Ans. 24 feet.

18. The ladder and ditch given, required the wall.

Ans. 32 feet.

19. The distance between the lower ends of two equal rafters is 32 feet, and the height of the ridge, above the beam on which they stand, is 12 feet; required the length of each rafter.

Ans. 20 feet.

20. There is a building 30 feet in length and 22 feet in width, and the caves project beyond the wall I foot on every side; the roof terminates in a point at the centre of the

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. 32 feet. two equal above the he length s. 20 feet. 22 feet in ot on evtre of tha building, and is there supported by a post, the top of which is 10 feet above the beams on which the rafters rest : what is the distance from the foot of the post to the corners of the caves ! and what is the length of a rafter reaching to the middle of one side? — a rafter reaching to the middle of one end? and a rafter reaching to the corners of the eaves?

Answers, in order, 20ft.; 15'62+ft.; 18'86+ft.; and

22'36+ft.

21. There is a field 800 rods long and 600 rods wide: what is the distance between two opposite corners?

Ans. 1000 rods.

22. There is a square field containing 90 acres; how mamy rods in length is each side of the field? and how many rods apart are the opposite corners ?

Answers, 120 rods; and 169'7+rods.

23. There is a square field containing 10 acres; what distance is the centre from each corner ! Ans. 28'28+ rode.

EXTRACTION OF THE CUBE ROOT.

A solid body, having six equal sides, and each of the sides an exact square, is a CUBE, and the measure in length of one of its sides is the root of that cube; for the length, breadth, and thickness of such a body are all alike; consequently, the length of one side, raised to the third power, gives the solid contents. See ¶ 33.

Hence it follows, that extracting the cube root of any number of feet is finding the length of one side of a cubic body, of which the whole contents will be equal to the given

number of feet.

1. What are the solid contents of a cubic block, of which each side measures 2 feet? Ans. $2^3 = 2 \times 2 \times 2 = 8$ feet.

2. How many solid feet in a cubic block, measuring 5 feet on each side? Ans. 53=125 feet.

3. How many feet in length is each side of a cubic block. containing 125 solid feet ! Ans. 125=5 feet.

The root may be found by trial.

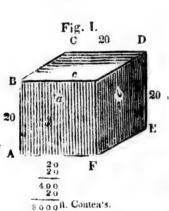
4. What is the side of a cubic block containing 64 solid feet ! - 27 solid feet ! - 216 solid feet ! - 512 solid Ans. 4ft.; 3 ft.; 6 ft.; and 8 ft. feet?

5. Supposing a man has 13824 feet of timber, in separate blocks of I cubic foot each; he wishes to pile them up in a cubic pile; what will be the length of each side of such a pile?

It is evident, the answer is found by extracting the cube root of 13824; but this number is so large, that we cannot so easily find the root by trial as in the former examples; We will endeavor, however, to do it by a sort of trial; and,

1st. We will try to ascertain the number of figures, of which the root will consist. This we may do by pointing the number off into periods of three figures each (¶ 101, ex. 1.)

OPERATION. 13824(2 8 5824



Pointing off, we see, the root will consist of 2 figures. a ten and a unit. Let us, then seek for the first figure, or tens of the root, which must be extracted from the left hand period, 13 (thousands.) The greatest cube in 13, (thousands) we find by trial, or by the table of powers, to be 8, (thousands,) the root of which is 2, (tens;) therefore, we place 2 (tens) in the root. The root, it will be recollected, is one side of a cube. Let us, then, form a cube, (Fig.I.) each side of which shall be supposed 20 feet, expressed by the root now obtained. The contents of this cube are $20 \times 20 \times 20 = 8000$ solid

feet, which are now disposed of, and which, consequently, are to be deducted from the whole number of feet, 13824. 8000 taken from 13824 leave 5824 feet. This deduction is most readily performed by subtracting the cubic number, 8, or the cube of 2, (the figure of the root already found,) from the period 13, (thousands,) and bringing down the next period by the side of the remainder, making 5824, as before.

2d. The cubic pile A D is now to be enlarged by the addition of 5824 solid feet, and, in order to preserve the cubic form of the pile, the addition must be made on one half of its ides, that is, on 3 sides a, b, and c. Now, if the 5824

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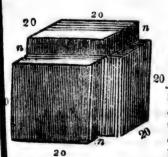
if the 5824

solid feet be divided by the square contents of these 3 equal sides, that is, by 3 times, [20×20=400]=1200, the quotient will be the thickness of the addition made to each of the sides a, b, c. But the root, 2, [tens,] already found, is the length of one of these sides; we therefore square the root, 2, [tens,]=20×20=400, for the square contents of one side, and multiply the product by 3, the number of sides. 400×3=1200, or, which is the same in effect, and more convenient in practice, we may square the 2, (tens.) and multiply the product by 800, thus, $2\times2=4$, and $4\times300=1200$. for the divisor, as before.

13824(24 Root.

Divis. 1200)5824 Dividend.

Fig. II.



The divisor, 1200, is con-OPERATION-CONTINUED. tained in the dividend 4 times; consequently, 4 feet is the thickness of the addition made to each of the three sides, a. b, c, and $4 \times 1200 = 4800$, is the solid feet contained in these additions; but if we look at Fig. II., we shall perceive, that this addition to the 3 sides does not complete the cube; for there are deficiencies in the 3 corners n, n, n. Now the length of each of these deficiencies is the same as the length of each side, that is, 2 [tens] =20, and their width and thickness are each equal to the last quotient figure, [4]; their contents, therefore, or the number of feet required to 20 fill these deficiencies, will be found by multiplying square of the last quotient figure, $[4^2]$ =16, by the length of all the deficiencies, that is, by 3 times the length of each

de, which is expressed by the former quotient figure, 2 ens.] 3 times 2 [tens] are 6 [tens] =60; or what is the me in effect, and more convenient in practice, we may

multiply the quotient figure, 2, [tens,] by 30, thus, 2×30 =60, as before; then, 60×16 =960, contents of the three deficiencies, n, n, n.

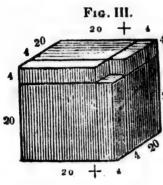
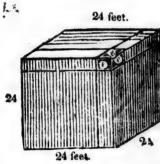


Fig. IV.



Looking at Fig. III., we perceive there is still a deficiency in the corner where the last blocks meet. This deficiency is a cube, each side of which is equal to the last quotient figure, 4. The cube 20 of 4, therefore, [4×4×4=64,] will be the solid contents of this corner, which, in Fig. IV. is seen filled.

Now, the sum of these several additions, viz. 4800+960+64=5824, will make the subtrahend, which, subtracted from the dividend, leaves no remainder, and the work is done.

Fig. IV. shows the pile which 13824 solid blocks of one foot each would make when laid together, and the root 24, shows the length of one side of the pile. The correctness of the work may be ascertained by cubing the side now found, 24°, thus, 2 ×24×24—13824, the gives

number; or it may may be proved by adding together the contents of all the several parts, thus,

Feet. 8000—contents of Fig. I.

4800—addition to the sides a, b, and c, Fig. 1.
960—addition to fill the deficiencies n, n, n, Fig. II.

64=addition to fill the corner e, e, e, Fig. IV.

13824—contents of the whole pile, Fig. IV. 24 feet a

From the foregoing example and illustration we denote the following

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Fig. 1. n, n, Fig. II. Fig. IV.

IV. 24 feet

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RULE

For extracting the Cube Root.

- I. Separate the given number into periods of three figures each by putting a point over the unit figure, and every third figure beyond the place of units.
- II. Find the greatest cube in the left hand period, and put its root in the quotient.
- III. Subtract the cube thus found from the said period, and to the remainder bring down the next period, and call this the dividend.
- IV. Multiply the square of the quotient by 300, calling it the divisor.
- V. Seek how many times the divisor may be had in the dividend, and place the result in the root; then multiply the divisor by this quotient figure, and write the product under the dividend.
- VI. Multiply the square of this quotient figure by the former figure or figures of the root, and this product by 30, and place the product under the last; under all write the cube of this quotient figure, and call their amount the subtrahend.
- VII. Subtract the subtrahend from the dividend, and to the remainder bring down the next period for a new dividend, with which proceed as before; and so on, till the whole is finished.
- Note 1. If it happens that the divisor is not contained in the dividend, a cipher must be put in the root, and the next period brought down for a dividend.
- Note 2. The same rule must be observed for continuing the operation, and pointing off for decimals, as in the square root.
- Note 3. The pupil will perceive that the number which we call the divisor, when multiplied by the last quotient figure, does not produce so large a number as the real subtrahend; hence, the figure in the root must frequently be smaller than the quotient figure.

EXAMPLES FOR PRACTICE.

6. What is the cube root of 1860867 !

OPERATION.

1860867 (128 Ans.

 $1^2 \times 300 = 300 \times 860$ first Dividend.

600

 $2^2 \times 1 \times 30 = 120$ 23 ==

728 first Subtrahend.

 $12^2 \times 300 = 43200 \cdot 132867$ second Dividend.

3240

129600 $3^2 \times 12 \times 30 =$

 $3^{3} =$ 27

132867 second Subtrahend.

000000

7. What is the cube root of 373248?

8. What is the cube root of 21024576 ! Ans. 276.

9. What is the cube root of 84'604519 ! Ans. 4'39.

10. What is the cube root of '000343? Ans. '07

11. What is the cube root of 2? Ans. 1.25+. 12. What is the cube root of 3 1 Ans. 4.

Note. See ¶ 99, ex. 10, and ¶ 102, ex. 14.

13. What is the cube root of 175? Ans. A.

14. What is the cube root of 1343 ? Ans. Jr.

15. What is the cube root of 500? Ans. '125+.

16. What is the cube root of 135? Ans. 1.

SUPPLEMENT TO THE CUBE ROOT.

QUESTIONS.

1. What is a cube? 2. What is understood by the cube root? 3. What is it to extract the cube root? 4. Why is the square of the quotient multiplied by 300 for a divisor? 5. Why, in finding the subtrahend, do we multiply the square of the last quotient figure by 30 times the former figure of the root? 6. Why do we cube the quotient figure? 7. How do we prove the operation?

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EXERCISES.

1. What is the side of a cubical mound, equal to one 288 feet long, 216 feet broad, and 48 feet high?

Ans. 144 ft.

2. There is a cubic box, one side of which is 2 feet; how many solid feet does it contain?

Ans. S feet.

3. How many cubic feet in one 8 times as large? and what would be the length of one side?

Ans. 64 solid feet, and one side is 4 feet.

4. There is a cubical box, one side of which is 5 feet; what would be the side of one containing 27 times as much?

— 64 times as much? — 125 times as much?

Ans. 15, 20, and 25 feet.

5. There is a cubical box, measuring 1 foot on each side; what is the side of a box 8 times as large? — 27 times? — 64 times? — Ans. 2, 3, and 4 feet.

¶ 105. Hence we see, that the sides of cubes are as the cube roots of their solid contents, and, consequently, their contents are as the cubes of their sides. The same proportion is true of the similar sides, or of the diameters of all solid figures of similar forms.

6. If a ball, weighing 4 pounds, be 3 inches in diameter, what will be the diameter of a ball of the same metal, weighing 32 pounds? 4:32::33:63

Ans. 6 inches.

7. If a ball, 6 inches in diameter, weigh 32 pounds, what will be the weight of a ball 3 inches in diameter? Ans. 4lbs.

8. If a globe of silver, 1 inch in diameter, he worth \$6, what is the value of a globe 1 foot in diameter?

Ans. \$10368.

9. There are two globes; one of them is 1 foot in diameter, and the other 40 feet in diameter; how many of the smaller globes would it take to make 1 of the larger?

Ans. 64000.

10. If the diameter of the sun is 112 times as much as the diameter of the earth, how many globes like the earth would it take to make one as large as the sun?

Ans. 1404928.

11. If the planet Saturn is 1000 times as large as the earth, and the earth is 7900 miles in diameter, what is the diameter of Saturn?

Ans. 79000 miles.

12. There are two planets of equal density; the diameter of the less is to that of the larger as 2 to 9; what is the ratio of their solidities?

Ans. $\frac{8}{729}$; or, as 8 to 729.

u. idend.

trahend.

Ans. 72. Ans. 276. Ans. 4'39. Ans. '07 is. 1'25+. Ans. -2.

Ans. \$\frac{5}{6}\$.

Ans. \$\frac{72}{72}\$.

Ans. \$\frac{1}{5}\$.

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Note. The roots of most powers may be found by the square and cube root and the square root; thus, the biquadrate, or 4th root, is the square root of the square root; the 6th root is the cube root of the square root; the 8th root is the square root of the 4th root; the 6th root is the cube root of the cube root, &c. Those roots and the 5th, 7th, 11th, &c., which are not resolvable by a square and cube roots, seldom occur, and, when they do the work is most easily performed by logarithms; for, if the logarithm of any number be divided by the index of the root, the quotient will be the logarithm of the root itself.

ARITHMETICAL PROGRESSION.

¶ 106. Any rank or series of numbers, more than two. increasing or decreasing by a constant difference, is called an Arithmetical Series, or Progression.

When the numbers are formed by a continual addition of the common difference, they form an ascending series; but when they are formed by a continual subtraction of the common difference, they form a descending series.

Thus, \{ 3, 5, 7, 9, 11, 13, 15, &c. is an ascending series. \} 15, 13, 11, 9, 7, 5, 3, &c. is a descending series.

The numbers which form the series are called the terms of the series. The first and last terms are the extremes, and the other terms are called the means.

There are five things in arithmetical progression, any three of which being given, the other two may be found:—

1st. The first term.

2d. The last term.

3d. The number of terms.

4th. The common difference.

5th. The sum of all the terms.

1. A man bought 100 yards of cloth, giving 4 pence for the first yard, 7 pence for the second, 10 pence for the third, and so on, with a common difference of 3 pence; what was the cost of the last yard?

As the common difference, 3, is added to every yard except the last, it is plain the last yard must be 99×3 , = 297 pence, more than the first yard.

Ans. 301 pence.

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rd except 3, == 297 11 pence. Hence, when the first term, the common difference, and the number of terms, are given, to find the last term,—Multiply the number of terms, less 1, by the common difference, and add the first term to the product for the last term.

2. If the first term be 4, the common difference 3, and the number of terms 100, what is the last term? Ans. 301.

3. There are, in a certain triangular field, 41 rows of corn; the first row, in 1 corner, is a single hill, the second contains 3 hills, and so on, with a common difference of 2; what is the number of hills in the last row 1 Ans. 81 hills.

4. A man puts out $1\mathcal{L}$, at 6 per cent simple interest, which, in 1 year, amounts to $1\frac{1}{50}\mathcal{L}$, in 2 years to $1\frac{6}{50}\mathcal{L}$, and so on, in arithmetical progression, with a common difference of $\frac{1}{50}\mathcal{L}$; what would be the amount in 40 years?

Ans. 320£.

Hence we see, that the yearly amounts of any sum, at simple interest, form an arithmetical series, of which the principal is the first term, the last amount is the last term, the yearly interest is the common difference, and the number of years is I less than the number of terms.

5. A man bought 100 yards of cloth in arithmetical progression; for the first yard he gave 4 pence, and for the last 301 pence; what was the common increase of the price on each succeeding yard?

This question is the reverse of example 1; therefore, 301-4=297, and $297 \div 99=3$, common difference.

Hence, when the extremes and number of terms are given, to find the common difference,—Divide the difference of the extremes by the number of terms, less 1, and the quotient will be the common difference.

6. If the extremes be 5 and 605, and the number of terms 151, what is the common difference?

Ans. 4.

7. If a man puts out 1£, at simple interest, for 40 years, and receives, at the end of the time, 3\frac{2}{3}\mathcal{L}, what is the rate?

If the extremes be 1 and 3\frac{2}{3}\mathcal{R}, and the number of terms 41,

If the extremes be 1 and $3\frac{2}{3}9$, and the number of terms 41, what is the common difference?

Ans. $\frac{2}{3}0$.

8. A man had 8 sons, whose ages differed alike; the youngest was 10 years old, and the eldest 45; what was the common difference of their ages?

Ans. 5 years.

9. A man bought 100 yards of cloth in arithmetical se-

ries, he gave 4 pence for the first yard, and 301 pence for the last yard; what was the average price per yard, and what was the amount of the whole?

Since the price of each succeeding yard increases by a constant excess, it is plain, the average price is as much less than the price of the last yard, as it is greater than the price of the first yard; therefore, one half the sum of the first and last price is the average price.

One half of 4d. + 301d. = 152½d. = average price; and the price, 152½d. \times 100 = 15250d. = Ans.

63£ 10s. 10d., whole cost.

Hence, when the extremes and the number of terms are given, to find the sum of all the terms,—Multiply 2 the sum of the extremes by the number of terms, and the product will be the answer.

10. If the extremes be 5 and 605, and the number of terms be 151, what is the sum of the series? Ans. 46055.

11. What is the sum of the first 100 numbers, in their natural order, that is, 1, 2, 3, 4, &c. ?

Ans. 5050.

12. How many times does a common clock strike in 12 hours?

Ans. 78.

13. A man rents a house for $50\mathcal{L}$, annually, to be paid at the close of each year; what will the rent amount to in 20 years allowing 6 per cent, simple interest, for the use of the money?

the money?

The last year's rent will evidently be $50\pounds$ without interest, the last but one will be the amount of $50\pounds$ for 1 year, the last but two the amount of $50\pounds$ for 2 years, and so on, in arithmetical series, to the first, which will be the amount of $50\pounds$ for 19 years = $107\pounds$.

If the first term be 50, the last term 107, and the number of terms 20, what is the sum of the series? Ans. 1570£.

14. What is the amount of an annual pension of $100\pounds$, being in arrears, that is, remaining unpaid, for 40 years, allowing 5 per cent simple interest?

Ans. 7900£.

15. There are, in a certain triangular field, 41 rows of corn; the first row, being in 1 corner, is a single hill, and the last row, on the side opposite, contains 81 hills; how many hills of corn in the field?

Ans. 1681 hills.

16. If a triangular piece of land, 30 rods in length, be 20 rods wide at one end, and come to a point at the other, what

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number of square rods does it contain? Ans. 300.

Ans. whole debt, 440£; common difference, 7.£.

18. What is the sum of the series 1, 3, 5, 7, 9, &c. to 1001!

Note. By the reverse of the rule under ex. 5, the difference of the extremes 1000, divided by the common difference 2, gives a quotient, which, increased by 1, is the number of terms = 501.

19. What is the sum of the arithmetical series 2, 2½, 3, 3½, 4, 4½, &c., to the 50th term inclusive?

Ans. 7124.

Note. $30 \div \frac{1}{3} + 1 = 91$, number of terms. Ans. 1365.
QUESTIONS.

1. What is an arithmetical progression? 2. When is the series called ascending? 3. — when descending? 4. What are the numbers, forming the progression, called? 5. What are the first and last terms called? 6. What are the other terms called? 7. When the first term, common difference, and number of terms, are given, how do you find the last term? 8. How may arithmetical progression be applied to simple interest? 9. When the extremes and number of terms are given, how do you find the common difference? 10 — how do you find the sum of all the terms?

GEOMETRICAL PROGRESSION.

¶ 107. Any series of numbers, continually increasing by a constant multiplier, or decreasing by a constant divisor, is called a Geometrical Progression. Thus, 1, 2, 4, 8, 16, &c. is an increasing geometrical series, and 8, 4, 2, 1, $\frac{1}{2}$, $\frac{1}{4}$, &c. is a decreasing geometrical series.

As in arithmetical, so also in geometrical progression, there are five things, any three of which being given, the other two may be found:—

1st. The first term.

2d. The last term.

3d. The number of terms.

4th. The ratio.

5th. The sum of all the terms.

The ratio is the multiplier, or divisor, by which the series is formed.

1. A man bought a piece of silk, measuring 17 yards, and, by agreement, was to give what the last yard would come to, reckoning 3 pence for the first yard, 6 pence for the second, and so on doubling the price to the last; what did the piece of silk cost him?

×2=196608 pence, = 819£ 4s. answer.

th examining the process by which the last term (196608) has been obtained, we see, that it is a product, of which the catio (2) is sixteen times a factor, that is, one time less than the number of terms. The last term, then, is the sixteenth power of the ratio, (2,) multiplied by the first term (3.)

Now, to raise 2 to the 16th power, we need not produce all the intermediate powers; for $2^4 = 2 \times 2 \times 2 \times 2 = 16$, is a product of which the ratio 2 is 4 times a factor; now, if 16 be multiplied by 16, the product, 256, evidently contains the same factor (2) 4 times + 4 times, = 8 times; and 256 \times 256 = 65536, a product of which the ratio (2) is 8 times + 8 times, = 16 times, factor; it is, therefore, the 16th power of 2, and, multiplied by 3, the first term, gives 196608, the last term, as before. Hence,

When the first term, ratio, and number of terms, are given, to find the last term,—

1. Write down a few leading powers of the ratio with their indices over them.

H. Add together the most convenient indices, to make an index less by one than the number of the term sought.

III. Multiply together the powers belonging to those indices, and their product, multiplied by the first term, will be the term sought.

2. If the first term be 5, and the ratio 3, what is the 8th term?

Powers of the ratio, with their indices over them. $\begin{cases} 1 & 2 & 3 & +4 = 7 \\ 3, & 9, & 27, & \times 81 = 2187 \times 5 \end{cases}$ first term, = 10935, Ans.

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3. A man plants 4 kernels of corn, which, at harvest, produce 32 kernels; these he plants the second year; now, supposing the annual increase to continue 8 fold, what would be the produce of the 16th year, allowing 1000 kernels to a pint?

Ans. 2199023255:552 bushels.

4. Supposing a man had put out one penny at compound interest in 1620, what would have been the amount in 1824,

allowing it to double once in 12 years?

 $2^{17} = 131072$. Ans. 546.2 2s. 8d.

5. A man bought 4 yards of cloth, giving 2 pence for the first yard, 6 pence for the second, and so on, in 3 fold ratio: what did the whole cost him?

2+6+18+54 = 80 pence.

Ans. 80 pence.

In a long series, the process of adding in this manner would be tedious. Let us try, therefore, to devise some shorter method of coming to the same result. If all the terms, excepting the last, viz. 2+6+18, be multiplied by the ratio, 3, the product will be the series 6+18+54 subtracting the former series from the latter, we have, for the remainder, 54-2, that is, the last term, less the first term, which is evidently as many times the first series (2+6+18) as is expressed by the ratio, less 1: hence, if we divide the difference of the extremes (54-2) by the ratio, less 1, (3-1), the quotient will be the sum of all the terms, excepting the last, and, adding the last term, we shall have the whole amount. Thus, 54, -2 = 52, and 3 - 1 = 2; then, $52 \div 2 = 26$, and 54 added, makes 80, Ans. as before.

Hence, when the extremes and ratio are given, to find the sum of the series,—Divide the difference of the extremes by the ratio less 1, and the quotient, increased by the greater term,

will be the answer.

6. If the extremes be 4 and 131072, and the ratio 8, what is the whole amount of the series?

 $\frac{131072 - 4}{8 - 1} + 131072 = 149796 \text{ Answell}$

7. What is the sum of the descending series 3, 1, $\frac{1}{3}$.

It is evident the last term must become 0, or indefining near to nothing; therefore, the extremes are 3 and 0, the ratio 3.

8. What is the value of the infinite series $1 + \frac{1}{4} + \frac{1}{16} + \frac{1}{4}$, &c.?

Ans. $1\frac{1}{3}$.

9. What is the value of the infinite series, $\frac{1}{10} + \frac{1}{100} + \frac{1}{1000} + \frac{1}{10000}$, &c., or, what is the same, the decimal 11111, &c., continually repeated?

Ans. $\frac{1}{4}$.

10. What is the value of the infinite series, $\frac{2}{100} + \frac{2}{10000}$, &c., descending by the ratio 100, or, which is the same, the repeating decimal '020202, &c. ?

Ans. $\frac{2}{300}$.

11. A gentleman, whose daughter was married on a new year's day gave her I pound, promising to triple it on the first day of each month in the year; to how much did her portion amount?

Here, before finding the amount of the series, we must find the last term, as directed in the rule after ex. 1.

Ans. 265720£.

The two processes of finding the last term, and the amount may, however, be conveniently reduced to one, thus:

When the first term, the ratio, and the number of terms, are given, to find the sum or amount of the series,—Raise the ratio to a power whose index is equal to the number of terms, from which subtract 1; divide the remainder by the ratio, less 1, and the quotient, multiplied by the first term, will be the answer.

Applying this rule to this last example, 3^{12} =531441 and $\frac{531441-1}{3-1} \times 1 = 265720 \mathcal{L}$. Ans. as before.

12. A man agrees to serve a farmer 40 years without any other reward then 1 kernel of corn for the first year, 10 for the second year, and so on, in 10 fold ratio, till the end of the time; what will be the amount of his wages, allowing 1000 kernels to a pint, and supposing he sells his corn for 30 pence per bushel?

 $\frac{10^{40}-1}{10-1}\times 1=\left\{\begin{array}{l}1,111,111,111,111,111,111,111,111,\\111,111,111,111,111,111,111,\\111,111,111,111,111,\\111,111,111,111,\\111,111,111,\\111,111,111,\\111,111,111,\\111,111,\\111,111,\\111,111,\\111$

43. A gentleman, dying, left his estate to his 5 sons, to he youngest 1000£ to the second 1500£ and ordered, hat each son should exceed the younger by the ratio of 1₁; hat was the amount of the estate?

Note. Before finding the power of the ratio 11, it may

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be reduced to an improper fraction = 3, or to a decimal, 1.5.

$$\frac{\frac{3}{2}^{5}-1}{\frac{3}{2}-1} \times 1000 = 13187\frac{1}{2}; \text{ or, } \frac{1\cdot 5^{5}-1}{1\cdot 5-1} \times 1000 = 13187\cdot 50\pounds = 13187\pounds 10s. Answer.$$

Compound Interest by Progression.

¶ 108. 1. What is the amount of 4£, for 5 years at 6

per cent compound interest?

We have seen, (¶ 86,) that compound interest is that, which arises from adding the interest to the principal at the close of each year, and, for the next year, casting the interest on that amount and so on. The amount of 1£ for 1 year is 1°06; if the principal, therefore, be multiplied by 1°06, the product will be its amount for 1 year; this amount, multiplied by 1°06, will give the amount (compound interest) for 2 years; and this second amount, multiplied by 1°06, will give the amount for 3 years; and so on. Hence, the several amounts, arising from any sum at compound interest, form a geometrical series, of which the principal is the first term; the amount of 1£ or \$1, &c. at the given rate per cent, is the ratio; the time, in years, is 1 less than the number of terms; and the last amount is the last term.

The last question may be resolved into this: If the first term be 4, the number of terms 6, and the ratio 1.06 what

is the last term?

 $1^{\circ}06^{\circ}=1^{\circ}338$, and $1^{\circ}338\times4=\pounds5^{\circ}352+$.

Ans. 5£ 78. 01d1

Note 1. The powers of the amounts of 1£, at 5 and at 6 per cent, may be taken from the table, under ¶ 85. Thus, opposite 5 years, under 6 per cent, you find 1'338, &c.

Note. 2. The several processes may be conveniently exhibited by the use of letters thus:

Let P represent the Principal.

"R" the Ratio, or the amount of 1£, &c. for 1 yr.

" T " the Time in years.

" A " the Amount.

When two or more letters are joined together, like a word, they are to be multiplied together. Thus PR. implies, that the principal is to be multiplied by the ratio. When one-letter is placed above another, like the index of a power, the

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firts is to be raised to a power, whose index is denoted by the second. Thus RT. implies, that the ratio is to be raised to a power, whose index shall be equal to the time, that is. the number of years.

2. What is the amount of 40£ for 11 years, at 5 per

cent, compound interest?

 $R_T \times P = A$; therefore, $1.05^{11} \times 40 = 68.4$.

Ans. 68£ 8s.

3. What is the amount of 6£ for 4 years, at 10 per cent Ans. 8£ 15s. 8d. compound interest ?

4. If the amount of a certain sum for 5 years, at 6 per cent, compound interest, be 5£ 7s. 01d. what is that sum, or principal ?

If the number of terms be 6, the ratio 1'06, and the last

term 5'352, what is the first term ?

This question is the reverse of the last; therefore.

5'352 R = P; or, 1:338 Ans. 4£.

5. What principal, at 10 per cent. compound interest, will amount, in 4 years, to 8'7846£?

6. What is the present worth of 68£ 8s. due 11 years hence, discounting at the rate of 5 per cent compound interest? Ans. 40£.

7. At what rate per cent, will, 6£ amount to 8.7846£

in 4 years?

If the first term be 6, the last term 8.7846, and the number of terms 5, what is the ratio?

8.7846 p=R_T, that is, ==1'4641=the 4th power of the ratio; and then, by extracting the 4th root, we obtain 1'10 for the ratio. Ans. 10 per cent.

8. In what time will 6£ amount to 8'7846£, at 10 per

cent. compound interest?

8'7846 P=RT, that is, =1'4641=1'10"; therefore, if we divide 1'4641 by 1'10, and then divide the quotient thence. arising by 1.10, and so on, till we obtain a quotient that will not contain 1.10 the number of these divisions will be the number of years. Ans. 4 years.

9. At 5 per cent compound interest, in what time will

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Having found the power of the ratio 1.05, as before, which is 1'71, you may look for this number in the table. under the given rate, 5 per cent, and against it you will find the number of years.

10. At 6 per cent compound interest, in what time will 4£ amount to 5£ 7s. 04d. Ans. 5 years.

Annuities at Compound Interest.

It may not be amiss, in this place, briefly to show the application of compound interest, in computing the amount and present worth of annuities.

An Annuity is a sum payable at regular periods, of one year each, either for a certain number of years, or during the life of the pensioner, or forever.

When annuities, rents, &c. are not paid at the time they

become due, they are said to be in arrears.

The sum of all the annuities, rents, &c. remaining unpaid, together with the interest on each, for the time they have remained due, is called the amount.

1. What is the amount of an annual pension of 100£. which has remained unpaid 4 years, allowing 6 per cent

compound interest ?

The last year's pension will be 100£, without interest; the last but one will be the amount of 100£ for I year; the last but two the amount (compound interest) of 100£ for 2 years, and so on; and the sum of these several amounts will be the answer. We have then, a series of amounts, that is, a geometrical series, (¶ 108,) to find the sum of all the terms.

If the first term be 100, the number of terms 4, and the ratio 1'06, what is the sum of all the terms?

Consult the rule, under ¶ 107, ex. 11.

Hence, when the annuity, the time, and rate per cent, are given, to find the amount,-RAISE the ratio (the amount of 1£, &c. for 1 year) to a power denoted by the number of years; from this power subtract 1, then divide the remainder by the ratio less 1, and the quotient, multiplied by the annuity, will be the amount.

The powers of the amounts, at 5 and 6 per cent

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up to the 24th, may be taken from the table, under 7 85.

2. What is the amount of an annuity of 50£, it being in arrears 20 years, allowing 5 per cent compound interest?

Ans. 1653£ 5s. 92d.

3. If the annual rent of a house, which is 150£, be in arrears 4 years, what is the amount, allowing 10 per cent compound interest?

Ans. 696£ 3s.

4. To how much would a salary of 500£ per annum amount in 14 years, the money being improved at 6 per cent compound interest? —— in 10 years? —— in 20 years? —— in 22 years?

Ans. to the last, 25407£ 15s.

110. If the annuity is paid in advance, or if it be bought at the beginning of the first year, the sum which ought to be given for it is called the present worth.

5. What is the present worth of an annual pension of $100\mathcal{L}$, to continue for 4 years, allowing 6 per cent compound

interest !

The present worth is, evidently, a sum, which, at 6 per cent, compound interest, would, in 4 years, produce an amount, equal to the amount of the annuity in arrears the same time.

By the last rule we find the amount= $437^{\circ}45\mathcal{L}$, and by the directions under \$108, ex. 4, we find the present worth= $346^{\circ}51\mathcal{L}$.

Ans. $346\mathcal{L}$ 10s. $4\frac{2}{4}$ d.

Hence, to find the present worth of any annuity,—First find its amount in arrears for the whole time; this amount, divided by that power of the ratio denoted by the number of years, will give the present worth.

6. What is the present worth of an annual salary of 100£

to continue 20 years, allowing 5 per cent?

Ans. 1246£ 4s. 43d.

The operations under this rule being somewhat tedious, we subjoin a

TABLE,

Showing the present worth of 1£ or \$1 annuity, at 5 and 6 per cent compound interest, for any number of years, from 1 to 34.

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Years.	5 per cent.	6 per cent.	Years.	5 per cent.	6 per cent.
1	0.95238	0.94339	18	11 68958	10.8276
2	1'85941	1.83339	19	1208532	11:15811
3	2'72325	267301	20	12:46221	11'46902
4	3 5 4 5 9 5	34651	21	12.82115	11.76407
5	4'32948	4'21236	22	13463	12:04158
6	5'07569	4.91732	23	13'48807	12:30338
7	5'78637	5.58238	24	13'79864	12.55035
8	6'46321	6'20979	25	14.09394	12,78335
9	7'10782	6.80169	26	14.37518	13'00316
10	7'72173	7:36008	27	14 64303	13.21053
11	8'30641	7.88687	28	14.89813	13'40616
12	8.86325	8'38384	29	15.14107	13.59072
13	9.39357	8.85268	30	15.37245	13'76483
14	9'89864	9:29498	31	15.59281	13 92908
15	10.37966	9.71225	32	15'80268	14'08398
16	10.83777	10.10589	33	16.00255	14.22917
17	11.27407	10.47726	34	16:1929	14.36613

It is evident that the present worth of $2\mathcal{L}$ annuity is 2 times as much as that of $1\mathcal{L}$; the present worth of $3\mathcal{L}$ will be 3 times as much, &c. Hence, to find the present worth of any annuity, at 5 or 6 per cent,—Find, in this table, the present worth of $1\mathcal{L}$ annuity, and multiply it by the given annuity, and the product will be the present worth.

7. What ready money will purchase an annuity of 150£ to continue 30 years, at 5 per cent, compound interest?

The present worth of 1£ annuity, by the table, for 30 years, is $15^{\circ}37245$; therefore, $15^{\circ}37245 \times 150 = 2305 \cdot 867£ = 2305£ 17s. 4d. Answer.$

When annuities do not commence till a certain period of time has elapsed, or till some particular event has taken place, they are said to be in REVERSION.

9. What is the present worth of 100£ annuity, to be continued 4 years, but not to commence till 2 years hence, allowing 6 per cent compound interest?

The present worth is evidently a sum which, at 6 per cent compound interest, would in 2 years produce an amount

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equal to the present worth of the annuity, were it to commence immediately. By the last rule, we find the present worth of the annuity, to commence immediately, to be 346.51£, and, by directions under ¶ 108, ex. 4, we find the present worth of 346.51£ for 2 years to be 308.393£.

Ans. 308£ 7s. 104d.

Hence, to find the present worth of any annuity taken in reversion, at compound interest,—First, find the present worth, to commence immediately, and this sum, divided by the power of the ratio, denoted by the time in reversion, will give the answer.

10. What ready money will purchase the reversion of a lease of $60\mathcal{L}$ per annum, to continue 6 years, but not to commence till the end of 3 years, allowing 6 per cent compound interest to the purchaser?

The present worth to commence immediately, we find to be, 295'039, and $\frac{295'039}{1'06^3}$ =247'72. Ans. 247£ 14s. 44d.

It is plain, the same result will be obtained by finding the present worth of the annuity, to commence immediately, and to continue to the end of the time, that is 3+6=9 years, and then subtracting from this sum the present worth of the annuity, continuing for the time of the reversion, 3 years. Or, we may find the present worth of $1\pounds$ for the two times by the table, and multiply their difference by the given annuity. Thus, by the table,

The whole time, 9 years,=6'80169 The time in reversion, 3 years,=2'67301

Difference,=4'12868

247'72080£

247'72080£=247£ 14s. 43d. Ans.

11. What is the present worth of a lease of 100£ to continue 20 years, but not to commence till the end of 4 years, allowing 5 per cent 1 — what, if it be 6 years in reversion? — 8 years? — 10 years? — 14 years?

T 111. 12. What is the worth of a freehold estate, of which, the yearly rent is 60£, allowing to the purchaser 6 per cent?

In this case, the annuity continues forever, and the estate

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is evidently worth a sum, of which the yearly interest is equal to the yearly rent of the estate. The principal mulplied by the rate gives the interest; therefore, the interest divided by the rate will give the principal; $60 \div 06 = 1000$.

Hence, to find the present worth of an annuity, continuing forever,—Divide the annuity by the rate per cent, and the quotient will be the present worth.

Note. The worth will be the same, whether we reckon simple or compound interest; for since a year's interest of the price is the annuity, the profits arising from that price can neither be more nor less than the profits arising from the annuity, whether they be employed at simple or compound interest.

13. What is the worth of 100£ annuity, to continue forever, allowing to the purchaser 4 per cent? —allowing 5 per cent? —8 per cent? —10 per cent? —15 per cent? —20 per cent? ——20 £.

14. Suppose a freehold estate of $60\pounds$ per annum, to commence 2 years hence, be put on sale; what is its value, al-

lowing the purchaser 6 per cent ?

Its present worth is a sum which, at 6 per cent, compound interest, would, in 2 years, produce an amount equal to the worth of the estate if entered on immediately.

 $\frac{60}{06} = 1000 \pounds$ = the worth, if entered on immediately,

and $\frac{1000£}{1'06^2}$ =889'996£=889£ 19s.11d. the present worth.

The same result may be obtained by subtracting from the worth of the estate, to commence immediately, the present worth of the annuity 60, for 2 years, the time of reversion. Thus, by the table, the present worth of 1£ for 2 years is 1.83339×60=110.0034=present worth of 60£ for 2 years, and 1000£-110.0034=889.9966£=889£ 19s. 11d. Ans. as before.

15. What is the present worth of a perpetual annuity of 100£, to commence 6 years hence, allowing the purchaser 5 per cent compound interest? — what, if 8 years in reversion? — 10 years? — 4 years? — 30 years?

Ans. to the last, 462£ 15s, 14d. The foregoing examples, in compound interest, have been

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confied to yearly payments; if the payments are half yearly, we take half the principal or annuity, half the rate per cent, and twice the number of years, and work as before, and so for any other part of a year.

QUESTIONS.

1. What is a geometrical progression or series? 2. What is the ratio? 3. When the first term, the ratio and the number of terms, are given, how do you find the last term? 4. When the extremes and ratio are given, how do you find the sum of all the terms? 5. When the first term, the ratio, and the number of terms, are given, how do you find the amount of the series? 6. When the ratio is a fraction, how do you proceed? 7. What is compound interest? 8. How does it appear that the amounts, arising by compound interest, form a geometrical series? 9. What is the ratio in compound inter-- the number of terms? - the first term? the last term? 10. When the rate, the time, and the principal, are given, how do you find the amount? - 11. When A. R. and T. are given, how do you find P.? 12. When A. P. and T. are given, how do you find R.? 13. When A. P. and R. are given, how do you find T. 2 14. What is an annuity? 15. When are annuities said to be in arresrs? 16. What is the amount? 17. In a geometrical series, to what is the amount of an annuity, equivalent? 18. How do you find the amount of an annuity, at compound interest? 19. What is the present worth of an annuity? — how computed at compound interest? how found by the table? 20. What is understood by the term reversion? 21. How do you find the present worth of an annuity, taken in reversion? — by the table? 22. How do you find the present worth of a freehold estate, or a perpetual annuity? taken in reversion? — by the table?

PERMUTATION.

¶ 112. Permutation is the method of finding how many different ways the order of any number of things may be varied or changed.

1. Four gentlemen agreed to dine together so long as they could sit, every day, in a different order, or position; how many days did they dine together?

Had there been but two of them, a and b, they could sit only in 2 times 1 ($1 \times 2 = 2$) different positions, thus, a b, and b a. Had there been three, a b and c, they could sit in $1 \times 2 \times 3 = 6$ different positions; for, beginning the order with a, there will be 2 positions, viz. a b c, and a c b; next beginning with b, there will be 2 positions, b a c, and b c a; last-

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2. What is the number of terms. en the extremes all the terms? 5. terms, are given, hen the ratio is a und interest? 8. ompound interest. compound inter-? the last term? given, how do you w do you find R.? T. 2 14. What is in arrears? 16. , to what is the ai find the amount the present worth interest? y the term reveran annuity, taken

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ly, beginning with c, we have c a b, and c b a, that is, in all, $1\times2\times3=6$ different positions. In the same manner if there be four, the different positions will be $1\times2\times3\times4=24$.

Ans. 24.

Hence, to find the number of different changes or permutations, of which any number of different things are capable,—Multiply continually together, all the terms of the natual series of numbers, from I up to the given number, and the last product will be the answer.

2. How many variations may there be in the position of the nine digits?

Ans. 362880.

3. A man bought 25 cows, agreeing to pay for them 1 penny for every different order in which they could all be placed; how much did the cows cost him?

Ant. 64630041847212441600000£

4. A certain Church has 8 bells; how many changes may be rung upon them.

Ans. 40320.

MISCELLANEOUS EXAMPLES.

¶ 118. 1. $4+6 \times 7-1=60$

A line, or vinculum, drawn over several numbers, signifies, that the numbers under it, are to be taken jointly, or as one whole number.

2. $9-8+4 \times 8+4-6$ —how many? Ans. 30.

3. $7+4-\overline{2+3}+40\times 5$ —how many? Ans. 230.

4. $\frac{3+6-2\times 4-2}{2\times 2}$ how many? Ans. $3\frac{1}{2}$.

5. There are 2 numbers; the greater is 25 times 78, and their difference is 9 times 15; their sum and product are required. Ans. 3765 is their sum, 3539250 their product.

6. What is the difference between thrice five and thirty, and thrice thirty-five $! 35+3-5\times 3+30=60$, Ans.

7. What is the difference between six dozen dozen, and half a dozen dozen?

Ans. 792.

8. What number divided by 7 will make 6488?

9. What number multiplied by 6 will make 2058 !

10. A gentlemen went to sea at 17 years of age; 8 years after he had a son born, who died at the age of 35; after whom the father lived twice 20 years; how old was the father at his death?

Ans. 100 years.

11. What number is that, which being multiplied by 15 the product will be $\frac{3}{4}$? $\frac{3}{10}$ $\frac{15}{10}$ $\frac{15}{10}$ Ans.

12. What decimal is that, which being multiplied by 15, the product will be '75 ? '75 ÷ 15 = '05 Ans.

13. What is the decimal equivalent to 1/3 ?

Ans. '0285714.

14. What fraction is that, to which if you add \(\frac{2}{5} \), the sum will be \(\frac{2}{5} \).

Ans. \(\frac{1}{3} \frac{3}{5} \).

15. What number is that, from which if you take $\frac{3}{5}$, the remainder will be $\frac{1}{4}$?

Ans. $\frac{3}{4}$ 8.

16. What number is that, which being divided by $\frac{3}{4}$, the quotient will be 21?

Ans. 153.

17. What number is that, from which if you take $\frac{2}{5}$ of itself, the remainder will be 12?

Ans. 20.

19. What number is that, to which if you add $\frac{2}{5}$ of $\frac{4}{3}$ of itself, the whole will be 20?

Ans. 12.

20. What number is that, of which 9 is the 3 part?

Ans. 131.

21. A farmer carried a load of produce to market; he sold 780 lbs. of pork, at 3d. per pound; 250 lbs. of cheese, at 5d. per lb.; 154 lbs. of butter, at 10d. per lb.: in pay he received 60 lbs, of sugar, at 7d. per lb.; 15 gallons of molasses, at 2s. 3d. per gallon; ½ barrel of mackerel, at 18s. 9d.; 4 bushels of salt, at 6s. 4d. per bushel; and the balance in money; how much money did he receive?

Ans. 15£ 14s. 8d.

22. A farmer carried his grain to market, and sold 75 bushels of wheat at 7s. 3d. per bushel; 64 bushels of rye, at 4s. 9d. per bushel; 142 bushels of corn, at 2s. 6d. per bushel: in exchange he received sundry articles:—3 pieces cloth, each containing 31 yards, at 8s. 9d. per yard; 2 quintals of fish, 11s. 6d. per quintal; 8 hhds. of salt, $1\pounds$ 1s. 6d. per hhd. and the balance in money: how much money did he receive?

Ans. $9\pounds$ 14s.

23. A man exchanges 760 gallons of molasses, at 2s. per gallon, for 66½ cwt. of cheese, at 1£ per cwt.; how much will be the balance in his favor?

Ans. 9£ 10s.

24. Bought 84 yards of cloth, at 6s. 3d. per yard; how

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much did it come to? How many bushels of wheat, at 7s. Gd. per bushel, will it take to pay for it?

Ans. to the last, 70 bushels. 25. A man sold 342 pounds of beef, at 4d. per pound, ad received his pay in molasses, at 2s. per gallon; how

and received his pay in molasses, at 2s. per gallon; how many gallons did he receive?

Ans. 57 gallons.

26. A man exchanged 70 bushels of rye, at 4s. 6d. per bushel, for 40 bushels of wheat, at 7s. per bushel, and received the balance in oats, at 2s. per bushel; how many bushels of oats did he receive?

Ans. 171.

27. How many bushels of potatoes, at 1s. 6d. per bushel, must be given for 32 bushels of barley, at 2s. 6d. per bushel?

Ans. 534 bushels

28. How much salt, at \$1.50 per bushel, must be given in exchange for 15 bushels oats, at 2s. 3d. per bushel?

Note. It will be recollected that, when the price and cost are given, to find the quantity, they must both be reduced to the same denomination before dividing. Ans 44b ushels.

29. How much wine, at 82.75 per gallon, must be given in exchange for 40 yards of cloth, at 7s. 6d. per yard.

Ans. 21 9 gallons.

30. A had 41 cwt. of hops, at 30s. per cwt. for which B gave him 20£ in money, and the rest in prunes, at 5d. per pound; how many prunes did A receive?

Ans. 17 cwt. 3grs. 4 lb.

31. A has linen cloth worth 2s. 6d. per yard; but, in bartering he will have 2s. 9d. per yard; B has broadcloth worth 18s. 9d. per yard, ready money; at what price ought the broadcloth to be rated in bartering with Λ ?

30d. : 35d. :: .225d. : $.262\frac{1}{2}d$. Ans. Or, $.\frac{13}{3}$ of .225d. =1.£ 18. $.10\frac{1}{2}d$. Ans. The two operations will be seen to be ex-

actly alike.

32. If cloth, worth 2s. per yard, cash, be rated in barter at 2s. 6d., how should wheat, worth 8s. cash, be rated in exchange for the cloth?

Ans. 10s.

33. If 4 bushels of corn cost \$2, what is it per bushel?

34. If 9 bushels of wheat cost 3£ 7s. 6d. what is that per bushel?

Ans. 7s. 6d.

35. If 40 sheep cost 25£, what is that per head?

36. If 3 bushels of cats cost 7s. 6d. how much are they per bushel?

Ans. 2s. 6d.

37. If 22 yards of broadcloth cost 21£ 9s. what is the price per yard?

Ans. 19s. 6d.

38. At 2s. 6d. per bushel, how much corn can be bought for 10s.?

Ans. 4 bushels.

39. A man having 25£, would lay it out in sheep, at 12s. 6d. apiece, how many can he buy?

Ans. 40.

40. If 20 cows cost 75£, what is the price of 1 cow?
— of 2 cows? — of 5 cows? — of 15 cows?

Ans. to the last, 56£ 5s.

41. If 7 men consume 24 lbs. of meat in one week, how much would 1 man consume in the same time?——2 men?

5 men? ——10 men?

— 5 men? — 10 men? Ans. to the last, 34? lb. Note. Let the pupil also perform these questions by the rule of proportion.

42. It I pay 1£ 10s, for the use of 25£, how much must I pay for the use of 18£ 15s,?

Ans. 1£. 2s. 6d.

43. What premium must 1 pay for the insurance of my house against loss by fire, at the rate of \(\frac{1}{2}\) per cent, that is, \(\frac{1}{2}\) pound for 100 pounds, if my house be valued at 2475\(\frac{1}{2}\)?

Ans. 12\(\frac{1}{2}\) 7s. 6d.

44. What will be the insurance, per annum, of a store and contents, valued at $9876 \pm 8s$. at $1\frac{1}{2}$ per centum?

Ans. 148£ 2s. 11d.

45. What commission must I receive for selling 478£ worth of books, at 8 per cent? Ans. 38£ 4s. 94d.

46. A merchant bought a quantity of goods for 734£, and sold them so as to gain 21 per cent; how much did he gain? and for how much did he sell his goods?

Ans, to the last, 888£ 2s. 97d.

47. A merchant bought a quantity of goods at Montreal, for $500\pounds$, and paid $43\pounds$ for their transportation; he sold them so as to gain 24 per cent, on the whole cost; for how much did he sell them?

Ans. $673\pounds$ 6s. 43d.

48. Bought a quantity of books for $64\mathcal{L}$, but for cash a discount of 12 per cent. was made; what did the books cost?

Ans. $56\mathcal{L}$ 6s. 42d.

49. Bought a book, the price of which was marked 1£ 2s. 6d. but for eash the bookseller will sell it at 33½ per cent discount; what is the cash price?

Ans. 15s.

50. I bought a cask of liquor, containing 120 gallons, for $42\pounds$; for how much must I sell it to gain 15 per cent? how much per gallon?

Ans. to the last, 4s. 1d.

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88£ 2s. 9₹d. at Montreal, on; he sold ost; for how 73£ 6s. 43d. it for cash a d the books 56£ 6s. 43d. marked 1£ t at 331 per

Ans. 15s. gallons, for 5 per cent? last, 4s. 1d.

51. Bought a cask of sugar, containing 740 pounds, for 59£ 4s.; how must I sell it per pound, to gain 25 per cent?

52. What is the interest, at 6 per cent, of 712 0s. 43d. for 17 months 12 days ?

53. What is the interest of 487£0s. 2d. for 18 months ?

54. What is the interest of \$8'50 for 7 months? Åns. 43£ 16s. 74d.

55. What is the interest of 1000£ for 5 days? Ans. 8 2974

56. What is the interest of 10s. for 10 years? Ans. 16s. 8d.

57. What is the interest of \$84.25 for 15 months and 7 days, at 7 per cent?

58. What is the interest of \$154.01 for 2 yrs. 4 months and 3 days, at 5 per cent?

59. What sum put to interest at 6 per cent, will, in 2 years and 6 months, amount to \$150? Note. See ¶ 79.

60. I owe a man 475£ 10s. to be paid in 16 months without interest; what is the present worth of that debt, the use of money being worth 6 per cent?

61. What is the present worth of 1000£ payable in 4 years and 2 months, discounting at the rate of 6 per cent? 62. Bought articles to the amount of $500 \mathcal{L}$, and sold

them for 5752, how much was gained?

What per cent was gained? that is, how many pounds were gained on each 100£ laid out? If 500£ gain 75£, what does 100£ gain?

63. Bought cloth at 3£ 10s. per piece, and sold it at 4£ 5s. per piece; how much was gained per centum?

64. A man bought a cask of liquor, containing 126 gallons, for 283£ 10s., and sold it out at the rate of 2£ 15s. per gallon; how much was his whole gain? how much per gallon ! how much per cent !

Ans. His whole gain 63£; per gal. 10s. which is 226 per centum.

65. If 100£ gain 6£ in 12 months, in what time will it gain $4\pounds$? — $10\pounds$? — $14\pounds$?

Ans. to the last, 28 months.

66. In what time will 54£ 10s. at 6 per cent, gain, 2£ Ans. 8 months.

67. 20 men built a certain bridge in 60 days, but, it being carried away in a freshet, it is required how many men can rebuild it in 50 days.

days, days, men.

50 : 60 :: 20 : 24 men, ans.

68. If a field will feed 7 horses 8 weeks, how long will it feed 28 horses? Ans. 2 weeks.

69. If a field, 20 rods in length, must be 8 rods in width to contain an acre, how much in width must be a field, 16 rods in length, to contain the same? Ans. 10 rods.

70. If I purchase for a cloak 12 yards of plaid 5 of a yd. wide, how much bocking 14 yards wide must I buy to line Ans. 5 yards.

71. If a man earn 18£ 15s. in 5 months, how long must he work to earn 115£? Ans. 30% months.

72. B owes C 540£, but B, not being worth so much money, C agrees to take 15 s. on a pound; what sum must C receive for the debt?

73. A cistern, whose capacity is 400 gallons, is supplied by a pipe which lets in 7 gallons in 5 minutes; but there is a leak in the bottom of the cistern which lets out 2 gallons in 6 minutes, supposing the cistern empty, in what time would it be filled?

In 1 minute 7 of a gallon is admitted, but in the same time Ans. 6 hours, 15 minutes. 3 of a gallon leaks out.

74. A ship has a leak which will fill it so as to make it sink in 10 hours; it has also a pump which will clear it in 15 hours; now, if they begin to pump when it begins to leak, in what time will it sink?

In one hour the ship would be 10 filled by the leak, but In the same time it would be $\frac{1}{15}$ emptied by the pump.

Ans. 30 hours.

75. A cistern is supplied by a pipe which will fill it in 40 minutes; how many pipes, of the same bigness, will fill it in 5 minutes?

76. Suppose I lend a friend 500£ for 4 months, he promising to do me a like favour; some time afterward, I have need of 300£; how long may I keep it to balance the for-Ans. 63 months. mer favour ?

77. Suppose 800 soldiers were in a garrison with pro-

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visions sufficient for 2 months; how many soldiers must depart, that the provisions may serve them 5 months?

Ans. 480.

78. If my horse and saddle are worth 21£, and my horse be worth 6 times as much as my saddle, pray what is the value of my horse?

Ans. 18£.

79. Bought 45 barrels of beef, at 17s. 6d. per barrel, among which are 16 barrels, whereof 4 are worth no more

than 3 of the others; how much must I pay?

Ans. 35£ 17s. 6d.

80. Bought 126 gallons of rum for 27£ 10s. how much water must be added to reduce the first cost to 3s. 9d. per gallon?

Note. If 3s. 9d. buy I gallon, how many gallons will 27£ 10s. buy?

Ans. 204 gallons.

81. A thief, having 24 miles start of the officer, holds his way at the rate of 6 miles an hour; the officer pressing on after him at the rate of 8 miles an hour, how much does he gain in 1 hour? how long before he will overtake the thief?

82. A hare starts 12 rods before a hound, but is not perceived by him till she has been up 1\(\frac{1}{4}\) minutes; she scuds away at the rate of 36 rods a minute, and the dog, on view makes after, at the rate of 40 rods a minute; how long will the course hold? and what distance will the dog run?

Ans. 141 minutes, and he will run 570 rods.

83. The hour and minute hands of a watch are exactly together at 12 o'clock; when are they next together?

In 1 hour the minute hand passes over 12 spaces, and the hour hand over 1 space; that is, the minute hand gains upon the hour hand 11 spaces in 1 hour; and it must gain 12 spaces to coincide with it.

Ans. 1h. 5m. 27 3s.

84. There is an island 20 miles in circumference, and three men start together to travel the same way about it; A goes 2 miles per hour, B 4 miles per hour, and C 6 miles per hour; in what time will they come together again?

Ans. 10 hours.

35. There is an island 20 miles in circumference, and two men start together to travel around it; A travels 2 miles per hour, and B 6 miles per hour; how long before they will again come together?

B gains 4 miles per hour, and must gain 20 miles to over-

take A; A and B will therefore be together once in every 5 hours.

86. In a river, supposing two boats start at the same time from places 300 miles apart; the one proceeding up stream is retarded by the current 2 miles per hour, while that moving down stream is accelerated the same; if both be propelled by a steam engine, which would move them 8 miles per hour in still water, how far from each starting place will the boats meet?

Ans. $112\frac{1}{2}$ miles from the lower place, and $187\frac{1}{2}$ miles

from the upper place.

87. A man bought a pipe (126 gallons) of wine for $275\pounds$; he wishes to fill 10 bottles, 4 of which contain 2 quarts, and 6 of them 3 pints each, and to sell the remainder so as to make 30 per cent on the first cost; at what rate per gallon must he sell it?

Ans. $5.936\pounds$ +.

88. Thomas sold 150 pine apples at 1s. 3d. apiece, and received as much money as Harry received for a certain number of watermelons at 9d. apiece; how much money did each receive, and how many melons had Harry?

Ans. 9£ 7s. 6d. and 250 melons.

89. The third part of an army was killed, the fourth part taken prisoners, and 1000 fled; how many were in this army?

This and the eighteenth following questions are usually wrought by a rule called *Position*, but they are more easily solved on general principles. Thus, $\frac{1}{3} + \frac{1}{4} = \frac{7}{12}$ of the army; therefore, 1000 is $\frac{5}{12}$ of the whole number of men; and if $\frac{5}{12}$ be 1000, how much is 12 twelfths, or the whole?

Ans. 24000 men.

90. A farmer, being asked how many sheep he had, answered, that he had them in 5 fields; in the first were $\frac{1}{2}$ of his flock, in the second $\frac{1}{6}$, in the third $\frac{1}{8}$, in the fourth $\frac{1}{12}$, and in the fifth 450; how many had he?

Ans. 1200.

91. There is a pole, $\frac{1}{4}$ of which stands in the mud, $\frac{1}{3}$ in the water, and the rest of it out of the water; required the part out of the water.

Ans. $\frac{1}{3}$

92. If a pole be \(\frac{1}{2} \) in the mud, \(\frac{2}{3} \) in the water, and 6 feet out of the water, what is the length of the pole? Ans. 90 feet

93. The amount of a certain school is as follows: $\frac{1}{16}$ of the pupils study grammar, $\frac{2}{3}$ geography, $\frac{2}{10}$ arithmetic, $\frac{2}{20}$ learn to write, and 9 learn to read: what is the number of each?

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arithmetic, 33 he number o Ans. 5 in grammer, 30 in geography, 24 in arithmetic; 12 learn to write, and 9 learn to read.

94. A man, driving his geese to market, was met by another, who said, "Good morrow, sir, with your hundred geese;" says he, "I have not a hundred; but if I had, in addition to my present number, one half as many as I now have, and 2½ geese more, I should have a hundred:" how many had he?

100 - 21 is what part of his present number?

Ans. He had 65 geese.

95. In an orchard of fruit trees, ½ of them bear apples, ½ pears, ½ plums, 60 of them peaches, and 40, cherries; how many trees does the orchard contain?

Ans. 1200

96. In a certain village, $\frac{1}{2}$ of the houses are painted white, $\frac{1}{4}$ red and, $\frac{1}{6}$ yellow, 3 are painted green, and 7 are unpainted; how many houses in the village? Ans. 120.

97. Seven eights of a certain number exceed four fifths of

the same number by 6; repuired the number.

 $\frac{7}{8} - \frac{4}{5} = \frac{3}{40}$; consequently, 6 is $\frac{3}{40}$ of the required number.

Ans. 80.

98. What number is that to which if $\frac{1}{b}$ of itself be added, the sum will be 30?

Ans. 25.

99. What number is that, to which if its $\frac{1}{2}$ and $\frac{1}{4}$ be added, the sum will be 84?

 $84 = 1 + \frac{1}{2} + \frac{1}{4} = \frac{7}{4}$ times the repuired number. Ans. 48. 100. What number is that, which, being increased by $\frac{2}{3}$ and $\frac{3}{5}$ of itself, and by 22 more, will be made 3 times as much?

The number, being taken 1, $\frac{2}{3}$, and $\frac{2}{5}$ times, will make $2\frac{4}{15}$ times and 22 is evidently what that wants of 3 times.

Ans. 30.

101. What number is that, which being increased by $\frac{2}{5}$, and $\frac{5}{8}$ of itself, the sum will be 2343?

Ans. 90.

102. B, C, and D, talking of their ages, C said his age was once and a half the age of B, and D said his age was twice and one tenth the age of both, and that the sum of ther ages was 93; what was the age of each?

Ans. B 12 years, C 18 years, D 63 years old.

103. A schoolmaster being asked how many scholars he had, said, "If I had as many more as I now have, \(\frac{3}{4}\) as many, \(\frac{1}{2}\) as many, \(\frac{1}{4}\) and \(\frac{1}{8}\) as many, I should then have 435;" what was the number of his pupils?

Ans. 120.

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104. B and C commenced trade with equal sums of moncy; B gained a sum equal to ½ of his whole stock, and C lost 200£; then B's money was double that of C's; what was the stock of each?

By the condition of this question, one half of $\frac{6}{5}$, that is, $\frac{3}{5}$ of the stock is equal to $\frac{5}{5}$ of the stock, less $200\mathcal{L}$; consequently, $200\mathcal{L}$ is $\frac{3}{5}$ of the stock.

Ans. $500\mathcal{L}$.

105. A man was hired 50 days on these conditions,—that for every day he worked, he should receive 3s. 9d., and for every day he was idle, he should forfeit 1s. 3d.; at the expiration of the time, he received 2£ 17s. 6d.; how many days did he work, and how many was he idle?

Had he worked every day, his wages would have been 3s. 9d. \times 50=9£7s. 6d. that is 2£10s. more than he received; but every day he was idle lessened his wages 3s. 9d. +1s. 3d.=5s.; consequently he was idle 10 days.

Ans. He wrought 40, and was idle 10 days.

106. B and C have the same income; B saves $\frac{1}{8}$ of his; but C, by spending $30\pounds$ per annum more than B, at the end of 8 years finds himself $40\pounds$ in debt; what is their income, and what does each spend per annum?

Ans. Their income, 200£ per annum; B spends 175£,

and C 205£ per annum.

107. A man, lying at the point of death, left his three sons his property; to $B_{\frac{1}{2}}$ wanting $20\pounds$, to $C_{\frac{1}{2}}$, and to D the remainder, which was $10\pounds$ less than the share of B; what was each one's share?

Ans. $80\pounds$, $50\pounds$, and $70\pounds$.

108. There is a fish, whose head is 4 feet long; his tail is as long as his head and half the length of his body, and his body is as long as his head and tail; what is the length of the fish?

The pupil will perceive that the length of the body is \(\frac{1}{2} \) the length of the fish.

Ans. 32 feet.

109. B can do a certain piece of work in 4 days, and C can do the same work in 3 days; in what time would both working together, perform it?

Ans. 15 days.

110. Three persons can perform a certain piece of work in the following manner: B and C can do it in 4 days, C and D in 6 days, and B and D in 5 days: in what time can they all do it together?

Ans. 3.7 days.

111. B and C can do a piece of work in 5 days; B can do it in 7 days; in how many days can C do it? Ans. 171.

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112. A man died, leaving 1000£ to be divided between his two sons, one 14, and the other 18 years of age, in such proportion, that the share of each, being put to interest at 6 per cent, should amount to the same sum when they should arrive at the age of 21; what did each receive?

Ans. The elder $546\pounds$ 3s. $0\frac{3}{4}d.+$; the younger, $453\pounds$

16s. 11d.

113. A house being let upon a lease of 5 years, at 15£ per annum, and the rent being in arrear for the whole time, what is the sum due at the end of the term, simple interest being allowed at 6 per cent?

Ans. 84£.

114. If 3 dozen pair of gloves be equal in value to 40 yards of calico, and 100 yards of calico to three pieces of satinet of 30 yards each, and the satinet be worth 2s. 6d. per yard, how many pair of gloves can be bought for 20s.?

Ans. 8 pair.

115. B C and D would divide 100£ between them, so as that C may have 3£ more than B, and D 4£ more than C; how much must each man have?

Ans. B 30£, C 33£, and D 37£.

116. A man has pint bottles, and half pint bottles; how much wine will it take to fill one of each sort? —— how much to fill 2 of each sort? —— how much to fill 6 of each sort?

117. A man would draw off 30 gallons of wine into 1 pint and 2 pint bottles, of each an equal number; how many bottles will it take, of each kind, to contain the 30 gallons?

Ans. 80 of each.

118. A merchant has canisters, some holding 5 pounds, some 7 pounds, and some 12 pounds; how many, of each an equal number, can be filled out of 12 cwt. 3 qrs. 12 lbs. of tea?

Ans. 60.

119. If 18 grains of silver make a thimble, and 12 pwts. make a teaspoon, how many of each an equal number, can be made from 15 oz. 6 pwts. of silver?

Ans. 24 of each.

120. Let 60 pence be divided among three boys, in such a manner that, as often as the first has 3, the second shall have 5, and the third 7 pence, how many pence will each receive?

Ans. 12, 20, and 28 pence.

121. A gentleman, having 50 shillings to pay among his laborers for a day's work, would give to every boy 6d., to every woman 8d. and to every man 16d.; the number of

boys, women and men, was the same; I demand the number of each.

Ans. 20.

122. A gentleman had 7£ 17s. 6d. to pay among his laborers; to every boy he gave 6d., to every woman 8d., and to every man 16d.; and there were for every boy three women, for every woman two men; I demand the number of each?

Ans. 15 boys, 45 women, and 90 men.

123. A farmer bought a sheep, a cow and a yoke of oxen for 20£ 12s. 6d.; he gave for the cow 8 times as much as for the sheep, and for the oxen 3 times as much as for the cow; how much did he give for each?

Ans. For the sheep, 12s. 6d., the cow 5£, and the oxen

15£.

124. There was a farm, of which B owned $\frac{2}{4}$, and C $\frac{15}{25}$; the farm was sold for $441\pounds$; what was each one's share of the money?

Ans. B's $126\pounds$, and C's $315\pounds$.

125. Four men traded together on a capital of $3000\mathcal{L}$, of which B put in $\frac{1}{2}$, C $\frac{1}{4}$, D $\frac{1}{6}$, and E $\frac{1}{12}$; at the end of 3 years they had gained $2364\mathcal{L}$; what was each one's share of the gain?

Ans. B's 1182£, C's 591£, D's 394£, E's 197£.

126. Three merchants companied; B furnished $\frac{2}{5}$ of the capital, C $\frac{3}{8}$, and D the rest; they gain 1250£; what part of the capital did D furnish, and what is each one's share of the gain?

Ans. D furnished $\frac{9}{40}$ of the capital; and B's share of the

gain was 500£, C's 468£ 15s., and D's 281£ 5s.

127. B, C, and D, traded in company; B put in 125£, C 87£ 10s., and D 120 yards of cloth; they gained 83£ 2s. 6d., of which D's share was 30£; what was the value of D's cloth per yard, and what was B and C's shares of the gain?

Note. D's gain being 30£ is $\frac{600}{1662\frac{1}{2}} = \frac{1200}{3325} = \frac{48}{133}$ of the whole gain: hence the gain of B and C is readily found; also the price at which D's cloth was valued per yard.

Ans. D's cloth, per yard, 1£, B's share of the gain, 31£

5s., C's share, 21£ 17s. 6d.

128. Three gardeners, B, C, and D, having bought a piece of ground, find the profits of it amount to 120£ per annum. Now the sum of money which they laid down was in such proportion, that, as often as B paid 5£ C paid 7£,

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and as often as C paid $4\pounds$, D paid $6\pounds$; I demand how much each man must have per annum of the gain.

By the question, so often as B paid 5£, D paid \$ of 7£. Ans. B 26£ 13s. 4d., C 37£ 6s. 8d., D 56£.

129. A gentleman divided his fortune among his sons. giving B 9£ as often as C 5£, and D 3£ as often as C 7£; D's dividend was 1537\(\frac{1}{2}\); to what did the whole estate amount ? Ans. 11583£ 8s. 10d.

130. B and C undertake a piece of work for 13£ 10s. on which B employed 3 hands 5 days, and C employed 7 hands 3 days; what part of the work was done by B? what part by C? what was each one's share of the money?

Ans. B 5 and C 72; B's money 5£ 12s. 6d. C's 7£

17s. 6d.

131. B and C trade in company for one year only; on the 1st of January, B put in 300£, but C could not put any money into the stock until the 1st of April; what did he then put in to have an equal share with B at the end of the year? Ans. 400£.

132. B, (, \(\infty\), and E, spent 35s. at a reckoning, and, being a little dipped, agreed that B should pay \$\frac{1}{2}\$, \$\mathbb{L}\$\$\frac{1}{2}\$, \$\mathbb{L}\$\$\frac{1}{2}\$,

and E 1; what did each pay in this proportion?

Ans. B 13s. 4d., C 10s., D 6s. 8d., and E 5s. 133. There are 3 horses, belonging to 3 men, employed to draw a load of plaister from Montreal to Stanstead, for 6£ 12s. 3d. B and C's horses together are supposed to do $\frac{3}{4}$ of the work, B and D's $\frac{9}{10}$, C and D's $\frac{13}{20}$; they are to be paid proportionally; what is each one's share of the monev?

B's 2£ 17s. 6d. (== 19..) C's 1£ 8s. 9d. $(=\frac{5}{2}]$. (D's $2\pounds$ 6s. 0d. $(=\frac{8}{2})$

Proof. 6£ 12s. 3d.

134. A person, who was possessed of 2 of a vessel, sold 4 of his share for 375£; what was the vessel worth?

Ans. 1500£.

135. A gay fellow soon got the better of \$\frac{2}{3}\$ of his fortune; he then gave 1500£ for a commission, and his profusion continued till he had but 450£ left, which he found to be just 3 of his money, after he had purchased his commission; what was his fortune at first? Ans. 3780£.

136. A younger brother received 1560£, which was just

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rht a piece £ per an $\frac{7}{12}$ of his elder brother's fortune, and 5\frac{3}{2} times the elder brother's fortune was $\frac{3}{4}$ as much again as the father was worth; what was the value of his estate?

Ans. 19165£ 14s. 33d.

137. A gentleman left his son a fortune, $\frac{b}{16}$ of which he spent in three months; $\frac{3}{4}$ of $\frac{5}{6}$ of the remainder lasted him 9 months longer, when he had only 537£ left; what was the sum bequeathed him by his father?

Ans. 2082£ 18s. 2,2,d.

138. A cannon ball, at the first discharge, flies about a mile in 8 seconds; at this rate, how long would a ball be in passing from the earth to the sun, it being 95173000 miles distant?

Ans. 24 years, 46 days, 7 hours, 33 minutes, 20 seconds: 139. A general, disposing his army into a square battal-

ion, found he had 231 over and above, but, increasing each side with one soldier, he wanted 44 to fill up the square; of how many men did his army consist?

Ans. 19000.

140. B and C cleared by an adventure at sea, 45 guinas, which was 35£ per cent. upon the money advanced, nd with which they agreed to purchase a genteel horse nd carriage, whereof they were to have the use in proportion to the sums adventured, which was found to be 11 to B as often as 8 to C; what money did each adventure?

Ans. B $104\pounds$ 4s. $2\frac{1}{19}d.$, C $75\pounds$ 15s. $9\frac{9}{19}d.$

141. Tubes may be made of gold, weighing not more than at the rate of $_{18^{12}5}$ of a grain per foot; what would be the weight of such a tube, which would extend across the Atlantic from Quebec to London, estimating the distance at 3000 miles?

Ans. 1lb. 8oz. 6pwts. $3\frac{9}{18}$ grs.

142. A military officer drew up his soldiers in rank and file, having the number in rank and file equal; on being reinforced with three times his first number of men, he placed them all in the same form, and then the number in rank and file was just double what it was at first; he was again reinforced with three times his whole number of men, and, after placing them all in the same form as at first, his number in rank and file was 40 men each; how many men had he at first?

Ans. 100 men.

143. Supposing a man to stand 80 feet from a steeple, and that a line reaching from the belfry to the man is just 100 feet in length the top of the spire is 3 times as high above

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Ans. to last, 197 feet nearly.

144. Two ships sail from the same port; one sails directly east, at the rate of 10 miles an hour, and the other directly south, at the rate of 7½ miles an hour; how many miles apart will they be at the end of 1 hour? —— 2 hours?

24 hours? —— 3 days? Ans. to last, 900 miles.

145. There is a square field, each side of which is 50 rods; what is the distance between opposite corners?

Ans. $70^{\circ}71 + \text{rods}$.

146. What is the area of a square field, of which the opposite corners are 70°71 rods apart? and what is the length of each side?

Ans. to last, 50 rods nearly

147. There is an oblong field, 20 rods wide, and the distance of the opposite corners is 33½ rods; what is the length of the field? —— its area?

Ans. Length, 262 rods; area, 3 acres, 1 rood, 131 rods.

148. There is a room 18 feet square; how many yards of carpeting, 1 yard wide, will be required to cover the floor of it?

18² = 324 ft. = 36 yards. Ans.

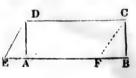
149. If the floor of a square room contain 36 square yards, how many feet does it measure on each side?

Ans. 18 feet.

When one side of a square is given, how do you find its area, or superficial contents?

When the area, or superficial contents, of a square is given, how do you find one side?

150. If an oblong piece of ground be 80 rods long and 20 rods wide, what is its area?



Note. A Parallelogram or Oblong, has its opposite sides equal and parallel, but the adjacent sides unequal. Thus, A B C D is a paralellogram, and also E F C D, and it is easy to see, that the contents of both are equal. Ans. 1600 rods,=10 acres.

151. What is the length of an oblong, or parallelogram, whose area is 10 acres, and whose breadth is 20 rods?

Ans. 80 rods.

152. If the area be 10 acres, and the length 80 rods, what is the other side?

When the length and breadth are given, how do you find the area of an oblong, or parallelogram?

When the area and one side are given, how do you find the other side

153. If a board he 18 inches wide at one end, and 10 inches wide at the other, what is the mean or average width of the board?

Ans. 14 inches.

When the greatest and least width are given, how do you

find the mean width !

154. How many square feet in a board 16 feet long, 1'8 feet wide at one end, and 1'3 at the other?

Mean width, $\frac{1.8 + 1.3}{2} = 1.55$; and $1.55 \times 16 = 24.8$ feet, Ans.

155. What is the number of square feet in a board 20 feet long, 2 feet wide at one end, and running to a point at the other?

Ans. 20 feet.

How do you find the contents of a straight edged board,

when one end is wider than the other?

If the length be in feet, and the breadth in feet, in what alenomination will the product be?

If the length be feet, and the breadth inches, what parts of

a foot will be the product?

156. There is an oblong field, 40 rods long and 20 rods wide; if a straight line be drawn frem one corner to the opposite corner, it will be divided into two equal right-angled triangles; what is the area of each?

Ans. 400 square rods = 2 acres 2 roods.

157. What is the area of a triangle, of which the base is 30 rods, and the perpendicular 10 rods?

Ans 150 rods.

158. If the area be 150 rods, and the base 30 rods, what is the perpendicular?

Ans. 10 rods.

159. If the perpendicular be 10 rods, and the area 150 rods what is the base?

Ans. 30 rods.

When the legs (the base and perpendicular) of a right-angled triangle are given, how do you find its area?

When the area and one of the legs are given, how do you

find the other leg?

Note. Any triangle may be divided into two right-angled triangles, by drawing a perpendicular from one corner to the opposite side, as may be seen by the annexed figure.

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ight-angled rner to the ture. Here, A B C is a triangle, divided into two right-angled triangles, A d C, and d B C; therefore, the whole base, A B, multiplied by one half the perpendicular d C, will give the area d A of the whole. If A B=60 feet, and d C=16 feet, what is the area?

160. There is a triangle, each side of which is 10 feet; what is the length of a perpendicular from one angle to its opposite side? and what is the area of the triangle!

Note. It is plain, the perpendicular will divide the oppo-

site side into two equal parts.

Ans. Perpendicular, 8.66+feet; arca, 43.3+ feet.

161. What is the solid contents of a cube measuring 6 feet on each side 1

Ans. 216 feet.

When one side of a cube is given, how do you find its

solid contents ?

When the solid contents of a cube are given, how do you find one side of it?

162. How many cubic inches in a brick whit a is 8 inches long, 4 inches wide, and 2 inches thick? — in 2 bricks? — in 10 bricks? Ans. to last, 640 cubic inches.

163. How many bricks in a cubic foot ? —— in 40 cubic feet ? —— in 1000 cubic feet —— Ans. to last, 27000.

164. How many bricks will it take to build a wall 40 feet in length, 12 feet high, and 2 feet thick?

Ans 25920.

165. If a wall be 150 bricks, = 100 feet, in length, and 4 bricks, = 16 inches, in thickness, how many bricks will lay one course? — 2 courses? — 10 courses? If the wall be 48 courses, = 8 feet high, how many bricks will build it? $150 \times 4 = 600$, and $600 \times 48 = 28 \times 100$, Ans.

166. The river Po is 1000 feet broad, and 10 feet deep, and it runs at the rate of 4 miles an hour; in what time will it discharge a cubic mile of water (reckoning 5000 feet to the mile) into the sea?

Ans. 26 days, 1 hour.

167. If the country, which supplies the river Po with water, be 380 miles long, and 120 broad, and the whole land upon the surface of the earth be 62,700,000 square miles, and if the quantity of water discharged by the rivers into the sea be every where proportional to the extent of land by which the rivers are supplied; how many times

greater than the Po will the whole amount of the rivers be?

Ans. 1375 times.

168. Upon the same supposition, what quantity of water, altogether, will be discharged by all the rivers into the sea in a year, or 365 days.

Ans. 19272 cubic miles.

169. If the proportion of the sea on the surface of the earth to that of land be as 10½ to 5, and the mean depth of the sea be a quarter of a mile; how many years would it take, if the ocean were empty, to fill it by the rivers running at the present rate?

Ans. 1708 years, 17 days, 12 hours.

170. If a cubic foot of water weigh 1000 oz. avoirdupois, and the weight of mercury be 13½ times greater than of water, and the height of the mercury in the barometer (the weight of which is equal to the weight of a column of air on the same base, extending to the top of the atmosphere) be 30 inches; what will be the weight of the air upon a square foot? — a square mile? and what will be the whole weight of the atmosphere, supposing the size of the earth as in questions 166 and 168?

Ans. 2109'375 lbs. weight on a square foot. 52734375000 " " mile.

10249980468750000000 " of the whole atmosphere.
171. If a circle be 14 feet in diameter, what is its circumference?

Note. It is found by calculation, that the circumference of a circle measures about 31 times as much as its diameter, or, more accurately, in decimals, 3'14159 times. Ans. 44 feet.

172. If a wheel measure 4 feet across from side to side, how many feet around it?

Ans. 124.

173. If the diameter of a circular pond be 147 feet, what is its circumference?

Ans. 462 feet.

174. What is the diameter of a circle, whose circumference is 462 feet?

Ans. 147 feet.

175. If the distance through the centre of the earth, from side to side, be 7911 miles, how many miles around it?
7911×3'14159=24853 square miles, nearly, Ans.

176. What is the area or contents of a circle, whose diameter is 7 feet, and its circumference 22 feet?

Note. The area of a circle may be found by multiplying the diameter into \(\frac{1}{2}\) the circumference. Ans. 38\(\frac{1}{2}\) sq. feet. 177. What is the area of a circle, whose circumference

177. What is the area of a circle, whose circumference is 176 rods?

Ans. 2464 rods.

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ultiplying ½ sq. feet. unference 464 rods. 178. If a circle is drawn within a square, containing I square rod, what is the area of this circle?

Note. The diameter of the circle being 1 rod, the circumference will be 3'14150, Ans. '7854 of a sq. rod nearly.

Hence, if we square the diameter of any circle, and multiply the square by '7854, the product will be the area of the circle.

179. What is the area of a circle whose diameter is 10 rods 1 10²×'7854=78'54. Ans. 78'54 rods.

180. How many square inches of leather will cover a ball 34 inches in diameter?

Note. The area of a globe or ball is 4 times as much as the area of a circle of the same diameter, and may be found, therefore, by multiplying the whole circumference into the whole diameter.

Ans. 384 square inches.

181. What is the number of square miles on the surface of the earth, supposing its diameter 7911 miles ?

7911×24853=196,612,083, Ans.

182. How many solid inches in a ball 7 inches in diameter?

Note. The solid contents of a globe are found by multiplying its area by \(\frac{1}{6}\) part of its diameter.

Ans. 1793 solid inches.

183. What is the number of cubic miles in the earth, supposing its diameter as above?

Ans. 259,233,031,435 miles.

184. What is the capacity, in cubic inches, of a hollow globe 20 inches in diameter, and how much wine will it contain, 1 gallon being 231 cubic inches?

Ans. 4188'8+ cubic arches, and 18'13+ gallons.

185. There is a round log, all the way of a bigness; the areas of the circular ends of it are each 3 square feet; how many solid feet does 1 foot in length of this log contain?——2 feet in length? ——3 feet? ——10 feet? A solid of this form is called a Cylinder.

How do you find the solid content of a cylinder, when

the area of one end, and the length are given?

186. What is the solid content of a round stick, 20 feet long and 7 inches through, that is, the ends being 7 inches in diameter?

Find the area of one end, as before taught, and multiply it by the length.

Ans. 5:347+ cubic feet.

If you multiply square inches by inches in length, what parts of a foot will the product be? —— if square inches by feet in length, what part?

187. A Winchester bushel is 1865 inches in diameter, and 8 inches deep; how many cubic inches does it contain?

Ans. 2150'4+.

It is plain, from the above, that the solid content of all bodies, which are of uniform bigness throughout, whatever may be the form of the ends, is found by multiplying the area of one end into its height or length.

Solids which decrease gradually from the base till they come to a point, are generally called *Pyramids*. If the base be a square, it is called a square pyramid; if a triangle, a triangular pyramid; if a circle, a circular pyramid or a cone. The point at the top of a pyramid is called the nertex, and a line, drawn from the vertex perpendicular to the base, is called the perpendicular height of the pyramid.

The solid content of any pyramid may be found by multiplying the area of the base by $\frac{1}{3}$ of the perpendicular height.

188. What is the solid content of a pyramid whose base is 4 feet square, and the perpendicular height 9 feet?

 $4^2 \times \frac{9}{3} = 48$. Ans 48 feet

189, There is a cone, whose height is 27 feet, and whose base is 7 feet in diameter; what is its content?

Ans. 3461 feet.

190. There is a cask, whose head diameter is 25 inches, bung diameter 31 inches, and whose length is 36 inches; how many wine gallons does it contain? —— how many beer gallons;

Note. The mean diameter of the cask may be found by adding 2 thirds, or, if the staves be but little curving, 6 tenths, of the difference between the head and bung diameters, to the head diameter. The cask will then be reduced

to a cylinder.

the content in ale or beer measure.

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eter will be multiplied by '7854, and divided, for wine gallons, by 231. Hence we may contract the operation by only multiplying by their quotient, $(\frac{7.9.54}{2.3.1} = 0.034)$; that is by '0034, (or by 34, pointing off 4 figures from the product for decimals.) For the same reason we may, for beer gallons, multiply by $(\frac{7.9.54}{2.82} = 0.028)$, nearly.) '0028, &c.

Hence this concise Rule, for guaging or measuring casks, Multiply the square of the mean diameter by the length; multiply this product by 34, for wine, or by 28 for beer, and pointing off four decimals, the product will be the content in gallons

and decimals of a gallon.

In the above example, the bung diameter, 31 in.—25 in. the head diameter = 6 in. difference, and $\frac{2}{3}$ of 6 = 4 inches; 25 in. +4 in.=29 in. mean diameter.

Then, $29^2 = 841$, and 841×36 in = 30276.

Then, $\begin{cases} 30276 \times 34 = 1029384. \text{ Ans. } 102'9384 \text{ wine gals.} \\ 30726 \times 28 = 847728. \text{ Ans. } 84'7728 \text{ beer gals.} \end{cases}$

191. How many wine gallons in a cask whose bung diameter is 36 inches, head diameter 27 inches, and length 45 inches?

Ans. 166'617.

192. There is a lever 10 feet long, and the fulcrum, or prop, on which it turns is 2 feet from one end; how many pounds weight at the end, 2 feet from the prop, will be balanced by a power of 42 pounds at the other end, 8 feet from

the prop?

Note. In turning around the prop, the end of the lever 8 feet from the prop will evidently pass over a space of 8 inches, while the end 2 feet from the prop passes over a space of 2 inches. Now it is a fundamental principle in mechanics, that the weight and power will exactly balance each other, when they are inversely as the spaces they pass over. Hence, in this example, 2 pounds, 8 feet from the prop, will balance 8 pounds 2 feet from the prop; therefore, if we divide the distance of the power from the prop by the distance of the weight from the prop, the quotient will always express the ratio of the weight to the power; \(\frac{9}{2} = 4 \), that is the weight will be 4 times as much as the power, \(42 \times 4 = 168 \).

Ans. 168 lbs.

193. Supposing the lever as above, what power would it require to raise 1000 pounds?

Ans. 100 = 250 lbs.

194. If the weight to be raised be 5 times as much as the power to be applied, and the distance of the weight from the

prop be 4 feet, how far from the prop must the power be applied?

Ans. 20 feet.

195. If the greater distance be 40 feet, and the less \(\frac{1}{2}\) of a foot, and the power 175 pounds, what is the weight?

Ans. 14000 pounds.

196. Two men carry a kettle, weighing 200 pounds; the kettle is suspended on a pole, the bale being 2 feet 6 inches from the hands of one, and 3 feet 4 inches from the hands of the other; how many pounds does each bear.

Ans. 1142 lbs. and 854 lbs.

197. There is a windlass, the wheel of which is 60 inches in diameter, and the axis, around which the rope coils, is 6 inches in diameter; how many pounds on the axle will be balanced by 240 pounds at the wheel?

Note. The spaces passed over are evidently as the diam-

ters, or the circumferences; therefore, & = 10, ratio.

Ans. 2400 pounds.

198. If the diameter of the wheel be 60 inches, what must be the diameter of the axle, that the ratio of the weight to the power may be 10 to 1?

Ans. 6 inches.

Note. This calculation is on the supposition, that there is no friction, for which it is usual to add 3 to the power

which is to work the machine.

199. There is a screw, whose threads are 1 inch asunder, which is turned by a lever 5 feet, = 60 inches, long; what

is the ratio of the weight to the power ?

Note. The power applied at the end of the lever will describe the circumference of a circle $60 \times 2 = 120$ inches in diameter, while the weight is raised 1 inch; therefore, the ratio will be found by dividing the circumference of a circle, whose diameter is twice the length of the lever, by the distance between the threads of the screw. $120 \times 34 = 3774$ circumference, and 3774 = 3774, ratio, Answer.

200. There is a screw, whose threads are 1 of an inch asunder; if it be turned by a lever 10 feet long, what weight will be balanced by 120 pounds power?

Ans. 30171 lbs.

201. There is a machine, in which the power moves over 10 feet, while the weight is raised 1 inch; what is the power of that machine, that is, what is the ratio of the weight to the power?

Ans. 120.

202. A rough stone was put into a vessel, whose capacity

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n inch ahat weight 30171 lbs . oves over the power ight to the Ans. 120. e capacity was 14 wine quarts, which was afterwards filled with $2\frac{1}{2}$ qts. of water; what was the cubic content of the stone 1

Ans. 6644 inches.

FORMS OF NOTES, RECEIPTS, ORDERS AND BILLS OF PARCELS.

SPOTUS.

No. I.

Montreal, Oct. 22, 1833.

For value received, I promise to pay to Oliver Bountiful, or order, two pounds, ten shillings and sixpence, on demand, with interest.

WILLIAM TRUSTY

Attest, TIMOTHY TESTIMONY.

No. II.

Kingston, October 10, 1833.

For value received of A B, in goods, wares and merchandize, this day sold and delivered, I promise to pay him, or bearer, — pounds, — shillings and — pence, in ten days from date, with interest.

No. 111.

By two persons.

Stanstead, October 1, 1833.

For value received, of _____, in ____ this day sold and delivered, we jointly and severally promise to pay him, or order, ____ pounds, ____ shillings and ____ pence in ____, days from date, with interest. B____ C____, D___ E____.

RECEIPTS.

Montreal, October, 10, 1833.

Received from Mr. Durance Adley ten pounds, in full of

all accounts.

ORVAND CONSTANCY.

Receipt for money received on a Note.

York, November 1, 1833.

Received of Mr. Simon Eastly (by the hand of Titus Trusty,) sixteen pounds ten shillings and six pence, which is endorsed on his note of June 3, 1831.

X 2

SAMSON SHOW.

A Receipt for money received on Account.

Stanstead, June 2, 1833. Received of Thomas Dubois twenty pounds, on account. ORLANDO PROMPT.

Receipt for money received for another person.

Sherbrooke, June 4, 1833. Received from P. D. twenty-five pounds for account of ELI TRUMAN. J. T.

Receipt for interest due on a Note.

Quebec, December 12, 1833. Received of I. S. fifteen pounds, in full of one year's interest of 250£, due to me on the — day of — last, on note from the said I. S. SOLOMON GRAY.

Receipt for Money paid before it becomes due.

Prescot, May 3, 1833. Received of T. Z. fifteen pounds, advanced in full for one year's rent of my farm, leased to the said T. Z. ending the first day of April next, 1834. JOHN HONORUS.

ORDINA.

Belville, November 3, 1833. Mr. Stephen Girard. For value received, pay to A B, or order, five pounds and six shillings, and place the same to my account. SAUL MAZE.

Montreal, September 1, 1830. Mr. TINOTHY TITUS. Please to deliver to Mr. L. D. such goods as he may call for, to the amount of seven pounds, and place the same to the account of your obedient servant. NICAMOR LINUA.

BLLS OF PARCELS.

It is usual when goods are sold for the seller to deliver to the buyer, with the goods, a bill of the articles, and their price calle

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er to their prices, with the amount cast up. Such bills are sometimes called bills of parcels.

Montreal, 6th May, 1833.

Mr. ABEL ATLAS.

Bought of BENJ. BUCK.

124 yds. figured Satin, at 12s. 6d. per yd. 7 . 16 . 3

" Sprigged Tabby, - 6s. 3d. -- 2 - 10 - 0

£10 · 6 · 3 Received payment, BENJ. BUCK.

Montreal, 14th May, 1833.

Mr. JOHN BURTON,

Bought of GEORGE WILLIAMS,

3 hogsheads new Rum, 118 gal. each, at Is. 6d. per gal. 2 pipes French Brandy, 126 & 132 gal. " 5s. 7d.

I hogshead brown Sugar, 93 cwt. " 2£ 11s. 9d. ewt.

3 casks of Rice, 269th. each, "

5 bags Coffee, 75lb. each, 1s. 2d. " I chest hyson Tea, 86lb. 48. 8d. 14

> Received payment, 111£ 6s. 7ad. For GEORGE WILLIAMS, THOMAS ROUSSEAU.

> > Wilderness, 8th Feb. 1833.

Mr. SIMON JOHNSON,

Bought of Asa Fullum,

5682 feet Boards, at 1£ 10s. per M. 2000 " 2£ 1s. Sd. "

" Stuff, 800 "3 . 3 . 2 . "

1500

650

" Timber, " 12 . 6 . " 879

-236 et ... 13 . 9 . "

18£ 8s. ≩d.

BOOK - KRRRLINGS.

this method shall be, the law does not prescribe; but in cases of dispute it requires that the several items of It is necessary that every man should have some regular uniform method of kéeping his accounts. the account be proved to have been sold and delivered.

For farmers and mechanics, the following method will he found both convenient and easy. It consists in having one single book, entering the name of the person, with whom an account is to be opened, at the top of the 19th hand page, Dr.; and at the top of the right hand page, his place of residence, and Cr. as follows:

LENOX VILLE,	at 8s. 9d 2 3 9 April 8. By 1 Plough, 7 6 May 19. By repairing Cart Wheels, 7 6 May 19. By repairing Cart Wheels, 12 6 at 3s. 9d. deliv. 15 8ept 12. By Cash to balance, 15 8 3 3
Dr. JAMES MACKEY,	Jan. 4. Jan. 4. May 5. To 1 day's work, self and oxen, July 20. To 4 bushels of Rye, at 3s. 9d. delivered by your order to C. D.

JOHN FORE, MINISTER	The same of the sa
Jan. 24. To 22 tons of Hay, at 2.2 per ton, 29. By 14 bushels of Corn, at 2s. 6d.	2 8 8 4 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8

Jan. 24. To 22 tons of Hay, at 2.2 per ton, 29. By 14 bushels of Corn, at 2s. 6d. Feb. 2, To 30 lbs. of Flax, d'd. by your order to A B, at 7.4d. 6. By Cash, to balance,
14 bushels of Corn, at 2s. 6d. 15 bushels of Corn, at 2s. 6d. 16 bushels of Flax, d'd. by your order to A B, at 74d. 17 Cash, to balance,
14 bushels of Corn, at 2s. 6d. 15 bushels of Corn, at 2s. 6d. 30 lbs. of Flax, d'd. by your order to A B, at 74d.
14 bushels of Corn, at 2s. 6d. 15 bushels of Corn, at 2s. 6d. 18 bushels of Flax, d'd. by your order to A B, at 73d. 18 Cash, to balance,
22 tons of Hay, at 2.c per ton, 14 bushels of Corn, at 2s. 6d. 30 lbs. of Flax, d'd. by your order to A B, at 73d. 7 Cash, to balance,
22 tons of Hay, at 2.2 per ton, 14 bushels of Corn, at 2s. 6d. 30 lbs. of Flax, d'd. by your order to A B, at 7.4d. 7 Cash, to balance,
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